Dr. Oda Schmalwasser, Michael Schidlowski

## Measuring Capital Stock in Germany

## Slightly abridged version of a paper published in the journal Wirtschaft und Statistik 11/2006

This treatise describes calculations of fixed assets or capital stock and consumption of fixed capital in the context of national accounts in Germany. To start with, we explain the terms used, followed by an overview of fixed assets and consumption of fixed capital estimations, and then we present the Perpetual Inventory Method as the principal method used. We explain both the mathematical model applied in Germany and the computational implementations based on Excel and Visual Basic for Applications. The treatise ends with a description of the data base and the results of capital stock and consumption of fixed capital estimations that were obtained in the context of the 2005 revision of national accounts and the 2006 backward calculations.

#### **Preliminary note**

Gross domestic product is the central value of national accounts. In Germany the Federal Statistical Office determines it by way of reconciling production and expenditure approach data. As data on business profits are not available, it is not possible to use the income approach in order to determine gross domestic product or gross national income. In contrast, the United States uses the income approach as a central method to calculate gross domestic product and gross national income. Work is in progress there to elaborate a self-contained production approach.<sup>1</sup> The setting of different priorities regarding the determination of central values in national accounts is a common feature of all esti-

mations up to the calculation of assets and liabilities, which conclude the system of accounts with balance sheets. Fixed assets or capital stocks are in the focus of the calculation of assets and liabilities and the way they change is the most important indicator of the extent to which production activity increases national wealth and creates, at the same time, the conditions needed to continue the production of goods and services in future. Unlike the United States, which determines fixed assets in net terms only as required for balance sheet calculations, Germany has pursued an integrated approach of determining fixed assets in both gross and net terms since the early 1970s, when capital stock calculations started. That means that fixed assets are determined not only in net terms as the current value of the capital stock, which is important for balance sheet calculations, but also in gross terms as a measure needed for the analysis of productivity and incorporating the capital stock's production capacity.

As the main focus of capital stock examinations has been on fixed assets in net terms, productivity analysis at international level has basically relied on the "capital services" concept in recent years.<sup>2</sup>) The term "capital costs" ("Kapitalkosten"), introduced in German, correctly includes the financing and distribution aspect, but does not cover the production or value added aspect, which has been read into it concerning its recommended use for productivity examinations. This treatise shows that conventional German

See Lawson, A./Moyer, B./Okubo, S./Planting, M.: "Integrating Industry and National Economic Accounts" (http://www.oecd.org/dataoecd/6/41/33871180.ppt; as of: 7 November 2006) and the paper by Moyer, B./Planting, M./Fahim-Nader, M./Lum, S., on which this presentation was based at the OECD Working Party meeting on national accounts in 2004: "Preview of the Comprehensive Revision of the Annual Industry Accounts: Integrating the Annual Input-Output Accounts and the Gross-Domestic-Product-by-Industry Accounts" (http://www.oecd.org/ dataoecd/42/18/33765748.pdf; as of: 7 November 2006).

<sup>2)</sup> See OECD (ed.): "Measuring Capital", OECD Manual, 2001.

fixed assets calculations represent an integrated approach to the calculation of both the capital stock's current value, on the one hand, and of the capacities available for production purposes, on the other hand, in a way that is consistent with the formats in which the gross domestic product is displayed. That is why this treatise places emphasis mainly on the coherent presentation and explanation of the Federal Statistical Office's methods of calculation used to determine fixed assets or capital stocks. In conclusion, we shall explain the database used and the results obtained by the calculations made in the context of the 2005 revision of national accounts for Germany regarding the years 1991 to 2004 and of the 2006 backward calculation for the years 1970 to 1991 relating to the former federal territory.

#### 1 Definition of fixed assets and capital stock

The terms "Kapitalstock" and "fixed assets" are often used synonymously in German and they are also used synonymously with the English term "capital stock". A definition of the terms used is imperative, as we are faced with concepts, such as (stocks of) fixed assets in gross and net terms apart from different price concepts, "gross" and "net capital stock" as well as "wealth" and "productive capital stock". It is the only way to avoid ambiguities caused by different meanings assigned to one and the same concept. Microeconomic issues are not considered here. The definitions are based on the internationally agreed concepts of national accounts. They provide the definitions and explanatory methodological notes that statistical offices use as a basis for their measurement concepts. Accordingly, (stocks of) fixed assets comprise all produced fixed assets that are used repeatedly, or continuously, in processes of production for more than one year. They include tangible and intangible assets. Tangible fixed assets consist of the stock of machinery and equipment, residential and non-residential buildings, and cultivated assets. Intangible fixed assets comprise mineral exploration, computer software and large databases as well as entertainment, literary or artistic originals.

In order to characterise capital stocks and fixed assets it is very important to distinguish between flows and stocks, a distinction made both by the 1993 System of National Accounts (SNA) of the United Nations and by the 1995 European System of Accounts (ESA). "Flows reflect the creation, transformation, exchange, transfer or extinction of economic value. They involve changes in the value of ... assets or liabilities."<sup>3</sup>) The gross domestic product and most of the other national accounts variables are flows that relate to a period of time. "Stocks are holdings of assets and liabilities at a point in time. Stocks are recorded at start and end of each accounting period. The accounts that show stocks are called balance sheets. Stocks are also recorded for population and employment. However, these stocks are recorded as mean values over the accounting period."<sup>4</sup>) Stock of fixed assets means a holding of assets, it therefore is a value measured at a point in time. "Flows refer to actions and effects of events that take place within a given period of time, while stocks refer to positions at a point of time."<sup>5</sup>)

A combination of data on stocks and flows is methodologically problematic, because stocks of fixed assets relate to a moment of time, whereas flow data refer to a period of time. If we wish to calculate capital productivity similar to labour productivity, we must make sure that the other production factor is subject to the same procedure as is laid down for employment (and the population) in the ESA-95 (see above): We must generate an annual average. Average annual gross fixed assets at constant prices are traditionally referred to as *Kapitalstock* in Germany's national accounts. Kapitalstock calculations provide us with the methodologically correct tools needed to determine capital productivity as gross domestic product per unit of capital stock, capital output ratios as their reciprocal value and capital intensity as capital stock per employed person (as an annual average). Although international concepts do not provide for such calculations, they are, nevertheless, methodologically exact. However, the German word "Kapitalstock", which is used to denote this annual average, often gives rise to misunderstandings caused by confusion with the English term "capital stock", which means a stock figure related to a point of time.

However, neither the SNA nor the ESA use a term such as "capital stock". Depreciation is exactly referred to as "consumption of fixed capital" and investments as "gross fixed capital formation", but stocks do not provide for a term such as "capital stock", but only for "stocks of fixed assets". The reason is that according to the SNA and the ESA not all gross fixed capital formation actually increases fixed assets.<sup>6</sup>) Both major improvements to non-produced non-financial assets and the costs of ownership transfer on non-produced non-financial assets as part of gross fixed capital formation are referred to as additions to the value of non-produced non-financial assets. The name says it already: This part of gross fixed capital formation does not increase the value of fixed assets, but adds to the value of non-produced non-financial assets (in particular, land). This approach may be reasonable from the perspective of fixed assets, but it has the undesirable side effect that gross fixed capital formation, fixed assets and consumption of fixed capital are defined differently: Fixed assets do not include additions to the value of non-produced non-financial assets, i.e. additions, which are included in gross fixed capital formation and need to be written off as consumption of fixed capital. Now the "capital stock" concept used by the OECD manual

<sup>3)</sup> Annex A to Council Regulation (EC) No. 2223/96 of 25 June 1996 on the European System of National and Regional Accounts in the European Community (Official Journal of the EC No. L 310, p. 1), section 1.32.

<sup>4)</sup> Ibid., section 1.47.

<sup>5)</sup> Ibid., section 1.31.

<sup>6)</sup> A detailed comparison of the classification of fixed assets and gross fixed capital formation can be found in Schmalwasser, 0.: "Revision der Anlagevermögensrechnung 1991 bis 2001" in WiSta 5/2001, p. 344.

on "Measuring Capital"<sup>7</sup>) establishes a connection between gross fixed capital formation and consumption of fixed capital by applying exactly the same definition to the different types of assets, which are subject to capital consumption (see chart 1). Coverage and classification of capital stock by type of asset, considered in this manual, show that they are composed of fixed assets, on the one hand, and major improvements to non-produced non-financial assets and costs associated with the transfer of ownership on non-produced non-financial assets as part of non-produced (tangible) assets, on the other hand.<sup>8</sup>)

"Capital stock", in German "*Kapitalstock*", is used in this treatise in the same way as in the OECD definition of "capital stock". The traditional German "Kapitalstock" described above is additionally specified as "annual average", which has also been done for some time in the Federal Statistical Office's English translations of publication tables in order to avoid misunderstandings.

Judging on the present course of discussions, the revision of the SNA 1993, which is to be completed by 2008, is expected to put an end to the practice that different definitions are applied to gross fixed capital formation and consumption of fixed capital, on the one hand, and fixed assets, on the other hand. Then all parts of gross fixed capital formation will be included in fixed assets as well and all assets actually produced will be covered as produced assets. With Germany's transition to the ESA-95, the costs of ownership transfer on unimproved land were not considered to be constituent parts of fixed assets, whereas land improvements, as in the past, were recorded under buildings. Two different approaches to the calculation of fixed assets and consumption of fixed capital were used to calculate total consumption of fixed capital: consumption of fixed capital in the context of calculating domestic product, including charges equivalent to the consumption of accumulated costs of ownership transfer on unimproved land, on the one hand, and in the context of the calculation of assets and liabilities excluding the latter ones, on the other hand. With the 2005 revision of national accounts and anticipating a revision of the SNA, this duplicate approach was abandoned and accumulated costs of ownership transfer on unimproved land were included in fixed assets as well. Strictly speaking, Germany's fixed assets are now equivalent to capital stock in terms of the OECD manual. We have deliberately accepted a slight deviation from the ESA concepts presently in force, because the cost of ownership transfer on land is a relatively insignificant component of total fixed assets.

# 2 Overview of the calculation of fixed assets and consumption of fixed capital

## 2.1 Gross and net approach and consumption of fixed capital

The way in which capital stock estimations are presently organised in Germany arises from the traditional approach of the Federal Statistical Office<sup>9</sup>) to such calculations and from the requirements of the data transmission programme under the ESA 1995.<sup>10</sup>) Besides the obligatory transmission of fixed assets data, a point of great importance is the supply of data on consumption of fixed capital. *Consumption of fixed capital* in national accounts measures the amount

Chart 1: Definition of gross fixed capital formation, fixed assets, consumption of fixed capital and capital stock
based on the SNA and ESA classification

Gross fixed capital formation P.51	Fixed assets AN.11	Consumption of fixed capital K.1	Capital stock (OECD Manual)
P.511 Acquisitions less disposals of tangible fixed assets	AN.111 Tangible fixed assets	To be calculated with respect to tangible fixed assets	Tangible fixed assets
P.512 Acquisitions less disposals of intangible fixed assets	AN.112 Intangible fixed assets	To be calculated with respect to intangible fixed assets	Intangible fixed assets
P.513 Additions to the value of non- produced non-financial assets, of which P.5131 Major improvements to non-financial non-produced assets P.5132		To be calculated with respect to major improvements to and costs of ownership transfer on non-financial non-produced assets	Major improvements to and costs of ownership transfer on non-financial non-produced assets as parts of non- produced assets
Costs of ownership transfer on non- financial non-produced assets	<b>†</b>		

Component of AN.2 non-produced assets

<sup>7)</sup> See footnote 2.

<sup>8)</sup> Ibid., p. 23 and p. 25 f.

<sup>9)</sup> See Lützel, H.: "Das reproduzierbare Anlagevermögen in Preisen von 1962" in WiSta 10/1971, p. 593 ff., and Lützel, H.: "Das reproduzierbare Sachvermögen zu Anschaffungs- und zu Wiederbeschaffungspreisen" in WiSta 11/1972, p. 611 ff.

<sup>10)</sup> See Annex B of the ESA regulation, footnote 3.

of fixed assets used up during the period under consideration as a result of normal wear and tear and foreseeable obsolescence including a provision for losses as a result of accidental damage which can be insured against. This calculation is done for all fixed assets, including both tangible fixed assets and intangible fixed assets such as mineral exploration costs and software. Animals are excluded by definition. Land improvement costs are not separately determined in Germany. They are included in buildings and structures. Costs of ownership transfer on unimproved land are written down as consumption of fixed capital together with the respective types of buildings. That is why calculations of fixed assets and consumption of fixed capital form a unity.

According to the ESA transmission programme, the stock of fixed assets is to be recorded both in gross terms and net terms, in either case at current replacement costs and constant replacement costs. Registration at historic cost value is voluntary and done in line with the valuation principles of microeconomic and fiscal balance sheets. Gross approach means that fixed assets are recorded as part of fixed assets at full value (current market prices of new fixed assets of a corresponding quality) without consideration of the decline in an asset's value by the time when these fixed assets retire from the production process. This is done in consideration of the fact that the production process makes use of all fixed assets irrespective of their age and that the output achieved is more or less the same every year, provided that fixed assets are maintained and repaired regularly. For instance, a 500 MW power generating unit produces these 500 MW as long as it is connected to the power grid even after 20 years, when most of its value will have been written off as consumption of fixed capital. That is why the stock of gross fixed assets is a suitable value for the analysis of production processes.

In balance sheets, however, fixed assets are to be valued at market prices (current market value) at the time to which the balance sheet relates. Since, in most cases, there are no market prices for existing fixed assets of different age other than motor vehicles, the net approach provides for a deduction of the amount that has been written off as consumption of fixed capital since the date of investment.<sup>11</sup>) This is a good compromise that reconciles what is desirable in theory with what is feasible in practice. Accordingly, the net capital stock corresponds to the current value of the fixed assets measured in terms of the fixed assets' current market value.

#### 2.2 Price concepts

Three price concepts are used in fixed assets calculations:

- current replacement costs,
- constant replacement costs, and
- historic cost value.

The above distinction is required, since the capital stock is composed of individual pieces of fixed assets, which were acquired in different years and which can be summed up in different ways. Using a perpetual inventory method which is based on the (original) acquisition prices that were actually paid in a given year of investment, one speaks of historic acquisition prices or historic cost value, which best agree with an enterprise's bookkeeping data. This method has the disadvantage that fully identical fixed assets are likely to be included in the accounts with completely different acquisition prices, just because these goods were acquired in different years and purchaser's prices changed between these years. The result of this calculation at historic cost for different years of acquisition has nothing to do with the current prices commonly used for flows, which relate to one reporting year, even if the calculation as such is based on current prices of gross fixed capital formation. In order to convert the stock at historic acquisition prices into one year's prices, we would need to make sure that the yearly proportions of fixed capital formation related to the total stock of assets are available in a detailed breakdown by type of assets and that the respective price indices are obtainable as well. This would allow us to construct a weighted average based on the price indices for all fixed assets acquired in all years, which would be much too expensive a procedure to be used. The Federal Statistical Office has abandoned this price concept for capacity reasons. Although this concept complies with the valuation techniques applied by businesses' bookkeeping systems, one should note that the values recorded for fixed assets at historic acquisition prices in net terms are not comparable, because the methods used to calculate consumption of fixed capital are very different.

Before the Perpetual Inventory Method is used in capital stock calculations, gross fixed capital formation data relating to different years are brought into a comparable form, which is done by using series of investment data at constant prices. As a result we obtain fixed assets data at constant prices of one reporting year, i.e. at constant replacement prices (costs). The data on the stock of fixed assets defined in that way and on the related decline in value by way of consumption of fixed capital comply with the concept of constant prices applied in national accounts, which means that the entire stock of all fixed assets is valued at prices of one reference year or at base-year prices. To obtain the current replacement prices (costs) of a given year under consideration, we revaluate the stock, which was consistently valued at base-year prices, into prices of the respective year under consideration with respect to all years. All that now is still needed is data on the price indices of the year under consideration (related to the base year), broken down into detailed items of fixed assets. Hence, current replacement prices (costs) for fixed assets correspond to current prices for flows in national accounts, since all fixed assets are valued at prices of that one year under consideration as are all other flow data, so that we have a real match. This relates, in particular, to the data on consumption of fixed capital at current prices, which are determined by using this method. The-

<sup>11)</sup> See ESA 1995, sections 7.29 and 7.33.

oretically, it would even be possible to revaluate all series of gross fixed capital formation data for every year under consideration into the prices of one specific year under consideration and to use the Perpetual Inventory Method later on, but that is an extra effort we spare by calculating the prices for one base year only and revaluating the results for all years under consideration.

The transition from constant prices to previous year's prices with chaining in national accounts brought about a methodological problem in the calculation of fixed assets, since price changes are correctly recorded only in relation to the previous year, but not in relation to the reference year. Constant prices, in their turn, correctly reflect the changes in prices between the reporting year and the base-year of price registration, but they are of restricted use for the measurement of year-to-year changes in prices, because weighting varies. Since the constant price approach corresponds to the approach used to cumulate gross fixed capital formation, constant prices continue to be used for the calculation of stocks of fixed assets and consumption of fixed capital. On this basis it is even possible to generate data at previous year's prices by applying the price indices that were used to revaluate data into current or replacement prices. For that purpose we must additionally convert the values at constant (replacement) prices into values at previous year's prices, which is done by using the price indices of the previous year. This method is actually used to calculate consumption of fixed capital as a flow item. However, if the stock of fixed assets is related to a concrete date, we are faced with additional methodological problems caused by the prices that must also relate to that date. For that reason we do not presently show the stock of fixed assets by chaining year-to-year data.

That is why, in order to show *capital productivity*, we use data on gross domestic product or gross value added at current prices and average capital stock for a year at current replacement prices. Relating chained data on gross domestic product or gross value added to a year's average capital stock at constant replacement prices is not a methodologically perfect solution. However, taking into account that the structure of fixed assets does not change considerably from year to year, the difference between constant prices and chained prices is practically negligible. That means that we can even tolerate such an approach, although it is not perfect from a methodological point of view.

#### 2.3 Multidimensionality of calculations

The ESA transmission programme provides for a cross classification of fixed assets by 31 industries and three types of fixed assets. Much more information is required – directly or indirectly – with respect to consumption of fixed capital. This is mainly due to the fact that consumption of fixed capital by other non-market producers of general government (sector S.13) and non-profit institutions serving households (S.15) has an influence on the size of gross domestic prod-

uct and gross national income. The output of other non-market producers is determined as total production costs and consumption of fixed capital is one component of these costs.<sup>12</sup>) That is why we need to determine consumption of fixed capital in the required detail by industry and government subsector, i. e. federal (central) government (S.1311), state government (S.1312), local government (S.1313) and social security funds (S.1314), in order to arrive at gross value added of other non-market producers. In addition, we need consumption of fixed capital of market producers for the sector accounts of the government sector by subsector, of non-profit institutions serving households, financial corporations (S.12) by subsector, non-financial corporations (S.11) and households (S.14) as well as total consumption of fixed capital for the sectors in total.

That means that calculations of fixed assets and consumption of fixed capital must have a multidimensional structure. Major dimensions such as industries, type of fixed assets and sectors/subsectors are shown in fig. 1. As a first step this presentation starts with a cross-classification by industry and type of fixed assets. In Germany we need not make an extra distinction between market and non-market producers, because this differentiation is completely available - with one exception - in terms of industries and subsectors (see section 4.1, chart 2). It should be noted that by far not all fields of the multidimensional matrix are filled with data. But for every field that is filled with data we need to have long series of data on gross fixed capital formation and a good's service life (distribution), which varies over time (see chapters 3 and 4). That means that two more dimensions are added to the calculations.

### 2.4 Perpetual Inventory Method and elements of the direct method

As no comprehensive direct data is available on the stock of fixed assets in Germany, the main method of calculating fixed assets and consumption of fixed capital is the Perpetual Inventory Method (PIM), which is recommended by the ESA. The details of this method are explained in chapter 3. In addition, we also use elements of the direct method in Germany:

- The calculation of cultivated assets is based on annual data of agricultural statistics on livestock and cultivated areas. This data on stocks and areas is valued, using the average weights and prices of a given calendar year (current replacement costs) and those of the year 2000 (constant replacement costs), which are provided by agricultural accounting. According to the ESA-1995 livestock is not written off, so that in this case net assets are equal to gross assets.
- Information on the stocks inherited from the ex-GDR is based on annual fixed assets reports and reports on the material, technological and age structure of the GDR's fixed assets, i.e. on direct statistical records about the

<sup>12)</sup> See also ESA 1995, section 3.53.



Fig. 1

stock of fixed assets. These stocks were separately determined on this basis, but comprehensive adaptations were required, since what we needed for the calculation was only the part that was still in use for production purposes after transition from planned to market economy, rather than the entire stock of the ex-GDR's fixed assets. For example, assets that proved to be useless under market conditions by the end of 1992 were excluded from the initial stock of inherited fixed assets, determined as of 1 July 1990. The stocks of fixed assets inherited by the new federal states as of the beginning of 1991 were added to the initial stocks obtained by using the Perpetual Inventory Method. Write-offs and retirements were calculated well in advance and must annually be taken into account for inherited stocks.<sup>13</sup>)

 The ESA-1995 stipulates that changes caused by exceptional incidents, which do not comply with the original assumptions made by the perpetual inventory method, are recorded as other changes in the volume of fixed assets. Various cases of special retirements (withdrawals from the stock before the end of assumed service life) are recorded for fixed assets under this item, including the repercussions they have on consumption of fixed capital and retirements resulting from PIM, described in section 4.3.

Accordingly, the stock of fixed assets in gross and net terms recorded at start of 1991 for Germany as a whole consists of the following items:

- Stock of fixed assets at start of 1991, obtained by using the perpetual inventory method
- + Stock of cultivated assets at start of 1991
- + Stocks of inherited fixed assets of the ex-GDR at start of 1991

<sup>13)</sup> On the inclusion of inherited stocks from the former GDR see section 1.2.3 in Schmalwasser, O., footnote 6, here: p. 347.

- Accumulated special retirements and their counterpart entries for the former federal territory until and including 1990
- = Stock of fixed assets at start of 1991 for Germany as a whole

Consumption of fixed capital and retirements are determined analogously, which is shown here using consumption of fixed capital as an example:

Consumption of fixed capital obtained by using the perpetual inventory method

- + Consumption of old fixed capital which is further used by the new federal states
- Counterpart entries to consumption of fixed capital corresponding to other changes in the volume of fixed assets
- = Total consumption of fixed capital

Then the flows connected with fixed assets, which were determined in this way, and the stocks of fixed assets for Germany relating to the start of 1991 are used as the basis on which the stocks of fixed assets are determined for the years to come as follows:

Gross stock at start of year

- + Additions to fixed assets
- Retirements of fixed assets
- = Gross stock at end of year (= gross stock at start of the following year)

In the calculation of gross assets, entries for special retirements in conjunction with other changes in the volume of assets are recorded in the other changes in the volume of assets account according to the basic pattern described above and are included in retirements. Net assets, however, require other changes in the volume of assets to be considered separately, because these changes cannot be recorded as special consumption of fixed capital:

Net stock of assets at start of year

- + Additions to fixed assets
- Consumption of fixed capital
- Other changes in the volume of assets (net)
- Net stock of assets at end of year (= net stock at start of the following year)

Backward calculations of fixed assets and consumption of fixed capital for 1970 – 1991 regarding the *former federal territory* are also based on the stock at start of 1991. For that purpose we determine the stock at start of 1991 for the former federal territory according to the basic pattern described above. In so doing, we must leave out of account not only the inherited, old stocks of the former GDR. We must also exclude the respective East-German data from the stock of cultivated assets at start of 1991, and we must take into account that the data on the stock at start of year, which were obtained by using the perpetual inventory method, already include the new federal states' fixed capital formation for the second half of 1990 (after the introduction of DM on 1 July 1990). That means that we must exclude the respective parts of fixed capital formation, when calculating the stocks for the former federal territory at start of 1991. Accordingly, we must take into account the resulting consumption of fixed capital for 1990 in order to determine the 1990 consumption of fixed capital for the former federal territory. The influence on retirements in 1990 can be neglected. On that basis we effect a "real" backward calculation of the former federal territory's fixed assets as shown below, using the gross stock as an example:

Gross stock of fixed assets for the former federal territory at start of year

- Additions to the previous year's fixed assets
- + Retirements from the previous year's fixed assets
- Gross stock for the former federal territory at start of previous year

#### 3 Use of the Perpetual Inventory Method in Germany

#### 3.1 Brief outline of the Perpetual Inventory Method

As outlined in section 2.4, the Perpetual Inventory Method (PIM) is the main method used to determine fixed assets and consumption of fixed capital in Germany. This approach is based on the idea that today's stock of fixed assets is composed of assets that were added to the stock at some time in the past. Taking into account the service life of fixed assets, we can calculate the percentage of assets added in past years, which are still operational in the stock at start of the year under consideration, and determine the time when these assets will be withdrawn (retire from the stock). If the depreciation method is applied, we can use this information to derive data on consumption of fixed capital for every reference period. The use of the Perpetual Inventory Method requires the following conditions to be fulfilled: (1) data series on gross fixed capital formation are available, which reach far back into the past, (see section 4.1) and (2) it is possible to estimate the average service life for the various types of fixed assets (see section 4.2).

The *average* (economic) service life is estimated for all goods which are subject to consumption of fixed capital. This is done, assuming normal wear and tear and foreseeable obsolescence as a result of technological progress. The estimation also covers the risk of losses due to insurable accidental damage. As it is unrealistic to assume that all goods with the same average service life and added in the same year will also retire at the same time, we use a mortality



(*retirement*) *function* to distribute retirements so that they scatter around the average service life in a roughly bell-shaped manner (see section 3.2).

Fig. 2 schematically outlines the use of the perpetual inventory method for the calculation of fixed assets and consumption of fixed capital. This description clarifies the essential points of the method used:

- To begin with, we need some basic information, including long-term series of data on gross fixed capital formation (at constant prices for calculations at constant and current prices), approaches to service life determination and corresponding price indices for the various fixed assets needed for calculations at current price, provided that the depreciation method and the distribution of retirements are taken for granted.
- Consumption of fixed capital is calculated in a self-contained way, which does not require fixed assets to be calculated in an intermediate step ("inner circle").
- Any deviations from the normal economic trend that this model imputes can be recorded as other changes in the

#### 3.2 Mathematical model

The mathematical model used to implement the perpetual inventory method in Germany is designed so that the flow data, i.e. retirements and consumption of fixed capital, can directly be derived from the two pieces of basic information needed for the calculation of fixed assets, i.e. gross capital formation and service life of the various fixed assets. To describe the model<sup>14</sup>), we use the following standardised symbols:

- i : investment year
- t : (current) reporting year
- n : service life in years
- ñ : average service life

volume of assets (see section 4.3). This item enables us to ensure that exceptional, unanticipated events, which have an impact on the value of fixed assets and, as a later consequence, on the size of consumption of fixed capital, are included in the calculation.

- I<sub>i</sub> : additions of year *i*
- I<sub>in</sub> : additions of year *i* with service life *n*
- $f_{\tilde{n}}(n) \ :$  mortality function of gross fixed capital formation
- a, p : dilation parameter of the gamma distribution
- $A_t$  : retirements in the reporting year t
- $d_t(n)$  : depreciation function
- D<sub>t</sub> : consumption of fixed capital in the reporting year *t*

In Germany we use the *density function of the gamma distribution* to calculate the distribution of retirements. The choice of this function was based on empirical data of motor vehicle registration. In Germany we do not have a statistical basis as regards the actual service life of other groups of fixed assets. The gamma function provides the best approximation to the real retirements of vehicles, distributed around the average service life:

 $\phi(n/a, p) = a^p \Gamma(p)^{-1} n^{p-1} e^{-an}; n \ge 0, a > 0, p > 0$ 

Parameters a and p determine, inter alia, the steepness of the mortality function. The curve is the steeper, the higher these dilation parameters are. Dilation parameter 9 was assumed to be suitable for most goods. It ensures results most closely approximating past evaluations regarding retirements of vehicles. Adopting parameter 9 as the normal case, we obtain a mortality function as follows:

$$f_{\tilde{n}}(n) = 9^{9}(8!)^{-1} \tilde{n}^{-9} n^{8} e^{-\frac{9n}{n}}$$

Fig. 3 displays the curve progression of a mortality function related to an average service life of 10 or 20 years.



The retirements of the reporting year *t* are obtained as the sum of assets added during the past years *i* and having a service life of n = t - i years:

$$A_t = \sum_{i < t} I_i \cdot f_{\widetilde{n}} n(t-i)$$

Now it is possible to derive the *depreciation function* directly from the mortality function. The method used is straight line depreciation in accordance with a recommendation made by the ESA-1995. The depreciation rate in the investment year and in the year of retirement is just half as high as in the intermediate years. This is based on the assumption that in the first and last years the assets are included in the stock for half a year on average.

$$d_t(n) = \frac{1}{2n} \text{ for } t = i \text{ and } t = i + n,$$
$$d_t(n) = \frac{1}{n} \text{ for } i < t < i + n$$

As this function only considers goods which are still included in the stock and which have already been calculated by way of the mortality function, we can directly calculate consumption of fixed capital without having to determine the size of stocks. Due to the proportions of retirements already considered we obtain a non-linear function for the depreciation curve, as fig. 4 shows, displaying the distribution of consumption of fixed capital with respect to goods having an average service life of 10 or 20 years. Although straight line depreciation is used, the data obtained as a result of distributing consumption of fixed capital approximate those obtained by way of geometric depreciation, which is used, inter alia, by the United States. This results from the fact that straight line depreciation follows the real service life of the assets, for which consumption of fixed capital is measured, whereas according to the mortality function some of





the goods that were acquired in an investment year were already withdrawn from the stock after a short span of time (long before reaching the average service life of the respective group of assets).

We obtain a reporting year's consumption of fixed capital for assets added in a given investment year by multiplying the respective share of depreciation with the value of gross fixed capital formation. The following applies to consumption of fixed capital in the reporting year t related to the additions of the year i:

$$D_{i,t} = I_i \sum_{n \ge t-i} d_t(n) \cdot f_{\tilde{n}}(n)$$

Consumption of fixed capital in the reporting year *t* is obtained as the sum of consumption of fixed capital for the various years of fixed capital formation:

$$D_t = \sum_{i \le t} D_{i,t}$$

#### 3.3 IT solution

The software system for the perpetual inventory method was originally programmed on a mainframe platform in the late 1970s. At the end of the 1990s, when the shutdown of the system was imminent, we had to think about alternative IT tools that could be used to handle the complex computations required. A problem of the mainframe variant was the scarcity of available storage space, which had the effect that it was necessary to redetermine the distributions of retirements and consumption of fixed capital in every computational cycle and delete them again afterwards. Storage space ceased to be a problem, when modernised and larger hard disk systems were introduced at PC level. Considering that the spreadsheet programme Excel was generally available for difficult mathematical computations, a solution was chosen, which was based on "Visual Basic for Applications (VBA)".

Another problem that had to be considered was the extent to which it would be possible to map the model in the *file system* taking into account the model's complexity. As the computation of the gamma distribution and its final progression (linearization of the asymptotic function, see below) needs very much computing power, this process was separated from the rest of the file system. Besides, a strict separation was made in the file system between service life approaches and the calculation of flows and stocks, internally referred to (briefly) as B-matrices. This appeared advisable, first of all, in order to prevent large files from placing an extremely high burden on the network. This trichotomy – service life approaches, computation of the gamma distribution, and B-matrices – is schematically displayed in fig. 5 and will be explained in more detail below.

In compiling the *service life approaches and their goods proportions* a presentation was chosen, which it would be easy to understand. This did not raise any problems as regards machinery and equipment, as dilation parameter 9



was always used in subsequent calculations of the gamma distribution. Fig. 6 shows the structure of one such service life approach.



The table header includes the investment years and the proportions of the respective assets grouped by service life are listed thereunder for each investment year. As additional information the average service life for the year in question was indicated at the end of the column. These service life files still consist of several Excel worksheets, which include both the mortality distribution and the ensuing distribution regarding consumption of fixed capital. But the computing process as such has been relocated to another file. If a service life distribution changes, computing is done using VBA so that the new distribution is transferred to the computing file and, on completion of the computing process, the distributions of retirements and consumption of fixed capital are returned to the service life distribution. A separate mortality distribution is calculated for each individual service life

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Fig. 6

group. Subsequently, the various mortality distributions so defined are weighted with the proportions of the composite asset groups related to fixed capital formation of the year in question.

A factor that has to be considered as regards the computing process as such is the fact that the gamma distribution is an infinite function. That is the reason why we *discontinue the gamma distribution* in Germany as soon as 99% of assets have been withdrawn. In the years that follow the data is updated using the previous year's proportion as long as all assets are actually withdrawn from the stock. The related computing process is much more challenging in terms of mathematics and programming than the gamma distribution as such. VBA and if-queries were used to implement this step of computation.

Whilst the computing model of machinery and equipment was largely suitable for intangible assets as well, it was necessary to choose a different approach to buildings, because here it was not always possible to use just one standard dilation parameter in the gamma distribution. For example, the parameters chosen for residential buildings were different; the dilation parameter 7 was laid down for new buildings and 13 for modernisation activities. Fig. 7 shows the typical structure of a table displaying the service life approach to buildings.

Fig. 7

Example of a service life approach to buildings and structures														
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(B)	Datei	Bearbeiten	Ansicht	Einfügen	Format	Extras	Daten F	enster i	Veröffe	ntlichen			- 8	×
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	Rech-													
1	- nen	- 1004	4000	4000	400.4	1005	4000	4007	4000	4000	0000	0004	0000	
2		1991	1992	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002	
3		95	96	95	05	96	95	96	95	- /	95	95	/ 95	
5		0.35197	0.35337	0.37680	0.40870	0.35923	0.37692	0.37692	0.37692	0.37692	0.37692	0.37692	0.37692	
6		7	7	7	7	7	7	7	7	7	7	7	7	
7	1	85	85	85	85	85	85	85	85	85	85	85	85	
8		0,23971	0,26518	0,30727	0,34101	0,32786	0,27128	0,27128	0,27128	0,27128	0,27128	0,27128	0,27128	
9		13	13	13	13	13	13	13	13	13	13	13	13	
10		45	45	45	45	45	45	45	45	45	45	45	45	
11		0,40830	0,38144	0,31591	0,25027	0,31290	0,35178	0,35178	0,35178	0,35178	0,35178	0,36178	0,35178	
12														
14		-												
15														
16														
17	1							< 1 3						
18	1													
19														
20														
21	Σ DND	1,00	1,00	1,00	1,00	1,00	1,00	1,00	1,00	1,00	1,00	1,00	1,00	
22	UND	/2,2	/3,3	/6,1	/9,1	/6,1	/4,/	/4,/	/4,/	/4,/	/4,/	/4,/	/4,/	-
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Unlike the described model for machinery and equipment, this approach provides for all assets to be arranged in triads. The first cell of this group represents the dilation parameter, the second one the average service life and the third one the proportion of that asset for the year in question. Here again, a VBA procedure is started, which transfers service life data to the buildings worksheet used for computing purposes, and afterwards the ensuing distributions of retirements and consumption of fixed capital are transferred back to the service life file. German fixed assets calculations include 150 service life distributions for the various computing areas, but only two files for computing the gamma distribution and the cut-off process of this function. For each section, which is subject to computation, a separate file is used to determine flows and stocks. Fig. 8 shows the structure of the B-matrices files.

<u>a</u> M	icrosof	t Excel - BM	AT_513_	AUS_AGOV.xls			_10
3)	Datei	Bearbeiten	Ansicht	Einfügen Format	Extras Daten F	enster ? Veröffen	lichen – d
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2	Vermo	igensart	2011				Wirtschaftszweig
Jahr Zugänge		ge	Abschrei-	Abgänge	Nettobestand am	Bruttobestand am	
3				bungen		Jahresanfang	Jahresanfang
37	1982		453	476	331	3 834	7 078
38	1983		436	488	355	3 810	7 19
39	1984		456	497	383	3 758	7 27
90	1985		523	508	412	3 717	7 35.
91	1986		596	522	442	3 732	7 46.
32	1987		606	538	468	3 806	7 618
93	1988		642	556	490	3 874	7 75
94	1989		703	580	508	3 960	7 90
95	1990		765	610	525	4 083	8 103
96	1991		1 107	663	545	4 238	8 34
97	1992		1 186	733	573	4 682	8 90
98	1993		1 067	785	612	5 136	9 52
<del>9</del> 9	1994		800	808	659	5 417	9 97
00	1995	-	947	818	692	5 410	10 110
U1	1996	2	910	835	701	5 539	10 370
U2	1997		927	852	704	5 614	10 579
U3	1998		944	872	717	5 688	10.80
04	1999		1 066	899	744	5 760	11 02
05	2000		1 080	931	779	5 927	11 35
06	2001		1 124	963	815	6 0/6	11 65
U/	2002		1 169	996	852	6 238	11.96
UB 0C	2003	-	855	1 013	886	6 401	12 26
109	2004	2	937	1 016	920	6 243	12 23

All flows (consumption of fixed capital, retirements) and stocks (in net and gross terms at start of year) of fixed assets estimations are calculated in these B-matrices. Exceptional factors of influence (special retirements) are not considered by these files. Linking is used to apply the distribution of the mortality and depreciation functions to the service life distribution of the section, subject to computation. This model provides very many possibilities of ad hoc analysis. On the one hand, gross capital formation can be subject to changes and their influence on other flows becomes visible at once. On the other hand, one can directly see how the calculation will change by simply modifying the service life distribution, which results in corresponding changes regarding the distribution of the mortality and depreciation functions.

# 4 Data bases for calculations in the context of the 2005 revision and the 2006 backward calculation

### 4.1 Long-term series of gross fixed capital formation

*Gross fixed capital formation* means *additions* to fixed assets or the capital stock. If it is not possible or not desirable to use benchmark estimates for the capital stock in a start year, the series of gross fixed capital formation, on which the perpetual inventory method is based, must include a very long period of the past.<sup>15</sup>) Since, according

<sup>15)</sup> See also OECD Manual, footnote 2, p. 44.

to the gamma function, retirements may oscillate by more than double around the average service life, data on gross fixed capital formation should be available at least for a correspondingly long period of the past. The internal series of gross fixed capital formation in Germany start for buildings in 1799, for machinery and equipment in 1899 and for intangible assets in 1945 or even later.

Gross fixed capital formation is broken down by

- more than 200 types of machinery and equipment, 8 kinds of buildings and four types of other fixed assets,
- 60 industries and
- institutional sectors of national accounts (five sectors and seven sub-sectors)

(please, also refer to fig. 1). That means that gross fixed capital formation is available in three classification profiles. Regarding the consumption of fixed capital calculation, it is also necessary to distinguish between market producers and other non-market producers in gross fixed capital formation of the government sector (S.13) and non-profit institutions serving households (S.15) (see chart 2), because consumption of fixed capital of other non-market producers of the government sector and of non-profit institutions serving households has a direct influence on the size of gross domestic product and gross national income (see section 2.3). Although gross fixed capital formation is already available in a highly detailed manner, it may sometimes be necessary to specify it with even more detail for the purpose of fixed assets and consumption of fixed capital calculations (see fig. 6 and fig. 7).

Chart 2: Industries in which general government (S.13) and/or non-profit institutions serving households (S.15) are involved

		Sectors			
A601)	Industries	S.11/S.12/ S.14 <sup>2</sup> )	S.13	S.15	
01	Agriculture, hunting	MP	MP		
02	Forestry	MP	MP		
41	Collection, purification and distribution of water	MP	MP		
63	transport activities	MP	MP/NMP		
70	Real estate activities	MP	MP	MP	
73	Research and development	MP	NMP	NMP	
75	Public administration, defence;				
	compulsory social security .		NMP		
80	Education	MP	NMP	NMP	
85	Health, veterinary and social				
	work	MP	NMP	NMP	
90	Sewage and refuse disposal	MP	MP		
91	Activities of membership				
	organisations n.e.c	MP		NMP	
92	Recreational, cultural and				
	sporting activities	MP	NMP	NMP	

MP: Market output; NMP: Other non-market output

1) The A60 of national accounts corresponds to the two-digit items of the industrial classification, issue 2003 (WZ 2003). – 2) Non-financial and financial corporations and households.

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#### 4.2 Service life approaches

A category which is to be determined for all series of data on gross fixed capital formation is average (economic) service life - the second major input needed for the perpetual inventory method. Service life is the period, during which an asset's consumption is recorded. This value is insecure, because it is geared to the future. In order to determine it in line with the ESA-1995, it is necessary to take into account normal wear and tear as well as economic obsolescence and losses of fixed assets as a result of accidental damage which can be insured against. It is assumed that the assets are correctly maintained and minor repairs are continuously made. Service life approaches are determined by breaking down gross fixed capital formation by type of asset in as much detail as possible. The 2005 revision brought about minor modifications in the assumptions on the assets' average service lives, as they were adapted to the new asset structures.

The most important basis for the determination of an asset's average service life regarding machinery and equipment and some buildings is provided by the AfA tables, which are issued by the Federal Ministry of Finance. These tables contain deeply specified assets together with the service life data to be used in order to determine consumption of fixed capital for tax purposes. As the determination of an asset's fiscal life is based on the assumption that individual businesses act according to the principle of precaution, an asset's real life is, as a rule, longer than its fiscal life. That is why the figures of the AfA tables are augmented by an average 20 to 100%, when determining the average (economic) service life for the purpose of national accounts. The information used for that purpose was provided by enterprises and associations (expert assessments). Service life data of equal asset groups is sometimes differentiated by industry. For example, lorries operated in construction are supposed to have shorter service lives than those operated in other industries. An internal cross-classification of investors (assets/industry) is used to determine service life by industry.

The service lives of *buildings and structures*, in particular residential buildings, commercial buildings and public buildings, were extracted from the long-term accounts without major modifications. Many resources were opened by the latest revision when these assets had to be written off and/or recorded as fixed assets for the first time in order to determine the service life of *roads and other structures of general government and fixed assets used by the military.* These resources included, for instance, investigations made by the German Institute for Economic Research (DIW Berlin) and the ifo Institute for Economic Research e.V. as well as texts on how to determine the value of real estate and the cost directive elaborated by the Federal Ministry of Defence.<sup>16</sup>)

The latest revision also tapped various resources to determine the service life of *intangible assets*. Mineral explo-

<sup>16)</sup> See Schmalwasser, O., footnote 6, here: p. 349.

ration data could be obtained from AfA tables. The service life of software is differentiated by two groups. Software for mainframes is supposed to have a longer service life than PC software. In the course of the 1980s the proportion of PC software grew continuously. The proportions of the two types of software were also differentiated by industry. The average life of literary and artistic originals was estimated on the basis of differentiated information on motion pictures, TV productions, sound storage media, music compositions, artistic performances and texts.<sup>17</sup>)

Average lives of assets are obtained by type of asset, industry and sector for *every investment year*. The service life estimates by type of asset are revised every ten to 15 years, i.e. in relatively large intervals. This was based on several considerations. In the last decades of the past century Afa service lives were repeatedly shortened and partly pro-

Chart 3: Average service lives and range of average service lives
within the group by type of assets for the 2000 investment year
in years

Type of asset	Average service life	Range of average service lives by group		
Buildings and structures	66	15 - 150		
Dwellings	74	40 - 95		
Roads	57	35 - 116		
Other structures of general				
government	47	25 - 150		
Non-residential buildings of general				
government	66	25 - 68		
Other non-residential buildings	53	15 - 100		
Machinery and equipment (according				
to CPA) <sup>1</sup> )	12	5 - 30		
Transport equipment	11	8 - 25		
Motor vehicles, trailers and semi-		0 15		
Cthestropost equipment (25)	9	8 - 15		
Other transport equipment (35)	21	12 - 25		
Other machinery and equipment	12	5 - 30		
Fabricated metal products (28)	18	14 - 22		
Machinery and equipment n.e.c.	12	0 20		
(29)	13	8 - 30		
(30)	5	5_0		
Flectrical machinery and apparatus		J - 9		
n.e.c. (31)	18	8 - 22		
Radio, television and	_			
communication equipment and				
apparatus (32)	10	5 - 17		
Medical, precision and optical				
instruments, watches and clocks				
(33)	15	10 - 22		
Furniture, other manufactured	16	0 20		
Other machinery and equipment	10	8 - 50		
(part of 17 – 27)	13	7 - 20		
		, 20		
Vinevarde	20			
Hon fields	15			
Asparagus fields	8			
Fruit trees plantations	10			
		F 20		
	2	5 - 30		

1) Statistical goods classification in conjunction with the industries (kinds of activity) used in the European Economic Community, 2002.

longed in 2001. But not every change in the fiscal service life necessarily has an impact on the economic service life (according to an estimation of national accounts). Fiscal service lives are just one source among many others, which serve as an indication of possible changes occurring in economic service lives. According to the estimation of national accounts, the economic service life is also changed, for instance, on the basis of expert assessments and plausibility checks. But structural effects may occur even if the service life approaches in the most detailed breakdown by asset do not change at all. That means that every investment year has a service life distribution of its own. Chart 3 shows the average service lives by type of asset and the respective span of time on which a (sub) group's average service life is based.

A distinction must be made between the average service lives for the various investment years, on which the calculations are based, and the *average service life of assets in the stock*. The latter one corresponds to the reciprocal value of the depreciation rate (rate of consumption of fixed capital) for the total economy. It is obtained as a result of the division of gross annual average stock of fixed assets by consumption of fixed capital, if possible, in a breakdown by type of asset. The average for the total economy depends on the composition of fixed assets by goods that have very different service lives (in particular buildings and structures, machinery and equipment, and intangible assets).

#### 4.3 Consideration of special influences

According to the ESA-1995, changes in the volume of assets and liabilities caused by extraordinary events deviating from the perpetual inventory method's original assumptions are recorded as other changes in the volume of assets. This item includes those special retirements of fixed assets that were covered by German fixed assets calculations already in the past. It relates, in particular, to the reduction of refinery capacities, iron and steel capacities and ship-building (shipyard crisis) and to corrections of the gross stock, when used ships are sold abroad.18) Furthermore, from 1993 on this item has been used to record special retirements of old assets from the ex-GDR which are no longer usable from an economic point of view, provided that these assets were not already excluded when determining the initial stocks as of 1 July 1990. Correction is also required in the case of repeated sales of real estate within short intervals of time: It is assumed that real estate is sold at market prices and that it is not possible, as a rule, to realise the full costs associated with the transfers of ownership (tax on purchase of real estate, fees of brokers, notaries and courts). The respective amount should be considered for buildings under special retirements caused by costs associated with the transfers of ownership. And, finally, the high losses of fixed assets, which were caused by the flood in August 2002, were also recorded in this category as catastrophic losses. The sources used for that purpose consisted of lists of damages compiled by the Federal Government and by Sachsen (Sax-

<sup>17)</sup> See also Frankford, L.: "Urheberrechte in den Volkswirtschaftlichen Gesamtrechnungen" in WiSta 5/2000, p. 320 ff.

<sup>18)</sup> See Schmidt, L.: "Reproduzierbares Anlagevermögen in erweiterter Bereichsgliederung" in WiSta 5/1986, p. 499 ff., here: p. 503 f.



ony) and *Sachsen-Anhalt*, the federal states most severly affected, as well as information provided by the *Deutsche Bahn AG* (German Railways).

The perpetual inventory method predetermines all effects that gross fixed capital formation of a given year exerts on all elements of fixed assets calculations, until the last asset resulting from that investment year will be withdrawn from the stock. That means that whenever special retirements of fixed assets are recorded it is necessary to make the corresponding *counterentries* for consumption of fixed capital and retirements in the following years. Otherwise, for example, consumption of fixed capital would be recorded for assets, which are no longer in the stock.

#### 5 Results obtained in the context of the 2005 revision and the 2006 backward calculation

The results of the calculations related to fixed assets in Germany are commented on the basis of two figures (see fig. 9 and 10). Fixed assets are shown in line with two price concepts in gross and net terms by 60 kinds of industry broken down into buildings and other assets and, for the total economy, also into six types of fixed assets.<sup>19</sup>) This information is supplemented by corresponding data on consumption of fixed capital in prices of the year 2000 and in current prices.<sup>20</sup>)

19) See Thematic Series 18, Row 1.4 "Inlandsproduktsberechnung – Detaillierte Jahresergebnisse 2005", tables 3.1.3 and 3.2.16 to 3.2.19. 20) Ibid., tables 3.1.4, 3.2.20 and 3.2.21.

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