# On the Long-Run Evolution of Inheritance: France 1820-2050 

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#### Abstract

This paper attempts to document and account for the long run evolution of inheritance. We find that in a country like France the annual flow of inheritance was about $20 \%-25 \%$ of national income between 1820 and 1910, down to less than $5 \%$ in 1950 , and back up to about $15 \%$ by 2010. A simple theoretical model of wealth accumulation, growth and inheritance can fully account for the observed U-shaped pattern and levels. Using this model, we find that under plausible assumptions the annual bequest flow might reach about 20\%-25\% of national income by 2050. This corresponds to a capitalized bequest share in total wealth accumulation well above $100 \%$. Our findings illustrate the fact that when the growth rate g is small, and when the rate of return to private wealth $r$ is permanently and substantially larger than the growth rate (say, $r=4 \%-5 \%$ vs. $g=1 \%-2 \%$ ), which was the case in the $19^{\text {th }}$ century and early $20^{\text {th }}$ century and is likely to happen again in the $21^{\text {st }}$ century, then past wealth and inheritance are bound to play a key role for aggregate wealth accumulation and the structure of lifetime inequality. Contrarily to a widely spread view, modern economic growth did not kill inheritance.


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## 1. Introduction

There are basically two ways to become rich: either through one's own work, or through inheritance. In Ancien Regime societies, as well as during the $19^{\text {th }}$ century and early $20^{\text {th }}$ century, it was self-evident to everybody that the inheritance channel was an important one. For instance, 19 th century and early $20^{\text {th }}$ century novels are full of stories where ambitious young men have to choose between becoming rich through their own work or by marrying a bride with large inherited wealth - and often opt for the second strategy. However, in the late $20^{\text {th }}$ century and early $21^{\text {st }}$ century, most observers seem to believe that this belongs to the past. That is, most observers - novelists, economists and laymen alike - tend to assume that labor income is now playing a much bigger role than inherited wealth in shaping people's lives, and that human capital and hard work have become the key to personal material well-being. Although this is rarely formulated explicitly, the implicit assumption seems to be that the structure of modern economic growth has led to the rise of human capital, the decline of inheritance, and the triumph of meritocracy.

This paper asks a simple question: is this optimistic view of economic development justified empirically and well-grounded theoretically? Our simple answer is "no". Our empirical and theoretical findings suggest that inherited wealth will most likely play as big a role in $21^{\text {st }}$ century capitalism as it did in $19^{\text {th }}$ century capitalism - at least from an aggregate viewpoint.

This paper makes two contributions. First, by combining various data sources in a systematic manner, we document and establish a simple - but striking - fact: the aggregate inheritance flow has been following a very pronounced U-shaped pattern in France since the $19^{\text {th }}$ century. To our knowledge, this is the first time that such long-run, homogenous inheritance series are constructed for any country.

More precisely, we define the annual inheritance flow as the total market value of all assets (tangible and financial assets, net of financial liabilities) transmitted at death or through inter-vivos gifts during a given year. ${ }^{1}$ We find that the annual inheritance flow was about $20 \%-25 \%$ of national income around 1900-1910. It then gradually fell to less than $10 \%$ in the 1920s-1930s, and to less than $5 \%$ in the 1950s. It has been rising regularly since then, with an acceleration of the trend during the past 30 years, and according to our latest data point (2008), it is now close to $15 \%$ (see Figure 1).

[^1]If we take a longer run perspective, then the $20^{\text {th }}$ century U-shaped pattern looks even more spectacular. The inheritance flow was relatively stable around $20 \%-25 \%$ of national income throughout the 1820-1910 period (with a slight upward trend), before being divided by a factor of about $5-6$ between 1910 and the 1950s, and then multiplied by a factor of about 3-4 between the 1950s and the 2000s.

These are truly enormous historical variations - but they appear to be well founded empirically. In particular, we find similar patterns with our two fully independent estimates of the inheritance flow. The gap between our "economic flow" series (computed from national wealth estimates, mortality tables and observed age-wealth profiles) and our "fiscal flow" series (computed from observed bequest and gift tax data) can be interpreted as a measure of tax evasion and other measurement errors. This gap appears to approximately constant over time, and relatively small, so that our two series deliver fairly consistent long run patterns (see Figure 1).

If we use personal disposable income (national income minus taxes plus cash transfers) rather than national income as the denominator, then we find that the inheritance flow observed in the early $21^{\text {st }}$ century is back to about $20 \%$, i.e. approximately the same level as that observed one century ago. This simply comes from the fact that disposable income was as high as $90 \%-95 \%$ of national income during the $19^{\text {th }}$ century and early $20^{\text {th }}$ century (when taxes and transfers were almost non existent), while it is now about 70\% of national income. Though we prefer to use the national income denominator (both for conceptual and empirical reasons), this is an important fact to keep in mind when studying these issues. An annual inheritance flow around $20 \%$ of disposable income is a very large flow. It is typically larger than the annual flow of new savings, and almost as big as the annual flow of capital income. As we shall see, it corresponds to a cumulated, capitalized bequest share in aggregate wealth accumulation well above $100 \%$.

The second - and most important - contribution of this paper is to account for these facts, and to draw lessons for other countries and for the future. We show that a simple theoretical model of wealth accumulation, growth and inheritance can easily explain why the French inheritance flow seems to return to a high steady-state value around $20 \%$ of national income. Consider first a dynastic model where all savings come from capital income. Wealth holders save a fraction $\mathrm{g} / \mathrm{r}$ of their asset returns, so that aggregate private wealth $W_{t}$ and national income $Y_{t}$ grow at the same rate $g$, and the wealth-income ratio $\beta=W_{t} / Y_{t}$ is stationary. It is straightforward to prove that the steady-state inheritance flownational income ratio is equal to $b_{y}=\beta / H$, where $H$ is generation length (average age at parenthood). If $\beta=600 \%$ and $H=30$, then $b_{y}=20 \%$. We show that this intuition can be generalized to more general saving models. Namely, as long as the (real) growth rate g is
sufficiently small and the (real) rate of return on private wealth $r$ is sufficiently large - say, $g=1 \%-2 \%$ vs. $r=4 \%-5 \%-$, then steady-state $b_{y}$ is close to the class saving level $\beta / H$.

The key intuition boils down to a simple r>g logic. In countries with large growth, such as France during the 1950s-1970s, then wealth coming from the past (i.e. accumulated or received by one's parents or grand-parents, who were relatively poor as compared to today's incomes) does not matter too much. What counts is new wealth accumulated out of current income. Inheritance flows are bound to be a small fraction of national income. But in countries with low growth, such as France in the $19^{\text {th }}$ century and since the 1970s, the logic is reversed. With low growth, successors simply need to save a small fraction of their asset returns in order to ensure that their inherited wealth grows at least as fast as national income. In effect, $g$ small and $r>g$ imply that wealth coming from the past is being capitalized at a faster rate than national income. So past wealth tends to dominate new wealth, rentiers tend to dominate labor income earners, and inheritance flows are large relative to national income. As $g \rightarrow 0$, then $b_{y} \rightarrow \beta / H$ - irrespective of saving behavior.

The $r>g$ logic is simple, but powerful. We simulate a full-fledged, out-of-steady-state version of this model, using observed macroeconomic and demographic shocks. We are able to reproduce remarkably well the observed evolution of inheritance flows in France over almost two centuries. The 1820-1913 period looks like a prototype low-growth, rentier-friendly quasi-steady-state. The growth rate was very small: $\mathrm{g}=1.0 \%$. The wealthincome ratio $\beta$ was $600 \%-700 \%$, the capital share $\alpha$ was $30 \%-40 \%$, so the average rate of return on private wealth was as large as $r=\alpha / \beta=5 \%-6 \%$. Taxes at that time were very low, so after-tax returns were almost as high as pre-tax returns. It was sufficient for successors to save about 20\% of their asset returns to ensure that their wealth grows as fast as national income (or actually slightly faster). The inheritance flow was close to its steadystate value $b_{y}=\beta / H=20 \%-25 \%$. The 1914-1945 capital shocks (involving war destructions, and most importantly a prolonged fall in asset prices) clearly dismantled this steady-state. It took a long time for inheritance flows to recover, especially given the exceptionally high growth rates observed during the 1950s-1970s ( $\mathrm{g}=5.2 \%$ between 1949 and 1979). The recovery accelerated since the late 1970s, both because of low growth ( $\mathrm{g}=1.7 \%$ between 1979 and 2009), and because of the long term recovery of asset prices and of the wealthincome ratio ( $\beta=500 \%-600 \%$ in 2008-9). As predicted by the theoretical model, the inheritance flow is now close to its steady-state value $b_{y}=\beta / H=15 \%-20 \%$.

We then use this model to predict the future. According to our benchmark scenario, based upon current growth rates and rates of returns, the inheritance flow will stabilize around $16 \%$ of national income by 2040 , i.e. at a lower level than the $19^{\text {th }}$ century steady-state. This is due both to higher projected growth rates (1.7\% rather than 1.0\%) and to lower projected after-tax rates of return (3.0\% rather than 5.3\%). In case growth slows down to
1.0\% after 2010, and after-tax returns rise to $5.0 \%$ (which corresponds to the suppression of all capital taxes, and/or to a combination of capital tax cuts and a rising global capital share), then the model predicts that the inheritance flow will keep rising and converge towards $22 \%-23 \%$ after 2050. In all plausible scenarios, the inheritance-income ratio in the coming decades will be at least $15 \%-20 \%$, i.e. closer to the $19^{\text {th }}$ century levels than to the exceptionally low levels prevailing during the 1950s-1970s. A come-back to postwar levels would require pretty extreme assumptions, such as the combination of high growth rates (above $5 \%$ ) and a prolonged fall in asset prices and aggregate wealth-income ratios.

Now, the fact that aggregate inheritance flows return to $19^{\text {th }}$ century levels obviously does not imply that the concentration of inheritance and wealth will return to $19^{\text {th }}$ century levels. On distributional issues, this macro paper has very little to say. We view the present research mostly as a positive exercise in aggregate accounting of wealth, income and inheritance, and as a building block for future work on inequality. One should however bear in mind that the historical decline of wealth concentration in developed societies has been quantitatively less important than some observers tend to imagine. E.g. according to the latest SCF (Survey of consumer finances), the top $10 \%$ owns $72 \%$ of U.S. aggregate wealth in 2007, while the middle $40 \%$ owns $26 \%$ and the bottom $50 \%$ owns $2 \% .^{2}$ In a country like France, the top $10 \%$ currently owns about $60 \%$ of aggregate wealth, and the bottom $50 \%$ owns around $5 \%$. These $60 \%-70 \%$ top decile wealth shares are certainly lower than the $90 \%$ top decile wealth shares observed in developed countries around 1900-1910, when there was basically no middle class at all. ${ }^{3}$ But they are not that much lower. It has also been known for a long time that these high levels of wealth concentration have little to do with the life cycle: top wealth shares are almost as large within each age group. ${ }^{4}$ The bottom line is that the historical decline in intra-cohort inequality of inherited wealth has been less important quantitatively than the long term changes in the aggregate inheritance-income ratio. So aggregate evolutions matter a lot for the study of inequality.

In order to illustrate this point, we provide applications of our aggregate findings to the measurement of two-dimensional inequality in lifetime resources (labor income vs inheritance) by cohort. By making approximate assumptions on intra cohort distributions, we compute simple two-dimensional inequality indicators, and we find that they have changed a lot over the past two centuries. In the $19^{\text {th }}$ century, top successors vastly dominated top labor earners (not to mention bottom labor earners) in terms of total lifetime resources. Cohorts born in the 1900s-1950s faced very different life opportunities. For the first time maybe in history, high labor income was the key for high material well-being.

[^2]According to our computations, cohorts born in the 1970s and after will fall somewhere in between the "rentier society" of the $19^{\text {th }}$ century and the "meritocratic society" of the $20^{\text {th }}$ century - and in many ways will be closer to the former than to the latter.

Do our findings also apply to other countries? We certainly do not pretend that the fairly specific U-shaped pattern of aggregate inheritance flows found for France applies everywhere as a universal law. It probably also applies to Continental European countries that were hit by similar growth and capital shocks. For countries like the U.S. and the U.K., which were little hit by war destructions, but suffered from the same mid-century fall in asset prices, the long-run U-shaped pattern of aggregate inheritance flows was possibly somewhat less pronounced. ${ }^{5}$ In fact, we do not really know. We tried to construct similar series for other countries. But unfortunately there does not seem to exist any other country with estate tax data that is as long run and as comprehensive as the French data.

In any case, even though we cannot make detailed cross country comparisons at this stage, the economic mechanisms revealed by the analysis of the French historical experience certainly apply to other countries as well. In particular, the r>g logic applies everywhere, and has important implications. For instance, it implies that in countries with very large economic and/or demographic growth rates, such as China or India, inheritance flows must be a relatively small fraction of national income. Conversely, in countries with low economic growth and projected negative population growth, such as Spain, Italy or Germany, then inheritance is bound to matter a lot during the $21^{\text {st }}$ century. Aggregate inheritance flows will probably reach higher levels than in France. More generally, a major difference between the U.S. and Europe (taken as a whole) from the viewpoint of inheritance might well be that demographic (and to a lesser extent economic) growth rates have been historically larger in the U.S., thereby making inheritance flows relatively less important. This has little to do with cultural differences. This is just the mechanical impact of growth rates and of the $\mathrm{r}>\mathrm{g}$ logic. And this may not last forever. If we take a very long run, global perspective, and make the assumption that economic and demographic growth rates will eventually be relatively small everywhere (say, $g=1 \%-2 \%$ ), then the conclusion follows mechanically: inheritance will matter a lot pretty much everywhere.

The rest of this paper is organized as follows. In section 2, we relate this work to the existing literature. In section 3, we describe our methodology and data sources. In section 4, we present a decomposition of the U-shaped pattern into three components: an aggregate wealth-income effect, a mortality effect, and a relative wealth effect. In section 5 , we provide theoretical results on steady-state inheritance flows. In section 6, we report simulation results based upon a full fledged version of this model. In section 7, we present

[^3]applications of our results to the structure of lifetime inequality and to the share of inheritance in aggregate wealth. Section 8 offers concluding comments.

## 2. Related literature

### 2.1. Literature on top incomes

This paper is related to several literatures. First, this work represents in our view the logical continuation of the recent literature on the long run evolution of top income and top wealth shares initiated by Piketty (2001, 2003), Atkinson (2005) and Piketty and Saez (2003). In this collective research project, we constructed homogenous, long run series on the share of top decile and top percentile income groups in national income, using income tax return data. The resulting data base now includes annual series for over 20 countries, including most developed economies over most of the $20^{\text {th }}$ century. ${ }^{6}$ One the main findings is that the historical decline in top income shares that occurred in most countries during the first half of the $20^{\text {th }}$ century was largely due to the fall of top capital incomes, which apparently never fully recovered from the 1914-1945 shocks, possibly because of the rise of progressive income and estate taxes (the "fall of rentiers"). Another important finding is that the large rise in top income shares that occurred in the U.S. (and, to a lesser extent, in other anglo-saxon countries) since the 1970s seem to be mostly due to the unprecedented rise of very top labor incomes (the "rise of working rich").

One important limitation of this literature, however, is that although we did emphasize the distinction between top labor vs. top capital incomes, we did not go all the way towards a satisfactory decomposition of inequality between a labor income component and an inherited wealth component. First, due to various legal exemptions, a growing fraction of capital income has gradually escaped from the income tax base (which in several countries has almost become a labor income tax in recent decades), and we did not seriously attempt to impute full economic capital income (as measured by national accounts) back into our income-tax-returns-based series. ${ }^{7}$ This might seriously affect some of our conclusions (e.g. about working rich vs rentiers), ${ }^{8}$ and is likely to become

[^4]increasingly problematic in the coming decades. So it is important to develop ways to correct for this. Next, even if we were able to observe (or impute) full economic capital income, this would not tell us anything about the share of capital income coming from one's own savings and the share originating from inherited wealth. In income tax returns, one does not observe where wealth comes from. For a small numbers of countries, long run series on top wealth shares (generally based upon estate tax returns) have recently been constructed. ${ }^{9}$ These studies confirm that there was a significant decline in wealth concentration during the 1914-1945 period, apparently with no recovery so far. ${ }^{10}$ But they do not attempt to break down wealth into an inherited component and a life-cycle or selfmade component: these works use estate tax data to obtain information about the distribution of wealth among the living (using mortality multiplier techniques), but not to study the level of inheritance flows per se. ${ }^{11}$

This paper attempts to bridge this gap, by making use of the exceptionally high quality of French estate tax data. We felt that it was necessary to start by trying to reach a better empirical and theoretical understanding of the aggregate evolution of the inheritanceincome ratio, which to us was very obscure when we started this research. However the next step is obviously to close this detour via macroeconomics and to integrate endogenous distributions back into the general picture.

### 2.2. Literature on intergenerational transfers and aggregate wealth accumulation

The present paper is also very much related to the literature on intergenerational transfers and aggregate wealth accumulation. However as far we know our paper is the first attempt to account for the observed historical evolution of inheritance, and to take a long run perspective on these issues. Although the perception of a long term decline of inheritance relatively to labor income seems to be relatively widespread, to our knowledge there are very few papers which formulate this perception explicitly. ${ }^{12}$ For instance, in their famous

[^5]controversy about the share of inheritance in U.S. aggregate wealth accumulation, both Kotlikoff and Summers (1981) and Modigliani (1986) were using a single - and relatively ancient and fragile - data point for the U.S. aggregate inheritance flow (namely, for year 1962). In addition to their definitional conflict, we believe that the lack of proper data contributes to explain the intensity of the dispute, which the subsequent literature did not fully resolve. ${ }^{13}$ We return to this controversy when we use our aggregate inheritance flows series to compute inheritance shares in the total stock of wealth. The bottom line is that with steady-state inheritance flows around $20 \%$ of national income, the cumulated, capitalized bequest share in aggregate wealth accumulation is bound to be well above $100 \%$ - which in a way corroborates the Kotlikoff-Summers viewpoint. We hope that our findings contribute to clarify this long standing dispute.

### 2.3. Literature on calibrated models of wealth distributions

Our work is also related to the recent literature attempting to use calibrated general equilibrium models in order to replicate observed wealth inequality. Several authors have recently introduced new ingredients into calibrated models, such as large uninsured idiosyncratic shocks to labor earnings, tastes for savings and bequests, and/or asset returns. ${ }^{14}$ In addition to the variance and functional form of these shocks, one key driving force in these models is naturally the macroeconomic importance of inheritance flows: other things equal, larger inheritance flows tend to lead to more persistent inequalities and higher steady-state levels of wealth concentration. However this key parameter tends to be imprecisely calibrated in this literature, and is generally underestimated: it is often based upon relatively ancient data (typically dating back to the KSM controversy and using data from the 1960s-1970s) and frequently ignores inter vivos gifts. We hope that our findings can contribute to offer a stronger empirical basis for these calibrations.

### 2.4. Literature on estate multipliers

Finally, our paper is closely related to the late $19^{\text {th }}$ century and early $20^{\text {th }}$ century literature on national wealth and the so-called "estate multiplier". At that time, many economists were computing estimates of national wealth, especially in France and in the UK. In their view, it was obvious that most wealth derives from inheritance. They were satisfied to find that their national wealth estimates $W_{t}$ (obtained from direct wealth census methods) were always approximately equal to 30-35 times the inheritance flow $B_{t}$ (obtained from tax data). They interpreted 30-35 as generation length H , and they viewed the estate multiplier

[^6]formula $e_{t}=W_{t} / B_{t}=H$ as self-evident. ${ }^{15}$ In fact, it is not self-evident. This formula is not an accounting equation, and strictly speaking it is valid only under fairly specific models of saving behaviour and wealth accumulation, such as the class saving model. It is difficult to know exactly what model the economists of the time had in mind. From their informal discussions, one can infer that it was close to a stationary model with zero growth and zero saving (in which case $e_{t}=H$ is indeed self-evident), or maybe a model with small growth originating from slow capital accumulation and a gradual rise of the wealth-income ratio. Of course we now know that capital accumulation alone cannot generate positive self-sustained growth: one needs positive rates of productivity growth $g>0$. Economists writing in the $19^{\text {th }}$ and early $20^{\text {th }}$ centuries were not fully aware of this, and they faced major difficulties with the modelling of steady-state, positive self-sustained growth. This is probably the reason why they were unable to formulate an explicit dynamic, non-stationary model explaining where the estate multiplier formula comes from.

The estate multiplier literature disappeared during the interwar period, when economists realized that the formula was not working any more, or more precisely when they realized that it was necessary to raise the multiplier $e_{t}$ to as much as 50 or 60 in order to make it work (in spite of the observed constancy of H around 30 ). ${ }^{16}$ Shortly before World War 1, a number of British and French economists also started realizing on purely logical grounds that the formula was too simplistic. They started looking carefully at age-wealth profiles, and developed the so-called "mortality multiplier" literature, whereby wealth-at-death data is being re-weighted by the inverse morality rate of the given age group in order to generate estimates for the distribution of wealth among the living (irrespective of whether this wealth comes from inheritance or not). ${ }^{17}$ Unlike the estate multiplier formula, the mortality multiplier formula is indeed a pure accounting equation, and makes no assumption on saving behaviour. The price to pay for this is that the mortality multiplier approach does not say anything about where wealth comes from: this is simply a statistical technique to recover the cross-sectional distribution of wealth among the living. ${ }^{18}$

In the 1950s-1960s, economists then started developing the life cycle approach to wealth accumulation. ${ }^{19}$ This was in many ways the complete opposite extreme to the estate multiplier approach. In the life cycle model, inheritance plays no role at all, individuals die

[^7]with zero wealth (or little wealth), and the estate multiplier $e_{t}=W_{t} / B_{t}$ is infinite (or very large, say 100 or more). It is interesting to note that this theory was formulated precisely at the time when inheritance was at its historical nadir. According to our series, the inheritance flows were about $4 \%$ of national income in the 1950s-1960s, vs. as much as $20 \%-25 \%$ at the time of estate multiplier economists (see Figure 1). Presumably, economists were in both cases very much influenced by the wealth accumulation and inheritance patterns prevailing at the time they wrote.

Our advantage over both estate-multiplier and life-cycle economists is that we have more years of data. Our two-century-long perspective allows us to clarify these issues and to reconcile the various approaches in a unified framework (or so we hope). The lifecycle motive for saving is logically plausible. But it clearly cohabits with many other motives for wealth accumulation (bequest, security, prestige and social status, etc.). Most importantly, we show that with low growth rates and high rates of return, past wealth naturally tends to dominate new wealth, and inheritance flows naturally tend to converge towards levels that are not too far from those posited by the estate multiplier formula, whatever the exact combination of these saving motives might be.

## 3. Data sources and methodology

The two main data sources used in this paper are national income and wealth accounts on the one hand, and estate tax data on the other hand. Before we present these two data sources in a more detailed way, it is useful to describe the basic accounting equation that we will be using throughout the paper in order to relate national accounts and inheritance flows. In particular, this is the accounting equation that we used to compute our "economic inheritance flow" series.

### 3.1. Basic accounting equation: $B_{t} / Y_{t}=\mu_{t} \underline{m}_{t} W_{t} / Y_{t}$

If there was no inter vivos gift, i.e. if all wealth transmission occurred at death, then in principle one would not need in any estate tax data in order to compute the inheritance flow. One would simply need to apply the following equation:

$$
\begin{array}{rlrll} 
& B_{t} / Y_{t} & =\mu_{t} m_{t} & W_{t} / Y_{t} \\
\text { l.e. } & b_{y t} & =\mu_{t} & m_{t} & \beta_{t} \tag{3.1}
\end{array}
$$

With: $B_{t}=$ annual inheritance flow
$Y_{t}=$ national income
$\mathrm{W}_{\mathrm{t}}=$ aggregate private wealth
$\mathrm{m}_{\mathrm{t}}=$ annual mortality rate $=$ (total number of decedents)/(total living population)
$\mu_{\mathrm{t}}=$ ratio between average wealth of the deceased and average wealth of the living $b_{y t}=B_{t} / Y_{t}=$ aggregate inheritance flow-national income ratio
$\beta_{t}=W_{t} / Y_{t}=$ aggregate private wealth-national income ratio

Alternatively, equation (3.1) can be written in per capita terms:

$$
\begin{equation*}
b_{t} / y_{t}=\mu_{t} w_{t} / y_{t}=\mu_{t} \beta_{t} \tag{3.2}
\end{equation*}
$$

With: $b_{t}=$ average inheritance per decedent
$y_{t}=$ average national income per living individual
$\mathrm{w}_{\mathrm{t}}=$ average private wealth per living individual

Equation (3.1) is a pure accounting equation: it does not make any assumption about behaviour or about anything. For instance, if the aggregate wealth-income ratio $\beta_{t}$ is equal to $600 \%$, if the annual mortality rate $m_{t}$ is equal to $2 \%$, and if people who die have the same average wealth as the living ( $\mu_{\mathrm{t}}=100 \%$ ), then the annual inheritance flow byt has to be equal to $12 \%$ of national income. In case old-age individuals massively dissave in order to finance retirement consumption, or annuitize their assets so as to die with zero wealth, as predicted by the pure life-cycle model, then $\mu_{\mathrm{t}}=0 \%$ and $\mathrm{b}_{\mathrm{yt}}=0 \%$. I.e. there is no inheritance at all, no matter how large $\beta_{t}$ and $m_{t}$ might be. Conversely, in case people who die are on average twice as rich as the living ( $\mu_{\mathrm{t}}=200 \%$ ), then for $\beta_{\mathrm{t}}=600 \%$ and $m_{t}=2 \%$, the annual inheritance flow has to be equal to $24 \%$ of national income.

If we express the inheritance flow $B_{t}$ as a fraction of aggregate private wealth $W_{t}$, rather than as a fraction of national income $\mathrm{Y}_{\mathrm{t}}$, then the formula is even simpler:

$$
\begin{equation*}
b_{w t}=B_{t} / W_{t}=\mu_{t} m_{t} \tag{3.3}
\end{equation*}
$$

I.e. the inheritance-wealth ratio $b_{w t}$ is equal to the mortality rate multiplied by the $\mu_{t}$ ratio. In case $\mu_{\mathrm{t}}=100 \%$, e.g. if the age-wealth profile is flat, then $b_{\mathrm{wt}}$ is equal to the mortality rate. The estate multiplier $e_{t}=W_{t} / B_{t}$ is simply the inverse of $b_{w t}$. We will return to the evolution of the inheritance-wealth ratio $b_{w t}$ later in this paper. But for the most part we choose to focus the attention upon the inheritance-income ratio $b_{y t}$ and accounting equation (3.1), first because the evolution of the wealth-income ratio $\beta_{t}=W_{t} / Y_{t}$ involves economic processes that are interesting per se (and interact with the inheritance process); and next because national wealth data is missing in a number of countries, so that for future comparison purposes we find it useful to emphasize $b_{y t}$ ratios, which are easier to compute (if one has fiscal data). Also, $b_{y t}$ has arguably greater intuitive economic appeal than $b_{w t}$. E.g. it can easily be compared to other flow ratios such as the capital share $\alpha_{t}$ or the saving rate $s_{t}$.

An example with real numbers might be useful here. In 2008, per adult national income was about $35,000 €$ in France. Per adult private wealth was about $200,000 €$. That is, $\beta_{\mathrm{t}}=\mathrm{W}_{\mathrm{t}} / Y_{\mathrm{t}}=\mathrm{w}_{\mathrm{t}} / \mathrm{y}_{\mathrm{t}}=560 \%$. The mortality rate $\mathrm{m}_{\mathrm{t}}$ was equal to $1.2 \%$, and we estimate that $\mu_{\mathrm{t}}$ was approximately $220 \% .^{20}$ It follows from equations (3.1) and (3.3) that the inheritanceincome ratio $b_{y t}$ was $14.7 \%$ and that the inheritance-wealth ratio $b_{y t}$ was $2.6 \%$. It also follows from equation (3.2) that average inheritance per decedent $b_{t}$ was about $440,000 €$, i.e. about 12.5 years of average income $y_{t}\left(\mu_{t} \times \beta_{t}=12.5\right)$. One can then introduce distributional issues: about half of decedents have virtually no wealth, the other half owns about twice the average (i.e. about 25 years of average income); and so on. ${ }^{21}$

For the time being, however, we concentrate on $b_{y t}$ and equation (3.1), which is more suitable for the macro level analysis of inheritance. But it is important to keep in mind that the three accounting equations (3.1), (3.2) and (3.3) are by construction fully equivalent.

What kind of data do we need in order to compute equation (3.1)? First, we need data on the wealth-income ratio $\beta_{\mathrm{t}}=\mathrm{W}_{\mathrm{t}} / Y_{\mathrm{t}}$. To a large extent, this is given by existing national accounts data, as described below. It is conceptually important to use private wealth as the numerator (i.e. the sum of all tangible and financial assets owned by private individuals, minus their financial liabilities) rather than national wealth (i.e. the sum of private wealth and government wealth). Private wealth can be transmitted at death, while government wealth cannot. Practically, however, this does not make a big difference, since private wealth usually represents over $90 \%$ of national wealth (i.e. government net wealth is typically positive but small). The choice of the income denominator is unimportant, as long as one uses the same denominator on both sides of the equation. For reasons explained in the introduction, we choose to use national income (rather for instance than personal disposable income) as the denominator.

Next, we need data on the mortality rate $\mathrm{m}_{\mathrm{t}}$. This is the easiest part: demographic data is plentiful and easily accessible. ${ }^{22}$ In practice, children usually own very little wealth and receive very little income. In order to abstract from the large historical variations in infant mortality, and in order to make the quantitative values of the $m_{t}$ and $\mu_{t}$ parameters easier to interpret, we define them over the adult population. That is, we define the mortality rate $m_{t}$ as the adult mortality rate, i.e. the ratio between the number of decedents aged 20-year-old and over and the number of living individuals aged 20-year-old and over.

[^8]Similarly, we define $\mu_{\mathrm{t}}$ as the ratio between the average wealth of decedents aged 20-year-old and over and the average wealth of living individuals aged 20-year-old and over. ${ }^{23}$

Finally, we need data to compute the $\mu_{\mathrm{t}}$ ratio. This is the most challenging part, and also the most interesting part from an economic viewpoint. In order to compute $\mu_{\mathrm{t}}$ we need two different kinds of data. First, we need data on the cross-sectional age-wealth profile. The more steeply rising the age-wealth profile, the higher the $\mu_{\mathrm{t}}$ ratio. Conversely, if the agewealth profile is strongly hump-shaped, then $\mu_{\mathrm{t}}$ will be smaller. Next, we need data on differential mortality. For a given age-wealth profile, the fact that the poor tend to have higher mortality rates than the rich implies a lower $\mu_{t}$ ratio. In the extreme case where only the poor (say, zero-wealth individuals) die, and the rich never die, then the $\mu_{\mathrm{t}}$ ratio will be permanently equal to $0 \%$ (even with a steeply rising cross-sectional age-wealth profile), and there will be no inheritance. There exists a large research literature on differential mortality. We simply borrow the best available estimates from this literature. We checked that these differential mortality factors are consistent with the age-at-death differential between wealthy decedents and poor decedents, as measured by estate tax data and demographic data; they are consistent. ${ }^{24}$

Regarding the age-wealth profile, one would ideally like to use exhaustive, administrative data on the wealth of the living, such as wealth tax data. However such data generally does not exist for long time periods, and/or only covers relatively small segments of the population. Wealth surveys do cover the entire population, but they are not fully reliable (especially for top wealth holders, which might bias estimated age-wealth profiles), and in any case they are not available for long time periods. The only data source offering longrun, reliable raw data on age-wealth profiles appears to be the estate tax itself. ${ }^{25}$ This is wealth-at-death data, so one needs to use the differential mortality factors to convert them back into wealth-of-the-living age-wealth profiles. ${ }^{26}$ This data source combines many advantages: it covers the entire population (nearly everybody has to file an estate tax return in France), and it is available on a continuous and homogenous basis since the beginning of the $19^{\text {th }}$ century. We checked that the resulting age-wealth profiles are

[^9]consistent with those obtained with wealth tax data and (corrected) wealth survey data for the recent period (1990s-2000s); they are consistent. ${ }^{27}$

We have now described how we proceed in order to compute our "economic inheritance flow" series using equation (3.1). There is however one important term that needs to be added to the computation in order to obtain meaningful results. In the real world, inter vivos gifts do exist and play an important role in the process of intergenerational wealth transmission and in shaping the age-wealth profile. In France, gifts have always represented a large fraction of total wealth transmission (around 20\%-30\%), and moreover this fraction has changed a lot over time (currently it is almost $50 \%$ ). Not taking them into account would bias the results in important ways. The simplest way to take gifts into account is to correct equation (3.1) in the following way:

$$
\begin{equation*}
B_{t} / Y_{t}=\mu_{t}^{*} m_{t} W_{t} / Y_{t} \tag{3.1'}
\end{equation*}
$$

With: $\mu_{\mathrm{t}}{ }^{*}=\left(1+\mathrm{v}_{\mathrm{t}}\right) \mu_{\mathrm{t}}=$ gift-corrected ratio between decedents wealth and wealth of the living $\mathrm{V}_{\mathrm{t}}=\mathrm{V}_{\mathrm{t}}^{\mathrm{f0}} / \mathrm{B}_{\mathrm{t}}^{\mathrm{f0}}=$ observed fiscal gift-bequest ratio
$B_{t}^{\text {f0 }}=$ raw fiscal bequest flow (total value of bequests left by decedents during year $t$ )
$V_{t}^{\text {f0 }}=$ raw fiscal gift flow (total value of inter vivos gifts made during year $t$ )

Equation (3.1') simply uses the observed, fiscal gift-bequest ratio during year $t$ and upgrades the economic inheritance flow accordingly. Intuitively, the gift-corrected ratio $\mu_{\mathrm{t}}{ }^{*}$ attempts to correct for the fact that the raw $\mu_{\mathrm{t}}$ under-estimates the true relative importance of decedents' wealth (decedents have already given away part of their wealth before they die, so that their wealth-at-death looks artificially low), and attempts to compute what the $\mu_{\mathrm{t}}$ ratio would have been in the absence of inter-vivos gifts. Of course, this simple way to proceed is not fully satisfactory, since the individuals who make gifts during year $t$ are usually not the same as the individuals who die during year $t$ (on average gifts are made about 7-8 years before the time of death). In the simulated model, we re-attribute gifts to the proper generation of decedents, and re-simulate the entire age-wealth profile dynamics in the absence of gifts. We show that this creates time lags, but does not significantly affect long-run levels and patterns of the inheritance-income ratio.

Before we present and analyse the results of these computations, we give more details about our two main data sources: national accounts data and estate tax data. Readers who feel uninterested by these details might want to go directly to section 4.
3.2. National income and wealth accounts: $Y_{t}$ and $W_{t}$
${ }^{27}$ See Appendix B2 and section 4.3 below.

National income and wealth accounts have a long tradition in France, and available historical series are of reasonably high quality. ${ }^{28}$ In particular, the national statistical institute (Insee) has been compiling official national accounts series since 1949. Homogenous, updated national income accounts series covering the entire 1949-2008 period and following the latest international guidelines were recently released by Insee. These are the series we use in this paper for the post-1949 period, with no adjustment whatsoever. National income $Y_{t}$ and its components are defined according to the standard international definitions: national income equals gross domestic product minus capital depreciation plus net foreign factor income, etc.

Prior to 1949, there exists no official national accounts series in France. However a very complete set of retrospective, annual income accounts series covering the 1896-1949 period was compiled and published by Villa (1994). These series use the concepts of modern national accounts and are based upon a systematic comparison of raw output, expenditure and income series constructed by many authors. Villa also made new computations based upon raw statistical material. Although some of year-to-year variations in this data base are probably fragile, there are good reasons to view these annual series as globally reliable. ${ }^{29}$ These are the series we use for the 1896-1949 period, with minor adjustments, so as to ensure continuity in 1949. Regarding the 1820-1900 period, though a number of authors have produced annual national income series, we are not sure that the limited raw statistical material available for the $19^{\text {th }}$ century makes such an exercise really meaningful. Moreover we do not really need annual series for our purposes. So for the $19^{\text {th }}$ century, we use decennial-averages estimates of national income (these decennial averages are almost identical across the different authors and data sources), and we assume fixed growth rates, saving rates and factor shares within each decade. ${ }^{30}$

The national wealth part of our macro data base requires more care than the national income part. It is only in 1970 that Insee started producing official, annual national wealth estimates in addition to the standard national income estimates. For the post-1970 period, the wealth and income sides of French national accounts are fully integrated and consistent. That is, the balance sheets of the personal sector, the government sector, the corporate sector, and the rest of the world, estimated at asset market prices on January $1^{\text {st }}$ of each year, are fully consistent with the corresponding balance sheets estimated on the previous January $1^{\text {st }}$ and the income and savings accounts of each sector during the

[^10]previous year, and the recorded changes in asset prices. ${ }^{31}$ We use these official Insee balance sheets for the 1970-2009 period, with no adjustment whatsoever. We define private wealth $W_{\mathrm{t}}$ as the net wealth (tangible assets, in particular real estate, plus financial assets, minus financial liabilities) of the personal sector. $W_{t}$ is estimated at current asset market prices (real estate assets are estimated at current real estate prices, equity assets are estimated at current stock market prices, etc.). This is exactly what we want, since our objective is to relate aggregate private wealth to the inheritance flow, and since according to estate tax law - the value of bequests is always estimated at the market prices of the day of death (or on the day the gift is made). Although this is of no use for our purposes, one can also define government wealth $\mathrm{W}_{\mathrm{gt}}$ as the net wealth of the government sector, and national wealth $\mathrm{W}_{\mathrm{nt}}=\mathrm{W}_{\mathrm{t}}+\mathrm{W}_{\mathrm{gt}}$. According to the Insee estimates, private wealth during the 1990s-2000s has always represented around $90 \%-95 \%$ of national wealth. I.e. government wealth is positive but small: government tangible and financial assets only slightly exceed the value of government debt. During the 1970s-1980s, private wealth was equal to about $85 \%-90 \%$ of national wealth. Government net wealth was somewhat bigger than it is today, both because public debt was smaller and because the government owned more tangible and financial assets (the public sector was bigger at that time). ${ }^{32}$

Prior to 1970, we have to use various non-official, national wealth estimates. For the 18201913 period, national wealth estimates are plentiful and relatively reliable. This was a time of almost zero inflation ( $0.5 \%$ per year on average during the 1820-1913 period), so there was no big problem with asset prices. Most importantly, the economists of the time were literally obsessed with national wealth (which they found to be much more interesting than national income), and many of them produced relatively sophisticated national wealth estimates. They used the decennial censuses of tangible assets organized by the tax administration (the tax system of the time relied extensively on the property values of real estate, land and business assets, so such censuses played a critical role). They took into account the growing stock and bond market capitalisation and the booming foreign assets, and they explained in a precise and careful manner how they made all the necessary corrections in order to avoid all forms of double counting. We certainly do not pretend that these national wealth estimates are perfectly comparable to the modern, official balance sheets. In particular, these estimates are never available on an annual basis, and they certainly cannot be used to do short run business cycle analysis. But as far as decennial averages are concerned, we consider that the margin of error on these estimates does not exceed $5 \%-10 \%$. As compared to the enormous historical variations in aggregate wealthincome ratios and in the inheritance-income ratio, in which we are primarily interested in, such margins of errors are negligible. According to these national wealth estimates, private

[^11]wealth at that time accounted for as much as $97 \%-98 \%$ of national wealth, i.e. net government wealth was slightly positive but negligible.

The period 1914-1969 is the time period for which French national wealth estimates are the most problematic. This was a chaotic time for wealth, both because of war destructions and because of large inflation and wide variations in the relative price of the various assets. Very few economists compiled detailed, reliable national balance sheets for this time period. We proceed as follows. We use only two data points, namely the national wealth estimate for year 1925 due to Colson (1927), and the national wealth estimate for year 1954 due to Divisia, Dupin and Roy (1956). These are the two most sophisticated estimates available for this time period. They both rely on a direct wealth census method, and they both attempt to estimate assets and liabilities at asset market prices prevailing in 1925 and 1954, which is what we want. Moreover, Colson is the author of some of the most sophisticated pre-World War 1 national wealth estimates (we used his estimates for 1896 and 1913), and his 1925 computations are based on the same methods and sources as those used for 1896 and 1913. Divisia and his co-authors view the Colson 1896-19131925 estimates as their model, and they also attempt to follow the same methodology. To the extent that national wealth can be estimated during such a chaotic time period, this is probably the best one can find.

For the missing years, we estimate private wealth $W_{t}$ by using a simple wealth accumulation equation, based upon the private saving flows $S_{t}$ coming from national income accounts. Generally speaking, year-to-year variations in private wealth $W_{t}$ can be due either to volume effects (savings) or to price effects (asset prices might rise or fall relatively to consumer prices). That is, the accumulation equation for private wealth can be written as follows:

$$
\begin{equation*}
W_{t+1}=\left(1+q_{t+1}\right)\left(1+p_{t+1}\right)\left(W_{t}+S_{t}\right) \tag{3.4}
\end{equation*}
$$

In equation (3.4), $p_{t+1}$ is consumer price inflation between year $t$ and year $t+1$, and $q_{t+1}$ is the real rate of capital gain (or capital loss) between year $t$ and year $t+1$, which we define as the excess of asset price inflation over consumer price inflation. For the 1970-2009 period, since French national income and wealth accounts are fully integrated, $q_{t}$ can indeed be interpreted as the real rate of capital gains. For the pre-1970 period, $q_{t}$ is better interpreted as a residual error term: it includes real asset price inflation, but it also includes all the variations in private wealth that cannot be accounted for by saving flows. For simplicity, we assume a fixed $\mathrm{q}_{\mathrm{t}}$ factor during the 1954-1970 period (i.e. we compute the implicit average $\mathrm{q}_{\mathrm{t}}$ factor needed to account for 1970 private wealth, given 1954 private wealth and 1954-1969 private savings flows). We do the same for the 1925-1954 period, the 1913-1925 period, and for each decade of the 1820-1913 period. The resulting
decennial averages for the private wealth-national income ratio $\beta_{t}=W_{t} / Y_{t}$ are plotted on Figure 2. Summary statistics on the accumulation of private wealth in France over the entire 1820-2009 period are given on Table 1.

Again, we do not pretend that the resulting annual series are fully satisfactory, and we certainly do not recommend that one uses them for short run business cycle analysis, especially for the 1913-1925 and 1925-1954 sub-periods, for which the simplifying assumption of a fixed capital gain effect makes little sense. However we believe that the resulting decennial averages are relatively precise. In particular, it is re-insuring to see that most of wealth accumulation in the medium and long run seems to be well accounted for by savings. This suggests that saving rates are reasonably well measured by our national accounts series, and that in the long run there exists no major divergence between asset prices and consumer prices. The fact that our private wealth series delivers economic inheritance flow estimates that are reasonably well in line with the observed fiscal flow also gives us confidence about our wealth estimates.

A few additional points about the long-run evolution of the wealth-income ratio $\beta_{t}$ might be worth noting here. ${ }^{33}$ Consider first the 1820-1913 period. We find that $\beta_{\mathrm{t}}$ gradually rose from about $550 \%-600 \%$ around 1820 to about $650 \%-700 \%$ around 1900-1910 (see Figure 2). The real growth rate $g$ of national income was $1.0 \% .^{34}$ The savings rate s was about $8 \%-9 \%$, so that the average savings-induced wealth growth rate $g_{w s}=s / \beta$ was $1.4 \%$. I.e. it was larger than g . This explains why the wealth-income ratio was rising during the $19^{\text {th }}$ century: savings were slightly higher than the level required for a steady-state growth path (i.e. the savings rate was slightly higher than $s^{*}=\beta g=6 \%-7 \%$ ). The observed real growth rate of private wealth $g_{w}$ was actually $1.3 \%$, i.e. slightly below $g_{w s}$. In our accounting framework, we attribute the differential to changes in the relative price of assets, and we find a modest negative q effect ( $-0.1 \%$ ) (see Table 1 ). Of course, it could just be that we slightly overestimate $19^{\text {th }}$ century saving rates, or that we slightly underestimate the $19^{\text {th }}$ century rise in the wealth-income ratio, or both. But the important point is that our stock and flow series are broadly consistent. Although the data is imperfect, it is also well established that a very substantial fraction of the $19^{\text {th }}$ century rise in the wealth-income ratio (and possibly all of it) went though the accumulation of large foreign assets. ${ }^{35}$

Consider now the 1913-2009 period. The real growth rate $g$ of national income was $2.6 \%$, thanks to the high growth postwar decades. The real growth rate of private wealth $g_{w}$ was

[^12]$2.4 \%$. Given observed saving flows (and taking into account wartime capital destructions, which we include in volume effects), private wealth should have grown slightly faster, i.e. we find that the saving-induced wealth growth rate $g_{\text {ws }}$ was $2.9 \%$. We again attribute the differential to real capital gains, and we find a modest negative q effect (-0.4\%) (see Table 1). Taken literally, this would mean that the 1949-2009 gradual rise in the relative price of assets has not yet fully compensated the 1913-1949 fall, and that asset prices are currently about $30 \%$ lower than what they were at the eve of World War 1. Again, it could also be that we slightly overestimate $20^{\text {th }}$ century saving flows, or underestimate end-ofperiod wealth stocks. ${ }^{36}$ The important point is that our stock and flow data sources are mutually consistent. In the long run, the bulk of wealth accumulation is well accounted for by savings, both during the $19^{\text {th }}$ and the $20^{\text {th }}$ century. As a first approximation, the 19131949 fall in the relative price of assets seems to have been almost exactly compensated by the 1949-2009 rise, so that the total 1913-2009 net effect is close to zero.

The other important finding is that the 1913-1949 fall in the aggregate wealth-income ratio was not due - for the most part - to the physical destructions of the capital stock that took place during the wars. We find that $\beta_{t}$ dropped from about 600\%-650\% in 1913 to about $200 \%-250 \%$ in 1949. Physical capital destructions per se seem to account for little more than $10 \%$ of the total fall. On the basis of physical destructions and the observed saving response (saving flows were fairly large in the 1920s and late 1940s), we find that private wealth should have grown at $\mathrm{g}_{\mathrm{ws}}=0.9 \%$ per year between 1913 and 1949, i.e. almost as fast as national income ( $\mathrm{g}=1.3 \%$ ). However the market value of private wealth fell dramatically ( $g_{w}=-1.7 \%$ ), which we attribute to a large negative $q$ effect ( $q=-2.6 \%$ ). This large real rate of capital loss can be broken down into a variety of factors: holders of nominal assets (public and private bonds, domestic and foreign) were literally expropriated by inflation; real estate prices fell sharply relatively to consumer prices (probably largely due to sharp rent control policies enacted in the 1920s and late 1940s); and stock prices also fell to historical lows in 1945 (probably reflecting the dramatic loss of faith in capital markets, as well as the large nationalization policies and capital taxes enacted in the aftermath of World War 2). In effect, the 1914-1945 political and military shocks generated an unprecedented wave of anti-capital policies, which had a much larger impact on private wealth than the wars themselves.

This asset price effect explains why the wealth-income ratio also seems to have fallen substantially in countries whose territories were not directly hit by the wars. In the U.K., the

[^13]private wealth-national income ratio was apparently as large as $650 \%-750 \%$ in the late $19^{\text {th }}$ and early $20^{\text {th }}$ century, down to $350 \%-400 \%$ in the 1950 s-1970s, up to about $450 \%-$ $550 \%$ in the 1990s-2000s. ${ }^{37}$ In the U.S., it seems to have declined from about 550\%-600\% in the early $20^{\text {th }}$ century and in the interwar period to about $350 \%-400 \%$ in the 1950 s1970s, up to $450 \%-500 \%$ in the 1990 s-2000s. ${ }^{38}$ This suggests that the U.K. and the U.S. have gone through the same U-shaped pattern as France - albeit in a somewhat less pronounced manner, which seems consistent with the above observations. We stress however that these U.K.-U.S. series are not fully homogenous over time; nor are they fully comparable to our French series. We report them for illustrative purposes only. The Ushaped pattern is probably robust, but the exact levels should be interpreted with caution.

Finally, it is worth noting that if we use disposable income rather than national income as the denominator, then the wealth-income ratios reached in France in the 2000s (750\%$800 \%$ ) appear to be slightly higher than the levels observed in the $19^{\text {th }}$ and early $20^{\text {th }}$ century, rather than slightly smaller (see Figure 5). We feel that it is more justified to look at the wealth-national income ratios, but this is a matter of perspective.

### 3.3. Estate tax data: $B_{t}{ }^{f}, \mu_{t}$ and $v_{t}$

Estate tax data is the other key data source used in this paper. ${ }^{39}$ It plays an essential role for several reasons. First, because of various data imperfections (e.g. regarding national wealth estimates), we thought that it was important to compute two independent measures of inheritance flows: one "economic flow" indirect measure (based upon national wealth estimates and mortality tables, as described above) and one "fiscal flow" direct measure. The fiscal flow is a direct measure in the sense that it was obtained simply by dividing the observed aggregate bequest and gift flow reported to the tax administration (with a few corrections, see below) by national income, and therefore makes no use at all of national wealth estimates. Next, we need estate tax data in order to compute the gift-bequest ratio $\mathrm{V}_{\mathrm{t}}=\mathrm{V}_{\mathrm{t}}^{\mathrm{f0}} / \mathrm{B}_{\mathrm{t}}^{\mathrm{f0}}$, and in order to obtain reliable, long-run data on the age-wealth profile and to compute the $\mu_{\mathrm{t}}$ ratio. Finally, we also use estate tax data in order to know the age structure of decedents, heirs, donors and donees, which we need for our simulations.

[^14]French estate tax data is exceptionally good, for one simple reason. As early as 1791, shortly after the abolition of the tax privileges of the aristocracy, the French National Assembly introduced a universal estate tax, which has remained in force since then. This estate tax was universal because it applied both to bequests and to inter-vivos gifts, at any level of wealth, and for nearly all types of property (both tangible and financial assets). The key characteristic of the tax is that the successors of all decedents with positive wealth, as well as all donees receiving a positive gift, have always been required to file a return, no matter how small the estate was, and no matter whether the heirs and donees actually ended up paying a tax or not. This followed from the fact that the tax was thought more as a registration duty than as a tax: filling a return has always been the way to register the fact that a given property has changed hands and to secure one's property rights. ${ }^{40}$

Between 1791 and 1901, the estate tax was strictly proportional. The tax rate did vary with the identity of the heir or donee (children and surviving spouses have always faced much lower tax rates than other successors in the French system), but not with the wealth level. The proportional tax rates were fairly small (generally $1 \%-2 \%$ for children and spouses), so there was really very little incentive to cheat. The estate tax was made progressive in 1901. In the 1920s, tax rates were sharply increased for large estates. In 1901, the top marginal rate applying to children heirs was as small as $5 \%$; by the mid 1930 s it was $35 \%$; it is currently $40 \%$. Throughout the $20^{\text {th }}$ century these high top rates were only applied to small segments of the population and assets. So the aggregate effective tax rate on estates has actually been relatively stable around $5 \%$ over the past century in France. ${ }^{41}$ Most importantly, the introduction of tax progressivity did not significantly affect the universal legal requirement to fill a return, no matters how small the bequest or gift.

There is ample evidence that this legal requirement has been applied relatively strictly, both before and after the 1901 reform. In particular, the number of estate tax returns filled each year has generally been around $65 \%$ of the total number of adult decedents (about 350,000 yearly returns for 500,000 adult decedents, both in the 1900s and in the 2000s). This is a very large number, given that the bottom $50 \%$ of the population hardly owns any wealth at all. We do upgrade the raw fiscal flow in order to take non-filers into account, but the point is that the corresponding correction is small (generally around $5 \%-10 \%$ ).

The other good news for scholars is that the raw tax material has been well archived. Since the beginning of the $19^{\text {th }}$ century, the tax authorities transcribed individual returns in

[^15]registers that have been preserved. In a previous paper we used these registers to collect large micro samples of Paris decedents every five year between 1807 and 1902, which allowed us to study the changing concentration of wealth and the evolution of age-wealth profiles. ${ }^{42}$ Ideally one would like to collect micro samples for the whole of France over the two-century period, but this has proved to be too costly so far.

So in this paper we rely mostly on aggregate national data collected by the tax administration. For the 1826-1964 period, we use the estate tax tabulations published on a quasi-annual basis by the French Ministry of Finance. For the whole period, these tables indicate the aggregate value of bequests and gifts reported in estate tax returns, which is the basic information that we need. Starting in 1902, these annual publications also include detailed tabulations on the number and value of bequests and gifts broken down by size of estate and age of decedent or donor. These tabulations were abandoned in the 1960s-1970s, when the tax administration started compiling electronic files with nationally representative samples of bequest and gift tax returns. We use these so-called "DMTG" micro files for years 1977, 1984, 1987, 1994, 2000 and 2006. The data is not annual, but it is very detailed. Each micro-file includes all variables reported in tax returns, including the value of the various types of assets, total estate value, the share going each heir or donee, and the demographic characteristics of decedents, heirs, donors and donees.

We proceed as follows. We start from the raw fiscal bequest flow $B_{t}{ }^{f 0}$, i.e. the aggregate net wealth transmitted at death, as reported to tax authorities by heirs, whoever they are. In particular, we do not exclude the estate share going to surviving spouses, first because it has always been relatively small (about 10\%), ${ }^{43}$ and next because we choose in the present paper to adopt a gender-free, individual-centred approach to inheritance. So we ignore marriage and gender issues altogether, which given our aggregate perspective seems to be the most appropriate option. ${ }^{44}$

We first make an upward correction to $B_{t}^{\text {f0 }}$ for non filers (see above), and we then make another upward correction for tax exempt assets. When the estate tax was first created, the major exception to the universal tax base was government bonds, which benefited from a general estate tax exemption until 1850. Between 1850 and World War 1, very few assets were exempted (except fairly specific assets like forests). Shortly after World War 1, and again after World War 2, temporary exemptions were introduced for particular types

[^16]of government bonds. In order to foster reconstruction, new real estate property built between 1947 and 1973 also benefited from a temporary exemption. Most importantly, a general exemption for life insurance assets was introduced in 1930. It became very popular in recent decades. Life insurances assets were about $2 \%$ of aggregate wealth in the 1970s and grew to about $15 \%$ in the 2000s. Using various sources, we estimate that the total fraction of tax exempt assets in aggregate private wealth gradually rose from less than $10 \%$ around 1900 to $20 \%$ in the interwar period, $20 \%-25 \%$ in the 1950 s-1970s and $30 \%-35 \%$ in the 1990s-2000s. We upgrade the raw fiscal bequest flow accordingly.

We apply the same upward corrections to inter vivos gifts, leaving the gift-bequest ratio $v_{t}$ unaffected. To the extent that gifts are less well reported to tax authorities than bequests, this implies that we probably under-estimate their true economic importance. Also, in this paper we entirely ignore informal monetary and in-kind transfers between households, as well as parental transfers to children taking the form of educational investments, tuition fees and other non-taxable gifts (which ideally should all be included in the analysis, in one way or another). ${ }^{45}$ That is, we only consider formal, potentially taxable gifts.

## 4. The U-shaped pattern of inheritance: a simple decomposition

The accounting equation $B_{t} / Y_{t}=\mu_{t}^{*} m_{t} W_{t} / Y_{t}$ allows for a simple and transparent decomposition of changes in the aggregate inheritance flow. Here the important finding is that the long-run $U$-shaped pattern of $B_{t} / Y_{t}$ is the product of three $U$-shaped curves, which explains why it was so pronounced. We take these three effects in turn: the aggregate wealth-income effect $W_{t} / Y_{t}$, the mortality rate effect $m_{t}$, and the $\mu_{t}^{*}$ ratio effect.

### 4.1. The aggregate wealth-income ratio effect $W_{t} / Y_{t}$

We already described the U-shaped pattern the aggregate wealth-income ratio $\beta_{t}$ (see Figure 2). By comparing this pattern with that of the inheritance flow $b_{y t}$ (see Figure 1), one can see that the 1913-1949 decline in the aggregate wealth-income ratio explains about half of the decline in the inheritance-income ratio. Between 1913 and 1949, $\beta_{\mathrm{t}}$ dropped from $650 \%-700 \%$ to $200 \%-250 \%$. I.e. it was divided by a factor of about $2.5-3$. In the meantime, $b_{y t}$ dropped from $20 \%-25 \%$ to $4 \%$. I.e. it was divided by a factor of about 5-6.

### 4.2. The mortality rate effect $m_{t}$

[^17]Where does the other half of the decline in the inheritance-income ratio come from? By construction, it comes from a combination of $\mu_{t}{ }^{*}$ and $m_{t}$ effects. The simplest term to analyze is the mortality rate $\mathrm{m}_{\mathrm{t}}$. The demographic history of France since 1820 is simple. Population was growing at a small rate during the $19^{\text {th }}$ century (less than $0.5 \%$ per year), and was quasi-stationary around 1900 ( $0.1 \%$ ). The only time of sustained population growth during the past two centuries was due to the well-known postwar baby-boom, with population growth rates around $1 \%$ in the 1950s-1960s. Population growth has been declining since then, and in the 1990s-2000s it was approximately $0.5 \%$ per year (about a third of which comes from net migration flows). According to official projections, population growth will be less than $0.1 \%$ by 2040-2050, with a quasi-stationary population after 2050. Adult population was about 20 millions in the 1820s, 30 millions in the 1950s, 50 millions in the 2010s, and is projected to stabilize below 60 millions.

The evolution of mortality rates follows directly from this and from the evolution of life expectancy. Between 1820 and 1910, the mortality rate was relatively stable around $2.2 \%-$ $2.3 \%$ per year (see Figure 3). This corresponds to the fact that the population was growing at a very small rate, and that life expectancy was stable around 60, with a slight upward trend. In a world with a fully stationary population and a fixed adult life expectancy equal to 60 , then the adult mortality rate (i.e. the mortality rate for individuals aged 20-year-old and above) should indeed be exactly equal to $1 / 40=2.5 \%$. Since population was rising a little bit, the mortality rate was a bit below that.

There was a purely temporary rise in mortality rates in the 1910s and 1940s due to the wars. Ignoring this, we have a regular downward trend in the mortality rate during the $20^{\text {th }}$ century, with a decline from about $2.2 \%-2.3 \%$ in 1910 to about $1.6 \%$ in the $1950 \mathrm{~s}-1960 \mathrm{~s}$ and $1.1 \%-1.2 \%$ in the 2000 s . According to official projections, this downward trend is now over, and the mortality rate is bound to rise in the coming decades, and to stabilize around $1.4 \%-1.5 \%$ after 2050 (see Figure 3). This corresponds to the fact that the French population is expected to stabilize by 2050 , with an age expectancy of about 85 , which implies a stationary mortality rate equal to $1 / 65=1.5 \%$. The reason why the mortality rate is currently much below this steady-state level is because the large baby-boom cohorts are not dead yet. When they die, i.e. around 2020-2030, then the mortality rate will mechanically increase, and so will the inheritance flow. This simple demographic arithmetic is obvious, but important. In the coming decades, this is likely to be a very big effect in countries with negative projected population growth (Spain, Italy, Germany). In the extreme case where each couple has only one kid, the new cohorts are twice as small as the dying cohorts, and inheritance flows can mechanically become very large.

However the large inheritance flows observed in the 2000s are not due to a mortally rate effect. The U-shaped mortality effect will start operating only in future decades. The 2000-

2010 period actually corresponds to the lowest historical mortality ever observed, with mortality rates as low as $1.1 \%-1.2 \%$. On the basis of mortality rates alone, the inheritance flow in the 1990s-2000s should have been much smaller than what we actually observe.

### 4.3. The $\mu_{t}{ }^{*}$ ratio effect

So why has there been such a strong recovery in the inheritance flow since the 1950s1960s, and why is the inheritance flow so large in the 1990s-2000s? We now come to the most interesting part, namely the $\mu_{\mathrm{t}}{ }^{*}$ ratio effect. Here it is important to distinguish between the raw ratio $\mu_{\mathrm{t}}$ and the gift-corrected ratio $\mu_{\mathrm{t}}{ }^{*}=\left(1+\mathrm{v}_{\mathrm{t}}\right) \mu_{\mathrm{t}}$. We plot on Figure 4 the historical evolution of the $\mu_{\mathrm{t}}$ and $\mu_{\mathrm{t}}{ }^{*}$ ratios, as estimated using observed age-wealth-at-death profiles and differential mortality parameters. We plot on Figure 5 the inheritance flow-private wealth ratio $b_{w t}=m_{t} \mu_{t}{ }^{*}$ and compare it to the mortality rate $m_{t}$.

Between 1820 and 1910, the $\mu_{\mathrm{t}}$ ratio was around $130 \%$. I.e. on average decedents' wealth was about $30 \%$ bigger than the average wealth of the living. There was actually a slight upward trend, from about $120 \%$ in the 1820s to about $130 \%-140 \%$ in $1900-1910$. But this upward trend disappears once one takes inter vivos gifts into account: the gift-bequest ratio $v_{t}$ was as high as $30 \%-40 \%$ during the 1820 s-1850s, and then gradually declined, before stabilizing at about $20 \%$ between the 1870 s and 1900-1910. ${ }^{46}$ When we add this gift effect, i.e. when we take into account the fact that decedents have already given away about $30 \%-40 \%$ of their wealth when they die in the 1820 s-1840s, and about $20 \%$ of their wealth when they die in the $1870 \mathrm{~s}-1910 \mathrm{~s}$, then we find that the gift-corrected $\mu_{\mathrm{t}}{ }^{*}$ ratio was stable at about 160\% during the 1820-1913 period (see Figure 4).

During this entire period, cross-sectional age-wealth profiles were steeply increasing up until the very old, and were becoming more and more steeply increasing over time. ${ }^{47}$ Here we use observed profiles for the all of France. In Paris, where many of the top wealth holders lived, age-wealth profiles were even more steeply increasing. ${ }^{48}$

The 1913-1949 capital shocks clearly had a strong disturbing impact on age-wealth profiles. Observed profiles gradually become less and less steeply-increasing at old age after World War 1, and shortly become hump-shaped in the aftermath of World War $2 .{ }^{49}$ Consequently, our $\mu_{\mathrm{t}}$ ratio estimates declined from about $140 \%$ at the eve of World War 1 to about $90 \%$ in the 1940s (see Figure 4). The gift-bequest ratio was stable around $20 \%$ throughout this period, so the $\mu_{\mathrm{t}}{ }^{*}$ went through a similar evolution.

[^18]One possible explanation for this change in pattern is that it was too late for the elderly to recover from the capital shocks (war destruction, capital losses), while active and younger cohorts could earn labour income and accumulate new wealth. It could also be that elderly wealth holders were hit by proportionally larger shocks, e.g. because they held a larger fraction of their assets in nominal assets such as public bonds.

The most interesting fact is the strong recovery of the $\mu_{\mathrm{t}}$ and $\mu_{\mathrm{t}}{ }^{*}$ ratios which took place since the 1950s. The raw age-wealth-at-death profiles gradually became upward sloping again. In the 1900s-2000s, decedents aged 70 and over are about $20 \%-30 \%$ richer than the 50-to-59-year-old decedents. ${ }^{50}$ As a consequence, the $\mu_{\mathrm{t}}$ ratio gradually rose from about $90 \%$ in the 1940 s-1950s to over $120 \%$ in the 2000s (see Figure 4).

Next, and most importantly, the gift-bequest ratio $v_{t}$ rose enormously since the 1950s. The gift-bequest ratio was about $20 \%-30 \%$ in the 1950s-1960s, and then gradually increased to about $40 \%$ in the 1980 s, $60 \%$ in the 1990s and over $80 \%$ in the 2000 s. This is by far the highest historical level ever observed. Gifts currently represent almost $50 \%$ of total wealth transmission (bequests plus gifts) in France. That is, when we observe wealth at death, or wealth among the elderly, we are actually observing the wealth of individuals who have already given away almost half of their wealth. So it would make little sense to study agewealth profiles without taking gifts into account. Gifts are probably less well reported than bequests to the tax administration, so it is hard to see how our tax-data-measured $v_{t}$ ratio can be over-estimated. If anything, we probably underestimate the gift effect. We do not know whether such as large rise in gifts also occurred in other countries. ${ }^{51}$

The age differential between decedents and donors has remained relatively stable around $7-8$ years throughout the $20^{\text {th }}$ century, and in particular during the past few decades. On average, people have always made gifts about 7-8 years before they die. So the impact of gifts on the average age at which individuals receive wealth transfers has been relatively limited. We compute the evolution of the average age of "receivers" (by weighting average age of heirs and average age of donees by the relevant amounts), and we find that the rise

[^19]of gifts since the 1980s merely led to a pause in the historical rise in the average age of receivers (currently about 45-year-old), but not to an absolute decline. ${ }^{52}$

The most plausible interpretation for this large increase in gifts is the rise in life expectancy: wealthy parents realize that they are not going to die very soon, and decide that they should help their children to buy an apartment or start a business before they die. Tax incentives might also have played a role. ${ }^{53}$ There is an issue as to whether such a high gift-bequest ratio is sustainable in the long run, which we address in the simulations.

For the time being, it is legitimate to add the gift flow to the bequest flow, especially given the relatively small and stable age differential between decedents and donors. Consequently, we find that the gift-corrected $\mu_{t}{ }^{*}$ ratio has increased enormously since World War 2, from about $120 \%$ in the 1940s-1950s to over $180 \%$ in the 1990 s and over $220 \%$ in the 2000 s (see Figure 4).

To summarize: the long run decline in the mortality $m_{t}$ seems to have been (partially) compensated by a long run increase in the $\mu_{t}{ }^{*}$ ratio. Consequently, the product of two, i.e. the inheritance-wealth ratio $b_{w t}=m_{t} \mu_{t}^{*}$, declined much less than the mortality rate: $b_{w t}$ was about $3.3 \%-3.5 \%$ in the $19^{\text {th }}$ century (the estate multiplier $\mathrm{e}_{\mathrm{t}}=1 / \mathrm{b}_{\mathrm{wt}}$ was about 30 ), and it is above $2.5 \%$ in the 2000s (the estate multiplier is about 40).

## 5. Wealth accumulation, inheritance \& growth: a simple steady-state model

Why is it that the long-run decline in mortality rate $m_{t}$ seems to be compensated by a corresponding increase in the $\mu_{\mathrm{t}}$ ratio? I.e. why does the relative wealth of the old seem to rise with life expectancy? More generally, what are the economic forces that seem to be pushing for a constant inheritance-income steady-state ratio $b_{y t}$ (around 20\% of national income), independently from life expectancy and other parameters?

One obvious explanation as to why wealth tends to get older in aging societies is because individuals wait longer before they inherit. However there are other effects going on, so it is useful to clarify this effect with a stylized model, before moving to full-fledged simulations.

Consider first a standard Solow-type wealth accumulation model with class saving. National income $Y_{t}$ is given by a production function $F\left(K_{t}, H_{t}\right)$, where $K_{t}$ is the capital stock,

[^20]$H_{t}=L_{t} e^{g t}$ Is human capital (efficient labor), $g$ is the exogenous rate of labor productivity growth, and $L_{t}$ is labor supply (raw labor). Assuming away government debt and assets, and foreign assets (closed economy), private wealth $\mathrm{W}_{\mathrm{t}}=\mathrm{K}_{\mathrm{t}}$, so the wealth-income ratio is equal to the domestic capital-output ratio: $\beta_{t}=W_{t} / Y_{t}=K_{t} / Y_{t}$. With a Cobb-Douglas production function $F(K, H)=K^{\alpha} H^{1-\alpha}$, we have constant factor shares: $Y_{K t}=\alpha Y_{t}, Y_{L t}=(1-\alpha) Y_{t}$ and $r_{t}=\alpha / \beta_{t}$. With an exogenous saving rate $s=s=\alpha s_{K}+(1-\alpha) s_{L}$, the long-run wealth-income ratio and rate of return are given by the Harrod-Domar-Solow formula. As $t \rightarrow+\infty, \beta_{t} \rightarrow \beta^{*}$ and $r_{t} \rightarrow r^{*}$, with:
\[

$$
\begin{equation*}
\beta^{*}=s / g \text { and } r^{*}=\alpha / \beta^{*}=\alpha g / s \tag{5.1}
\end{equation*}
$$

\]

Example: If the savings rate $\mathrm{s}=10 \%$ and the growth rate $\mathrm{g}=2 \%$, then the long-run wealthincome ratio $\beta^{*}=500 \%$. If the Cobb-Douglas capital share $\alpha=30 \%$, then this corresponds to a long-run rate of return $r^{*}=\alpha / \beta^{*}=6 \%$.

Now assume pure class saving: $s_{L}=0, s_{K}>0$. E.g. $s_{L}=0 \%, s_{K}=20 \%, \alpha=30 \%$, so that $s=\alpha s_{k}=6 \%$. With $g=1 \%$, we have $\beta^{*}=s / g=600 \%$, and $r^{*}=\alpha / \beta^{*}=5 \%$. Wealth holders get a $5 \%$ return, consume $80 \%$ and save $20 \%$, so that $W_{t}$ grows at $1 \%$, just like $Y_{t}$.

Take a simple deterministic, stationary demographic structure. Everybody becomes adult at age $a=A$, has exactly one kid at age $a=H>A$, and dies at age $D>H$. As a consequence everybody inherits at age $\mathrm{a}=\mathrm{I}=\mathrm{D}-\mathrm{H}$. This is a gender free population. There is no inter vivos gift: all wealth is transmitted at death. Total adult population $N_{t}$ includes a mass $N_{t}(a)=1$ of individuals of age a $(A \leq a \leq D)$ and is permanently equal to $D-A$. The adult mortality rate $m_{t}$ is also stationary and is given by:

$$
\begin{equation*}
m_{t}=m^{*}=\frac{1}{D-A} \tag{5.2}
\end{equation*}
$$

Example. Around 1900, we have $A=20, H=30$ and $D=60$, so that people inherit at age $I=D-$ $H=30$, and $m^{*}=1 /(D-A)=1 / 40=2.5 \%$. Around 2020, we have $A=20, H=30$ and $D=80$, so that people inherit at age $I=D-H=50$, and $m^{*}=1 /(D-A)=1 / 60=1.7 \%$.

Then the steady-state age-wealth profile $\mathrm{w}_{\mathrm{t}}(\mathrm{a})$ takes a simple form (see Figure 6):

If a©A, I[, then $w_{t}(a)=0$
If $a$ © I, D], then $w_{t}(a)=\bar{w}_{t}$

Since $s_{L}=0$, young individuals have zero wealth until the time they inherit. Then, at age $a=1$, everybody inherits: some inherit very little or nothing at all, some inherit a lot, depending on the cross-sectional distribution, and on average they inherit $b_{t}=w_{t}(I)=w_{t}(D)$. So at age $a=I$ average wealth $w_{t}(a)$ jumps to some positive level $\bar{w}_{t}=b_{t}$. The interesting point is that
in the cross-section all age groups with age a between I and $D$ have the same average wealth $w_{t}(a)=\bar{w}_{t}$. This is because in steady-state the growth effect and the saving effect exactly compensate each other. Take the group of individuals with age $a>1$ at time $t$. They inherited $a-I$ years ago, at time $s=t-a+1$. They received average bequests $b_{s}=w_{s}(1)$ that are smaller than the average bequests $b_{t}=w_{t}(I)$ inherited at time $t$ by the l-year-old. Since everything grows at rate $g$ in steady-state, we simply have: $b_{s}=e^{-g(a-l)} b_{t}$. But although they received smaller bequests, they saved a fraction $s_{K}=g / r^{*}$ of the corresponding return, so at time $t$ their inherited wealth is now equal to: $w_{t}(a)=e^{s k r^{*}(a-l)} e^{-g(a-1)} b_{t}=b_{t}=w_{t}(I)=\bar{w}_{t}$.

Given this age-wealth profile, the average wealth $w_{t}$ over all age groups a©i,D] is given by: $w_{t}=(D-I) \bar{w}_{t} /(D-A)=H \bar{w}_{t} /(D-A)$. It follows that the steady-state relative wealth of decedents $\mu_{t}=w_{t}(D) / w_{t}=\bar{w}_{t} / w_{t}$ is entirely determined by demographic parameters:

$$
\begin{equation*}
\boldsymbol{\mu}^{*}=\frac{w_{t}(D)}{w_{t}}=\frac{D-A}{H} \tag{5.3}
\end{equation*}
$$

Once we know $\mu^{*}$, we can compute steady-state inheritance flow ratios $b_{w}{ }^{*}=B_{t} / W_{t}=m^{*} \mu^{*}$ and $b_{y}{ }^{*}=B_{t} / Y_{t}=m^{*} \mu^{*} \beta^{*}$. Since the mortality rate $m^{*}=1 /(D-A)$, the product $m^{*} \mu^{*}$ is simply equal to one divided by generation length $H$, and does not depend on adult life length $D-A$. We summarize these observations in the following proposition:

Proposition 1. Assume pure class savings: $s_{\mathrm{L}}=0 \& s_{\mathrm{K}}>0$. As $t \rightarrow+\infty, \mu_{\mathrm{t}} \rightarrow \mu^{*}, b_{\mathrm{wt}} \rightarrow b_{w}{ }^{*}$ and $b_{y t} \rightarrow b_{y}{ }^{*}$. Steady-state ratios $\mu^{*}, b_{w}{ }^{*}$ and $b_{y}{ }^{*}$ are uniquely determined as follows:
(1) The ratio $\mu^{*}$ between average wealth of decedents and average adult wealth depends solely on demographic parameters: $\boldsymbol{\mu}^{*}=\boldsymbol{\rho}=(\mathrm{D}-\mathrm{A}) / \mathbf{H}(>1)$.
(2) The inheritance flow-private wealth ratio $b_{w}{ }^{*}=\mu^{*} m^{*}$ and the estate multiplier $e^{*}=1 / b_{w}{ }^{*}$ depend solely on generation length $H: b_{w}{ }^{*}=1 / H$ and $e^{*}=H$
(3) The inheritance flow-national income ratio $b_{y}{ }^{*}=\mu^{*} m^{*} \beta^{*}$ depends solely on the aggregate wealth-income ratio $\beta^{*}$ and on generation length $H: \quad b_{y}{ }^{*}=\beta^{*} / \mathbf{H}$

Proposition 1 is simple, but powerful. It holds for any growth rate g , saving rate $\mathrm{s}_{\mathrm{K}}$, and life expectancy D. It says that societies with a higher life expectancy $D$ have both lower mortality rates $\mathrm{m}_{\mathrm{t}}$ and higher $\mu_{\mathrm{t}}$ ratios. In steady state both effects exactly compensate each other, so that the product $b_{w t}=m_{t} \mu_{\mathrm{t}}$ does not depend on life expectancy. It only depends on generation length $H$, i.e. the average age at which people have children -a parameter which has been relatively constant over the development process (around $\mathrm{H}=30$ ). If the wealth-income ratio $\beta^{*}$ also tends to be constant in the long run (around $\beta^{*}=600 \%$ ), then we have a simple explanation as to why the aggregate inheritance flow $b_{y}{ }^{*}=\beta^{*} / \mathrm{H}$ always seems to return to approximately $20 \%$ of national income.

The intuition is the following: in aging societies with higher life expectancy, people die less often, but they die with higher relative wealth, so that the aggregate inheritance flow is unchanged. In effect, the entire wealth profile is simply shifted towards older age groups: one has to wait longer before inheritance, but one inherits larger amounts, so that from a lifetime perspective inheritance is just as important as before. ${ }^{54}$

Example. Assume $\beta^{*}=600 \%$ and $H=30$. Then $b_{w}{ }^{*}=1 / H=3.3 \%$ and $b_{y}{ }^{*}=\beta^{*} / H=20 \%$. l.e. the aggregate inheritance flow equals $20 \%$ of national income, irrespective of other parameter values, and in particular irrespective of life expectancy $D$.

- Around 1900, we have $\mathrm{A}=20, \mathrm{H}=30$ and $\mathrm{D}=60$, so that people inherit at age $\mathrm{I}=\mathrm{D}-\mathrm{H}=30$. In steady-state, $m^{*}=1 /(D-A)=2.5 \%$ and $\mu^{*}=(D-A) / H=133 \%$. Then $b_{w}{ }^{*}=m^{*} \mu^{*}$ equals $3.3 \%$ of private wealth and $b_{y}{ }^{*}=m^{*} \mu^{*} \beta^{*}$ equals $20 \%$ of national income.
- Around 2020, we have $A=20, H=30$ and $D=80$, so that people inherit at age $I=D-H=50$. In steady-state, $m^{*}=1 /(D-A)=1.7 \%, \mu^{*}=(D-A) / H=200 \%$. Then $b_{w}{ }^{*}=m^{*} \mu^{*}$ again equals $3.3 \%$ of private wealth and $b_{y}{ }^{*}=m^{*} \mu^{*} \beta^{*}$ again equals $20 \%$ of national income.

Although this is a very crude model, we believe that this simple result provides the right intuition as to why the historical decline in mortality rates was to a large extent compensated by an historical rise in the relative wealth of decedents. Moreover, this intuition generalizes to more general demographic structures, and most importantly to more general saving models, assuming that the growth rate g is relatively small.

First, the discontinuous age-wealth profile obtained in this model (see Figure 6) is obviously an artefact due to the deterministic demographic structure, and would immediately disappear once one introduces demographic noise (as there is in the real world), without affecting the results. E.g. assume that individuals, instead of dying with certainty at age $a=D$, die at any age on the interval [ $D-d ; D+d]$, with uniform distribution. Then individuals will inherit at any age on the interval $[I-d ; I+d]$. To fix ideas, say that $A=20$, $H=30, D=70$ and $d=10$, i.e. individuals die at any age between 60 and 80 , with uniform probability, and therefore inherit at any age between 30 and 50 , with uniform probability. Then one can show that the steady-state age-wealth profile has a simple linear shape (see Figure 7), and that the theoretical results of proposition 1 are left unchanged. ${ }^{55}$ In the real world, there are several other types of demographic noise (age at parenthood is not the same everybody, fathers and mothers usually do not die at the same time, there is

[^21]differential mortality, there are inter vivos gifts, etc.), and we take all of these into account in the full fledged simulated model. The important point, however, is that the basic intuition provided by proposition 1 is essentially unaffected by demographic noise.

Next, proposition 1 can be extended to the case where savings come both from labor and capital income ( $s_{L} \geq 0 \& s_{k} \geq 0$ ), . One can show that steady-state inheritance ratios then depend negatively on the growth rate, and converge towards class saving levels as $g \rightarrow 0$ :

Proposition 2. Assume exogenous saving rates $\mathrm{s}_{\mathrm{L}}>0$, $\mathrm{s}_{\mathrm{K}} \geq 0$. As $\mathrm{t} \rightarrow+\infty, \mu_{\mathrm{t}} \rightarrow \mu^{*}=\mu(\mathrm{g})<\boldsymbol{\varphi}$ Higher growth reduces inheritance: $\boldsymbol{\mu}^{\prime}(\mathrm{g})<0$
With low growth, inheritance ratios converge to class saving levels: $\lim _{\mathbf{g} \rightarrow \mathbf{0}} \boldsymbol{\mu}(\mathbf{g})=\boldsymbol{\rho}$

The general formula for steady-state $\mu^{*}=\mu(\mathrm{g})$ turns out to be reasonably simple:

$$
\begin{equation*}
\mu(\mathrm{g})=\frac{1-\mathrm{e}^{-\left(\mathrm{g}-\mathrm{skr} r^{*}\right)(\mathrm{D}-\mathrm{A})}}{1-\mathrm{e}^{-\left(\mathrm{g}-\mathrm{skr} r^{+}\right) \mathrm{H}}} \tag{5.4}
\end{equation*}
$$

With $s_{L}>0$, the steady-state rate of wealth reproduction $s_{K} r^{*}$ is strictly less than the growth rate $g$, and $g-s_{K} r^{*}=g(1-\alpha) s_{L} / s>0$. If $s_{L} \rightarrow 0$, then $g-s_{K} r^{*} \rightarrow 0$. Simple first order approximation using the formula $\mu(g)$ shows that steady-state $\mu^{*}$ then tends toward $\grave{\rho}=(D-A) / H .{ }^{56}$ This is just a continuity result: as we get closer to class savings, we converge toward the same age-wealth profile and inheritance ratios, whatever the growth rate might be.

The more interesting part is that for any saving behaviour ( $\mathrm{s}_{\mathrm{L}}>0, \mathrm{~s}_{\mathrm{K}} \geq 0$ ), steady-state $\mu^{*}$ also tends toward the same class-saving level $\rho$ when the growth rate $g$ tends toward 0 . In the uniform savings case ( $s_{L}=s_{K}=s$ ), $g-s_{K} r^{*}=(1-\alpha) g$, so we simply have:

$$
\begin{equation*}
\mu(g)=\frac{1-e^{-(1-\alpha) g(D-A)}}{1-e^{-(1-\alpha) g H}} \tag{5.5}
\end{equation*}
$$

First-order approximations again show that $\mu(\mathrm{g}) \rightarrow \dot{\mu}$ as $\mathrm{g} \rightarrow 0$. Steady-state inheritance ratios $b_{w}{ }^{*}$ and $b_{y}{ }^{*}$ also tend toward their class saving levels $b_{w}=1 / H$ and $b_{y}=\beta^{*} / H$ when growth rates go to zero. Conversely, the higher the growth rate g , the lower the steadystate inheritance ratios $\mu^{*}=\mu(\mathrm{g}), \mathrm{b}_{\mathrm{w}}{ }^{*}$ and $\mathrm{b}_{\mathrm{y}}{ }^{*}$.

The intuition is the following. With $s_{L}>0$, the age-wealth profile is less extreme than the class saving profile depicted on Figure 6. Young workers now accumulate positive wealth before they inherit (and accumulate positive wealth even if they never inherit). So the relative wealth of the elderly $\mu_{\mathrm{t}}$ will always be lower than under class savings. Since labor income grows at rate g , this effect will be stronger for higher growth rates. With large

[^22]growth, young workers earn a lot more than their parents. This reduces the importance of inheritance. But with low growth, the inheritance effect increasingly dominates, and the steady-state age-wealth profile looks closer and closer to the class saving profile. So inheritance flows converge towards class saving levels, irrespective of saving behavior. ${ }^{57}$

Next, and most importantly, formulas (5.6)-(5.7) can be used to quantify the magnitude of the effects at play. The point is that convergence towards class saving levels happens very fast. That is, for low but realistic growth rates (typically, $\mathrm{g}=1 \%$ or $\mathrm{g}=2 \%$ ), we find that $\mu(\mathrm{g})$ is already very close to $\rho$. That is, inheritance-wise, a growth rate of $g=1 \%$ or $g=2 \%$ is not very different from a growth rate $\mathrm{g}=0 \%$.

Example. Assume $g=1 \%$ and uniform savings ( $s=s_{K}=s_{L}$ ). Then for $A=20, H=30, D=60$, i.e. I=D-H=30, we have $\mu(g)=129 \%$. This is lower than $\rho=(D-A) / H=133 \%$ obtained under class savings, but not very much lower. With $\beta^{*}=600 \%$, this corresponds to $b_{y}{ }^{*}=19 \%$ instead of $b_{y}{ }^{*}=20 \%$ under class savings. With $A=20, H=30, D=80$, i.e. $I=D-H=50$, we get $\mu(g)=181 \%$ under uniform savings instead of $\stackrel{\rho}{\mu}=200 \%$ with class savings, and again $b_{y}{ }^{*}=19 \%$ instead of $b_{y}{ }^{*}=20 \%$. Assuming $g=2 \%$, we still get $b_{y}{ }^{*}=19 \%$ with $D=60$, and $b_{y}{ }^{*}=17 \%$ with $D=80$, instead of $b_{y}{ }^{*}=20 \%$ in both cases under class savings. ${ }^{58}$

Assume for instance that there was a major structural shift from class saving behaviour in the $19^{\text {th }}$ century to uniform savings in the $20^{\text {th }}$ century (or even to reverse class saving, where all savings come from labor income), for instance because of a structural decline in wealth concentration. This will reduce the steady-state magnitude of inheritance flows. However with growth rates around $g=1 \%-2 \%$ the effect will be quantitatively extremely modest: the annual inheritance flow will be $17 \%-19 \%$ of national income instead of $20 \%$.

In order to obtain more substantial declines in $\mu^{*}$ and $b_{y}{ }^{*}$, one needs to assume much larger growth rates. E.g. with $g=5 \%$, then one gets $b_{y}{ }^{*}=17 \%$ with $D=60$, and $b_{y}{ }^{*}=13 \%$ with $D=80$ (again for $\beta^{*}=600 \%$ ). This can contribute to explain why inheritance flows remained low during the 1950s-1970s period, when growth rates were indeed exceptionally high. ${ }^{59}$

As $g \rightarrow+\infty$, then $\mu^{*}=\mu(g) \rightarrow 1, b_{w}{ }^{*} \rightarrow 1 /(D-A)$ and $b_{y}{ }^{*} \rightarrow \beta^{*} /(D-A)$. Assume $D=80$, so that adult life length $D-A=60$ is twice as long as generation length $H=30$. Then infinite growth leads to

[^23]a doubling of the estate multiplier $e^{*}$ (from $e^{*}=30$ to $e^{*}=60$ ), and a division by two of the inheritance flow $b_{y}{ }^{*}$ (from $b_{y}{ }^{*}=20 \%$ to $b_{y}{ }^{*}=10 \%$, for given $\beta^{*}=600 \%$ ). In case life expectancy rises to $D=110$, then the inheritance flow is divided by three. With infinite growth, $b_{w}{ }^{*} \rightarrow 0$ and $b_{y}{ }^{*} \rightarrow 0$ as $D \rightarrow+\infty$. That is, societies where people die later and later resemble societies where one never dies, and inheritance effectively vanishes. The key point, however, is that this naive intuition only applies to the case with infinite growth. With plausible growth rates, then the inheritance flow $b_{y}{ }^{*}$ depends almost exclusively on generation length $H$, and is little affected by the rise of life expectancy $D$.

These results can also be extended to the open economy case. One simply needs to replace $r^{*}$ by the world rate of return $r$ in the steady-state formula (5.4):

Proposition 3. Assume exogenous saving rates $s_{L} \geq 0, s_{K} \geq 0$, and a world rate of return $r \geq 0$. As $t \rightarrow+\infty, \mu_{\mathrm{t}} \rightarrow \mu^{*}=\mu(\mathrm{g}, \mathrm{r})$. If $\mathrm{r}>\dot{\mathscr{O}}=\mathrm{g} / \mathrm{s}_{\mathrm{K}}$, then $\mu(\mathrm{g}, \mathrm{r})=\hat{\boldsymbol{\rho}}$. If $\mathrm{r}<\dot{\mathscr{O}}$, then $\mu(\mathrm{g}, \mathrm{r})<\hat{\boldsymbol{\varphi}}$.
Lower growth and/or higher rates of return raise inheritance: $\boldsymbol{\mu}^{\prime}(\mathbf{g})<0, \mu^{\prime}(r)>0$.
With low growth and/or high rates of return, inheritance ratios converge to class saving levels: $\lim _{\mathrm{g} \rightarrow 0} \mu(\mathbf{g}, \mathbf{r})=\lim _{\mathrm{r} \rightarrow \boldsymbol{\oplus}} \mu(\mathbf{g}, \mathbf{r})=\boldsymbol{\rho}$

The open economy case is useful to understand the wealth accumulation patterns prevailing in France (and other European countries such as the U.K.) in the $19^{\text {th }}$ century and early $20^{\text {th }}$ century. The French $\beta_{\mathrm{t}}$ rose from $550 \%-600 \%$ in 1820 to $650 \%-700 \%$ in 1900-1910, and most of the rise came from the accumulation of foreign assets. The case $r>\grave{O}$ is particularly likely to prevail in environments with low growth and high wealth concentration (so that wealth holders can afford re-investing a large fraction $\mathrm{s}_{\mathrm{K}}$ of their asset returns). E.g. with $g=1 \%$ and $s_{K}=25 \%$, the world rate of return $r$ simply needs to be larger than $\grave{\oplus}=g / s_{k}=4 \%$. So if $r=5 \%$, then $s_{k} r=1.25 \%$, i.e. private wealth grows $25 \%$ faster than domestic output, which over a few decades makes a big difference. What we add to these well-know open economy insights is the inheritance dimension. In case $r>$ © then $\mu_{t}$ always converges towards its maximum class-saving level $\dot{\mu}$, whatever the growth rate g and the labor saving rate $\mathrm{s}_{\mathrm{L}}$. Intuitively, labor income as a whole matters less and less along such explosive paths, and the age-wealth profile becomes almost exclusively determined by inheritance receipts.

In case $r<\grave{0}$, then steady-state foreign assets (positive or negative) are a constant fraction of domestic output and assets, and $\mu^{*}=\mu(\mathrm{g}, \mathrm{r})<\dot{\rho}$. The intuition for $\mu^{\prime}(\mathrm{g})<0$ is the same as before: higher growth raises the relative wealth of the young and reduces the relative wealth of elderly (and therefore the relative importance of inheritance). The intuition for $\mu^{\prime}(r)>0$ is the opposite: a higher rate of return gives more weight to past inheritance and raises the relative wealth of the elderly. In the same way as in the closed economy case, the important point about this formula is that it converges very fast to class saving levels
as $g \rightarrow 0$ and/or as $r \rightarrow$ © . The formula $\mu(g, r)$ also shows that the $g$ effect is quantitatively larger than the $r$ effect, because the $r$ effect is multiplied by $s_{K}<1$. That is, the absolute growth rate g matters, and not only the differential $\mathrm{r}-\mathrm{g}$. For given $\mathrm{r}-\mathrm{g}$, the steady-state $\mu^{*}=\mu(\mathrm{g}, \mathrm{r})$ and the corresponding $\mathrm{b}_{\mathrm{y}}{ }^{*}$ will be lower for higher g .

Example. Assume $r-g=3 \%, D=80, s_{K}=20 \%$. If $g=1 \%$ and $r=4 \%$, then we obtain $\mu^{*}=\mu(\mathrm{g}, \mathrm{r})=194 \%$ and $\mathrm{b}_{y}{ }^{*}=19 \%$ (i.e. almost as much as the class saving levels $\grave{\mu}=200 \%$ and $\left.b_{y}{ }^{*}=20 \%\right)$. But if $g=5 \%$ and $r=8 \%$, then we get $\mu^{*}=\mu(\mathrm{g}, \mathrm{r})=136 \%$ and $\mathrm{b}_{\mathrm{y}}{ }^{*}=14 \% .{ }^{60}$

Finally, one can show that these results can be extended to standard endogenous saving models. ${ }^{61}$ Consider first an infinite horizon model. Dynasties maximize $U=\int_{t \geq s} e^{-\theta t} u\left(c_{t}\right) d t$, where $\theta$ is the rate of time preference and $u(c)=c^{1-\sigma} /(1-\sigma)$ with constant intertemporal elasticity of substitution (IES) equal to $1 / \sigma$. The steady-state rate of return $r^{*}$ and wealthincome ratio $\beta^{*}$ are given by the Ramsey-Cass golden rule of capital accumulation:

$$
r^{*}=\theta+\sigma g \quad \text { and } \quad \beta^{*}=\alpha / r^{*}(5.6)
$$

The special case $g=0$ implies $r^{*}=\theta$. More generally, for $g \geq 0$, the steady-state rate of return $r^{*}$ is always larger than the growth rate $g$ in the dynastic model. ${ }^{62}$ In the same way as in the exogenous saving model, $\mathrm{r}^{*}$ is also an increasing function of $\mathrm{g} .{ }^{63}$

Example: If $\theta=1 \%, \sigma=2, g=2 \%$, then $r^{*}=5 \%$. If $\alpha=30 \%$, then $\beta^{*}=600 \%$.

In effect, utility-maximizing dynasties in this model behave exactly in the same way as in the exogenous class saving model. In order to ensure that their consumption path grows at rate g , they save a fraction $\mathrm{s}_{\mathrm{K}}=\mathrm{g} / \mathrm{r}^{*}$ of their asset returns (and consume a fraction $1-\mathrm{g} / \mathrm{r}^{*}$ ) and a fraction $s_{L}=0$ of their labor income. ${ }^{64}$ It follows that the steady-state age-wealth profile $w_{t}(a)$ is the same as before (see Figures 6-7), and that $\mu_{t} \rightarrow \rho=(D-A) / H$ as $t \rightarrow+\infty$. So we again have the same steady-state formulas for inheritance flows $\left(b_{w}=1 / H, b_{y}=\beta / H\right) .{ }^{65}$

[^24]Consider now a finite-horizon, wealth-in-the-utilty model. Each agent $i$ is assumed to maximize $\mathrm{V}(\mathrm{U}, \mathrm{w})=\left(1-\mathrm{s}_{\mathrm{B}}\right) \log (\mathrm{U})+\mathrm{s}_{\mathrm{B}} \log (\mathrm{w})$, where $\mathrm{U}=\mathrm{U}_{\mathrm{c}}$ is the utility derived from lifetime consumption flow, $w=w(D)$ is wealth at death, and $s_{B}$ is the share of lifetime resources devoted to end-of-life wealth. One standard interpretation is that agents care directly about the bequest $b=w(D)$ which they leave to the next generation. In the presence of uninsurable lifetime shocks (income, health, time of death), people might also like the security that goes with wealth. So this utility function can be interpreted as a reduced form for precautionary savings. ${ }^{66}$ People might also derive direct utility from the prestige, power and social status conferred by wealth. ${ }^{67}$ Presumably the exact combination of these saving motives varies a lot across individuals, just like other tastes. ${ }^{68}$ Whatever the interpretation, we have a very simple formula for the steady-state inheritance flow $b_{y}{ }^{*}$ :

$$
\begin{equation*}
\mathrm{b}_{\mathrm{y}}^{*}=\mathrm{b}_{\mathrm{y}}(\mathrm{~g}, \mathrm{r})=\frac{\mathrm{s}_{\mathrm{B}} \lambda(1-\alpha) \mathrm{e}^{(\mathrm{r}-\mathrm{g}) \mathrm{H}}}{1-\mathrm{s}_{\mathrm{B}} \mathrm{e}^{(r-\mathrm{g}) \mathrm{H}}} \tag{5.7}
\end{equation*}
$$

This formula follows directly from the fact that agents devote a fraction $\mathrm{s}_{\mathrm{B}}$ of their capitalized, end-of-life lifetime resources (labor income and inherited wealth) to their end-of-life wealth. ${ }^{69}$ It holds both in the closed and open economy cases, and for any structure of intra-cohort labor income or preference shocks. The intuition as to why the inheritanceincome ratio $b_{y}{ }^{*}$ is a rising function of $r-g$ is straightforward. The excess of the rate of return over the growth rate exactly measures the extent to which wealth coming from the past is being capitalized at a faster pace than the growth rate of current income. Moreover, numerical solutions again show that for plausible parameter values and low growth $b_{y}{ }^{*}$ is close to $\beta^{*} / \mathrm{H}$, in the same way as in the exogenous saving and dynastic models. ${ }^{70}$

Example. Assume $\mathrm{A}=20, \mathrm{H}=30, \mathrm{D}=80, \mathrm{~s}_{\mathrm{B}}=10 \%$, and $\mathrm{g}=1 \%$. Then in the closed-economy case we get $r^{*}=4 \%$ and $b_{y}{ }^{*}=22 \%$. If life expectancy was instead $D=60$, we would get instead $b_{y}{ }^{*}=21 \%$. I.e. inheritance ratios are almost exclusively determined by generation length H, and depend very little on life expectancy. With $g=2 \%$, we get $r^{*}=5 \%$ and $b_{y}{ }^{*}=18 \%$ (both for $D=60$ and $D=80$ ). One needs to assume much larger growth rates to obtain more significant declines. In the open-economy case, inheritance can reach higher levels. E.g. with $D=80, s_{B}=10 \%, g=1 \%$ and $r=5 \%$, then $b_{y}{ }^{*}=30 \%$.

[^25]
## 6. Simulations

We now come to the full fledged simulations. Our simulated model is conceptually simple. We start from observed demographic data. We also take as given observed nationalaccounts aggregate values for all macroeconomic variables (growth rates, factor shares, tax rates, rates of return, saving rates). We then make different assumptions about saving behaviour in order to see whether we can replicate observed age-wealth profiles, $\mu_{\mathrm{t}}$ ratios and the resulting inheritance flows.

More precisely, we constructed an exhaustive, annual demographic data base on the age structure of the living population and of decedents, heirs, donors and donees in France over the 1820-2008 period. In practice, bequest and gift flows accrue to individuals in several different payments during their lifetime: usually both parents do not die in the same year, sometime individuals receive gifts from their parents, and sometime they receive bequests and gifts from individuals other than their parents. We use the estate tax returns micro-files available since the 1970s (and the historical tabulations broken by decedent and donor age group available for the earlier period), as well as historical demographic data on age at parenthood, in order to compute the exact fraction of bequest and gift flow accruing to each cohort and transmitted by each cohort during each year of the 1820-2008 period. In the simulated model, the value of bequests is endogenous: it depends on the wealth at death of the relevant cohorts, as determined by the endogenous dynamics of the age-wealth profile. But the fraction of the aggregate bequest flow going to each cohort is taken from observed data. Regarding gifts, in some variants we take the observed giftbequet ratio $v_{t}$ as given, and in some other variants we assume other gift-bequest ratios (so as to check whether long run patterns are affected by $v_{t}$ ). In all variants, the age structure of donors and donees is exogenously given by our demographic data base.

Regarding the economic side of the model, we proceed as follows. We start from observed factor shares in national income, as measured by national accounts: $Y_{t}=Y_{K t}+Y_{L t}$. We use national accounts tax and transfer series to compute aggregate, net-of-tax labor and pension income $\left(1-T_{L t}\right) Y_{L t}$ (where $\mathrm{T}_{\mathrm{Lt}}$ is the aggregate labor tax rate, excluding pension payroll taxes). We use income tax data to estimate the age-labor income profile (including pension income) $Y_{\text {Lt }}(a)$ throughout the period, which we take as given. On this basis we attribute an average net-of-tax labor and pension income $y_{\text {Lt }}(a)$ to each cohort for each year of the 1820-2008 period. Because we use liner saving models, we do not attempt to model intra-cohort inequality labor income or wealth.

We also take as given the average pre-tax rate of return $r_{t}$, which we compute by dividing capital income $Y_{\mathrm{Kt}}$ by aggregate private wealth $\mathrm{W}_{\mathrm{t}}$, and the average after-tax rate of return $r_{d t}=\left(1-T_{K t}\right) r_{t}$ (where $T_{K t}$ is the aggregate capital tax rate). We assume that wealth holders
from all age groups get the same average after-tax rate of return $r_{d t}$ on their wealth $W_{t}(a)$. This is very much a simplifying assumption. In the real world, rates of return vary widely across assets: typically, returns on stock and real estate are much larger than returns on bonds. ${ }^{71}$ This might possibly entail systematic differences across age groups. ${ }^{72}$ However we know very little on such systematic variations, so as a first approximation attributing the same average return to all age groups seems like the most reasonable assumption.

Our national-accounts approach to average rates of return $r_{t}$ and $r_{d t}$ also appears to be the most appropriate option. To the extent that national accounts correctly measure annual flows of capital income $Y_{K t}$ (rental income, interest, dividend, etc.), then $r_{t}$ and $r_{d t}$ indeed measure the true average rate of return received by holders of private wealth $W_{t}$ in France over the past two centuries. National accounts are not perfect. But this is arguably the most comprehensive data source we have, and one ought to start from there.

We present two main series of simulations: one for the 1820-1913 quasi-steady-state period, and one for the 1900-2008 U-shaped period (which was then extended to the future). In the first one, we start from the observed age-wealth profile in 1820, and attempt to simulate the evolution of the profile during the 1820-1913 period. In the second one, we start from the observed age-wealth profile in 1900, and attempt to simulate the evolution of the age-wealth profile during the 1900-2008 period. In both cases, the cohort level transition equation for wealth is the following: ${ }^{73}$

$$
\begin{equation*}
W_{t+1}(a+1)=\left(1+q_{t+1}\right)\left[W_{t}(a)+s_{L t} Y_{L t}(a)+s_{K t} r_{d t} W_{t}(a)\right] \tag{6.1}
\end{equation*}
$$

( + bequests and gifts received - bequests and gifts transmitted)

The real rates of capital gains $q_{t}$ come from our aggregate wealth accumulation equation. ${ }^{74}$ The only parameters on which we need to make assumptions are the labor-income and capital-income savings rates $s_{L t}$ and $s_{k t}$. We make various assumptions on these and analyze the extent to which we replicate observed age-wealth profiles, $\mu_{\mathrm{t}}$ ratios and resulting inheritance flows. In all simulations we make sure that the aggregate savings $s_{t}=\left(1-\alpha_{t}\right) s_{L t}+\alpha_{t} s_{k t}$ (where $\alpha_{t}$ is the observed, after-tax capital share) is equal to the observed private savings rate $s_{\mathrm{t}}$, which according to national accounts data has been relatively stable around $8 \%-10 \%$ in France in the long run (see Figure 8).

[^26]By construction, the simulated model always perfectly reproduces the aggregate wealthincome ratio $\beta_{t}=W_{t} / Y_{t}$. The name of the game is the following: what assumptions on saving behaviour also allow us to reproduce the observed dynamics of age-wealth profiles, the $\mu_{\mathrm{t}}$ ratio and the inheritance flow-national income ratio byt?

Our main conclusion is summarized on Figure 9. By making simple assumptions on savings behaviour (namely, class saving for the 1820-1913 period, and uniform saving for the 1913-2008 period), we are able to reproduce remarkably well the observed evolution of the aggregate inheritance flow over almost two centuries. If we then use the model to predict the future, we find that the inheritance flow should stabilize or keep rising, depending on the future evolutions of growth rates and after-tax rates of return.

### 6.1. Simulating the 1820-1913 quasi-steady-state

The most interesting period to simulate and investigate is maybe the 1820-1913 period. As was already stressed, this is because this time period looks very close to the theoretical steady-state associated to the class saving model, with $\mathrm{s}_{\mathrm{K}}$ close to $\mathrm{g} / \mathrm{r}$, and $\mathrm{s}_{\mathrm{L}}$ close to 0 .

The first thing to notice is that the 1820-1913 period was a time when the rate of return to private wealth $r$ was much bigger than the growth rate g . Generally speaking, factor shares appear to have been relatively stable in France over the past two centuries, with a capital share generally around $30 \%$ (see Figure 10). Note however that according to the best available data, the capital share during the $19^{\text {th }}$ century was somewhat higher than during the $20^{\text {th }}$ century ( $30 \%-40 \%$, vs $20 \%-30 \%$ ). Dividing capital shares by aggregate wealthincome ratios, we get average rates of returns to private wealth $r_{t}$ of about $5 \%-6 \%$ in 18201913, much larger than the growth rate, which on average was only $1.0 \%$ (see Figure 11).

We run several simulations. If we assume uniform saving rates, then we under-predict somewhat the aggregate evolution of inheritance. Most importantly, we predict an agewealth profile in 1900-1910 that is flat after age 60 (or even slightly declining after age 70), while the observed profile is steeply increasing, including for the very old. This has a limited impact on the aggregate $\mu_{\mathrm{t}}$ and byt ratios, because at that time few people died after age 70. But this is an important part of the observed data. This shows that uniform saving is an inadequate description of actual savings behaviour at that time. If we assume that all savings came from capital income, which implies $\mathrm{s}_{\mathrm{K}} \approx 25 \%-30 \%$ and $\mathrm{s}_{\mathrm{L}} \approx 0 \%$ (instead of $\left.\mathrm{s}_{\mathrm{K}}=\mathrm{s}_{\mathrm{L}} \approx 8 \%-10 \%\right)$, then we can predict adequately both the evolution of the inheritanceincome ratio $b_{y t}$ and the evolution of the age-wealth profiles $w_{t}(a)$.

Given the very large wealth concentration prevailing at that time, class saving behavior seems highly plausible. The income levels and living standards attained by wealth holders
were so much higher than those of the rest of the population that is was not too difficult for them to save $25 \%-30 \%$ of their capital income annually. In order to fully account for the steepness of the age-wealth profile around 1900-1910, one would actually need to assume not only that (most) savings come from capital income, but also that the average saving rate $s_{k}(a)$ actually rises with age. This could be explained by a simple consumption satiation effect among elderly wealth holders. To properly study this issue, one would need however to explicitly introduce distributional issues and to use micro data.

We also did various sensitivity checks by varying the gift-bequest ratio $\mathrm{v}_{\mathrm{t}}$. In particular, in one variant, we set $\mathrm{v}_{\mathrm{t}}=0 \%$ for the entire 1820-1913 period, i.e. $19^{\text {th }}$ century wealth holders were assumed to make no inter vivos gifts and to hold on their wealth until the die. Of course, this leads us to under-predict the observed inheritance (bequests plus gifts) flow at the beginning of the period. The interesting finding, however, is that we get approximately the same inheritance-income ratio at the end of the period (about 20\%) than the observed ratio with gifts (but with an even more steeply increasing age-wealth profile). This validates our methodological choice of adding gifts to bequests. The existence of inter-vivos gifts has an impact on the timing of inheritance receipts, but very little impact on the long run aggregate flow of aggregate wealth transmission.

### 6.2. Simulating the $\mathbf{2 0}^{\text {th }}$ century chaotic U-shaped pattern

We proceed in the same way for the $20^{\text {th }}$ century. Whether we assume uniform savings or class savings, the model predicts a decline in the $\mu_{\mathrm{t}}$ ratio during the 1913-1949 period. The channel through which this effect operates is the one that we already described, i.e. it was too late for the elderly to start re-accumulating wealth again after the shocks. However we get a significantly better fit by assuming that aggregate savings behaviour has shifted from class savings to uniform savings during the 1913-1949 period. For instance, if we look at the inheritance-income ratio at its lowest point, i.e. during the 1950s (4.3\%), we predict $5.3 \%$ with uniform saving and $6.0 \%$ with class saving.

Intuitively, this structural change in saving behaviour could come from the large decline in wealth concentration that occurred during that time: top wealth holders were much less prosperous than they used to be, and they were not able to save as much. It could even be that they saved even less than labor earners, for instance if they tried to maintain their living standards for too long. The other possible interpretation as to why we slightly over predict the observed 1950s inheritance flow (even with uniform saving) is because the capital shocks of the 1913-1949 disproportionally hit elderly wealth holders, e.g. because they held a larger fraction of their wealth in bonds and other nominal assets. In the simulated model, we assume that the shocks (both the destruction shocks and the capital losses) hit all wealth holders in a proportional manner. Finally, it is possible that the
gradual rise in age expectancy that occurred during this period led to a rise in lifecycle savings out of labor income. The data we use in this paper is insufficient to settle this issue. Our aggregate approach allows us to adequately reproduce the general pattern over a two century period. But in order to better understand the micro processes at work, one would clearly need to model explicitly distributional issues and to use micro data.

The post 1949 simulations confirm the view that a structural shift from class saving to uniform saving occurred during the $20^{\text {th }}$ century. All saving models predict a strong recovery of $\mu_{\mathrm{t}}$ and $\mathrm{b}_{\mathrm{yt}}$ between the 1950s and the 2000s (especially since the 1970s, due to lower growth rates, see below). But class saving would lead us to over predict the recovery, with an inheritance flow of $16.8 \%$ in 2010 , vs $14.4 \%$ with uniform savings, vs $13.8 \%$ with reverse class savings (i.e. zero saving from capital income), vs $14.5 \%$ in the observed data. We interpret this as evidence in favour of the uniform saving assumption as an adequate way to describe postwar aggregate savings behaviour (as a first approximation). This interpretation seems to be consistent with micro evidence from French household budget surveys: aggregate age-saving rates profiles have been quasiflat during the 1978-2006 period, and do not appear to vary systematically with factor income composition. ${ }^{75}$ This is imperfect data, however, and this issue would need to be better addressed in future research, by introducing explicitly distributional effects.

The simulations as a whole also confirm the critical importance of the $\mathrm{r}>\mathrm{g}$ logic. Also, as predicted by the theoretical formulas, the absolute level of $g$ appears to have a stronger quantitative impact than the differential r-g. This is exemplified by the 1949-1979 period. Growth rates were above $5 \%$, which slowed down considerably the rise of the $\mu_{\mathrm{t}}$ ratio. During the 1979-2009 period, growth slowed down to $1 \%-2 \%$, the rise of the $\mu_{\mathrm{t}}$ ratio was more rapid, and so was the recovery of the inheritance-income ratio byt. This simple growth effect plays a much bigger role than saving behaviour, as predicted by the theory.

Finally, capital taxes play an important role in our simulations. The average rate of return on private wealth $r_{t}=\alpha_{t} / \beta_{t}$ has always been much larger than the growth rate $g_{t}$ in France, both during the $19^{\text {th }}$ and the $20^{\text {th }}$ centuries (see Table 3). The major change is that the effective capital tax rate $T_{K t}$ was less than $10 \%$ prior to World War 1, then rose to about $20 \%$ in the interwar period, and finally grew to $30 \%-40 \%$ in the postwar period. ${ }^{76}$ This had

[^27]a large impact on the differential between $r_{d t}=\left(1-T_{K t}\right) r_{t}$ and $g_{t}$. In particular, capital taxes largely explain why the differential was relatively small (but still positive) during the 19491979 period, in spite of positive capital gains. In our simulations, this differential has a smaller impact on $\mu_{t}$ and $b_{y t}$ than the absolute growth rate level, but the effect is still significant. We further investigate this issue with $21^{\text {st }}$ century simulations.

### 6.3. Simulating the $21^{\text {st }}$ century: towards a new steady-state?

In our baseline scenario, we assume that growth rates in 2010-2100 will be the same as the 1979-2009 average (1.7\%), that the aggregate saving rate will be the same as the 1979-2009 average ( $9.4 \%$ ), and that the capital share will be the same as the 2008 value $(26 \%) .{ }^{77}$ On the basis of the historical evolutions described in section 3.2 above, we assume that asset prices remain the same (relatively to consumer prices) after 2010.

In this scenario, we predict that the inheritance-income ratio $b_{y t}$ will keep increasing somewhat after 2010, but will soon stabilize at about $16 \%$ (see Figure 9). There are several reasons why this new steady-state level is substantially below the $20 \%-25 \%$ quasi-steady-state level prevailing in 1820-1913. First, our projected growth rate (1.7\%) is small, but bigger than the $19^{\text {th }}$ century growth rate (1.0\%). Next, our projected after-tax rate of return $(3.0 \%)$ is substantially smaller than the $19^{\text {th }}$ century level ( $5.3 \%$ ).

We then consider an alternative scenario with a growth slowdown after 2010 (1.0\%), and a rise of the after-tax rate of return to $5.0 \%$. This could be due either to a large rise in the capital share (say, because of increased international competition to attract capital), or to a complete elimination of capital taxes (which could also be triggered by international competition), or to a combination of the two. Under these assumptions, the inheritanceincome ratio converges towards a new steady-state around $22 \%-23 \%$ by $2050-2060$, i.e. approximately the same level as that prevailing in the early $20^{\text {th }}$ century (see Figure 9).

This finding confirms that the rise in life expectancy has little effect on the long run level of inheritance. With low growth and high returns, the inheritance-income ratio depends almost exclusively on generation length H. Detailed results also show that the largest part of the effect (about two thirds) comes from the growth slowdown, versus about one third for the rise in the net-of-tax rate of return. This decomposition is relatively sensitive to assumptions about savings behaviour, however.

We also explored various alternative scenarios. With a 5\% growth rate after 2010, and a rise in saving rate to $25 \%$, so as to preserve a plausible aggregate wealth income ratio,

[^28]inheritance flows converge towards about 12\% of national income by 2050-2060. With no rise in savings, inheritance flows converge to about $5 \%-6 \%$ of national income (i.e. approximately the same level as in the 1950s-1960s). But this is largely due to the fall in the aggregate wealth-income ratio. Another equivalent scenario would involve large scale capital shocks similar to the 1913-1949 period, with capital destructions, and/or a prolonged fall in asset prices, due to rent control, nationalization, high capital taxes or other anti-capital policies. Given the chaotic $20^{\text {th }}$ century record, one certainly cannot exclude such a radical scenario. The bottom line, however, is that a return to the exceptionally low inheritance flows of the 1950s-1960s can occur only under fairly extreme assumptions. One needs a combination of exceptionally high growth rates during several decades and a large fall in aggregate wealth-income ratio.

Finally, we made simulations assuming that the gift-bequest ratio $v_{t}$ did not rise after 1980. This is an important sensitivity check, because the large rise in gifts in recent decades played an important role in the overall analysis. We find a predicted inheritance-income ratio of $15 \%$ by 2050 , instead of $16 \%$ in the baseline scenario. This suggests that the current gift levels are almost fully sustainable. We also simulated the entire 1900-2100 period assuming there was no gift at all. In the same way as for the 1820-1913 period, this has little effect on long run patterns, which again validates the way we treated gifts.

## 7. Applications \& directions for future research

### 7.1. The share of inheritance in total lifetime resources by cohort

In this paper, we mostly focused on the cross-sectional inheritance flow-national income ratio $b_{y t}=B_{t} / Y_{t}$. However this ratio is closely related to another ratio: namely the share of inheritance in the lifetime resources of the currently inheriting cohort, which we note $\hat{\alpha}_{t}$.

To see why, consider again the deterministic, stationary demographic structure introduced in section 5. Everybody becomes adult at age A, has one kid at age H , inherits at age I=D-H, and dies at age D. Each cohort size is normalized to 1, so that total (adult) population $N_{t}$ is equal to (adult) life length $D-A$. Per decedent inheritance $b_{t}=B_{t}=b_{y t} Y_{t}$ and per adult income $y_{t}=Y_{t} /(D-A)$. At time $t$, the cohort receiving average inheritance $b_{t}$ is the cohort born at time $x=t-I$. We note $\tilde{y}_{t}=b_{t} e^{r H}+\tilde{y}_{L t}$ the total lifetime resources received by cohort x , where $\mathrm{b}_{\mathrm{t}} \mathrm{e}^{\mathrm{rH}}$ is the end-of-life capitalized value of their inheritance resources, and $\tilde{y}_{\mathrm{Lt}}$ is the end-of-life capitalized value of their labor income resources. We define $\hat{\alpha}_{t}=b_{t} e^{r H} / \tilde{y}_{t}$ the share of inheritance in total lifetime resources of this cohort. Assuming flat age-labor income profile $y_{L t}(a)=y_{L t}$ (i.e. full replacement rate $\rho=1$ ), we have:

$$
\tilde{y}_{L t}=\int_{A \leq a \leq D} e^{r(D-a)} y_{L}{ }^{x}(a) d a=\int_{A \leq a \leq D} e^{r(D-a)} y_{L t} e^{g(a-l)} d a
$$

I.e. $\tilde{y}_{L t}=\lambda(D-A) y_{L t} e^{r H}=\lambda Y_{L t} e^{r H}=\lambda(1-\alpha) Y_{t} e^{r H}$

$$
\begin{equation*}
\text { With: } \quad \lambda=\frac{e^{(r-g)(1-A)}-e^{-(r-g)(D-1)}}{(r-g)(D-A)} \tag{7.1}
\end{equation*}
$$

We therefore have a simple formula for $\hat{\alpha}_{t}$ as a function of $b_{y t}$ :

Proposition 4. Define $\hat{\alpha}_{t}$ the share of inheritance in the total lifetime resources of the cohort inheriting at time $t$. Then we have: $\hat{a}_{t}=\frac{b_{y t}}{b_{y t}+\lambda(1-\alpha)}$

With: $b_{y t}=$ inheritance flow-national income ratio
$1-\alpha=$ labor share in national income
$\lambda=$ correcting factor given by equation (7.1)

The inheritance share $\hat{\alpha}_{t}$ can be viewed as an indicator of the functional distribution of resources accruing to individuals. During their lifetime, individuals from cohort $x$ receive on average a fraction $\hat{\alpha}_{t}$ of their resources through inheritance, and a fraction 1- $\hat{\alpha}_{t}$ through their labor income. $\hat{\alpha}_{t}$ is simply related to the standard cross-sectional capital share $\alpha$. If $\lambda \approx 1$, which as we see below is typically the case, then $\hat{\alpha}_{t}>\alpha$ iff $b_{y t}>\alpha$. That is, the share of inheritance in lifetime resources is larger than the capital share in national income if and only if the inheritance flow is larger than the capital share. In general, both cases can happen: there are societies where the capital share is large but the inheritance share is low (say, because most wealth comes from lifecycle accumulation), and conversely there are societies where the inheritance is large but where the capital share is low (say, because capital serves mostly as storage of value and produces little flow returns).

It is interesting to see that in practice the inheritance share $\hat{\alpha}$ and the capital share $\alpha$ happen to have the same order of magnitude (typically around $20 \%-30 \%$ ) - mostly by coincidence, as far as we can see. Proposition 10 is pure accounting, and it holds for any saving model, both in and out of steady-state (one simply needs to use time-varying $g_{t}$ and $r_{t}$ to compute $\lambda$ ). If we now apply Proposition 10 to the steady-state models analyzed in section 5 , then we just need to replace $b_{y t}$ by the relevant steady-state value $b_{y}$. So for instance in the class saving model or in the dynastic model, we have $b_{y}=\beta / H$, so that:

$$
\begin{equation*}
\hat{\alpha}=\frac{b_{y}}{b_{y}+\lambda(1-\alpha)}=\frac{\beta}{\beta+\lambda(1-\alpha) H} \tag{7.3}
\end{equation*}
$$

Example. With benchmark values $\beta=600 \%, H=30, \alpha=30 \%, \lambda=1$, we have $b_{y}=20 \%$, and $\hat{\alpha}=b_{y} /\left(b_{y}+1-\alpha\right)=22 \%$. That is, in steady-state each cohort derives $\hat{\alpha}=22 \%$ of its lifetime resources through inheritance, and $1-\hat{\alpha}=78 \%$ through labor. To put it differently, inheritance resources represents $\gamma=b_{y} /(1-\alpha)=29 \%$ of their labor resources.

We now come to the correcting factor $\lambda$. Intuitively, $\lambda$ corrects for differences between the lifetime profile of labor income flows and the lifetime profile of inheritance flows. That is, $\lambda$ measures the relative capitalized value of $1 €$ in labor resources vs $1 €$ in inheritance resources, given the differences in lifetime profile between both flows of resources.

In the stylized model with deterministic demographic structure, all inheritance flows come at age $a=l$, while labor income flows come from age $a=A$ until age $a=D$. The flows received before age $a=1$ are smaller in size but needs to be capitalized; the flows received after age $a=1$ are larger in size but needs to be discounted. In case r-g=0\%, then the growth and capitalization effects cancel each other, so $\lambda$ is exactly equal to $100 \%$. Simple first order approximations using the $\lambda$ formula (equation (7.1) above) also show that if inheritance happens around mid-life (say, $A=20, H=30, D=80, I=D-H=50$ ), then $\lambda$ will tend to be close to $100 \%$ even if $r-g>0 .{ }^{78}$ When inheritance happens early in adult life (say, $A=20, H=30$, $D=80, I=D-H=30$ ), then $\lambda$ is below $100 \%$. Flows of resources accruing earlier in life are worth more from a lifetime, capitalized value perspective. Since inheritance flows were received relatively earlier in life one century ago, this effect implies that - other things equal - the relative importance of labour income should have increased over time.

Example. Assume $r-g=3 \%$ (say, $g=2 \%, r=5 \%$ ). With $A=20, H=30, D=80$, then $\lambda=114 \%$. With $A=20, H=30, D=60$, then $\lambda=79 \% .^{79}$

In practice, however, there are several other counteracting effects. In the real world, individuals receive bequests and inter vivos gifts at different point in their life (and not only at age $\mathrm{a}=\mathrm{I}$ ), and the gift-bequest ratio has risen over time. Also the cross-sectional agelabor income profile is not flat: young and old individuals receive smaller average labor income and middle age individuals.

So we use our simulated model, based upon observed and simulated data on the complete age profiles of bequest, gift and labor income receipts, in order to compute the correcting factor $\lambda^{x}$ for all cohorts born in France between $x=1800$ and $x=2030$. We find that $\lambda^{x}$ has been remarkably constant around $90 \%-110 \%$ over two centuries, with no long run trend. Since we observe bequest and gift flows until 2008, the latest cohorts for which we have complete (or near complete) observed data are those born in 1950s-1960s, for whom the $\lambda^{x}$ factor is about $100 \%-110 \%$. For cohorts born in the 1970 s and later, our computations increasingly rely on our simulations on future inheritance flows, i.e. on our assumptions about 2010-2100 growth rates and rates of return. Under the benchmark scenario ( $g=1.7 \%$, $\left(1-\mathrm{T}_{\mathrm{K}}\right) \mathrm{r}=3.0 \%$ ), we find that $\lambda^{\mathrm{x}}$ will be stable around $100 \%-110 \%$ for

[^29]cohorts 1970-2030. Under the growth slowdown-rising wealth returns scenario ( $\mathrm{g}=1.0 \%$, $\left(1-\mathrm{T}_{\mathrm{K}}\right) \mathrm{r}=5.0 \%$ ), we find that $\lambda^{x}$ will be rising to about $110 \%-120 \%$ for cohorts 1970-2030. ${ }^{80}$

We also use our simulated model in order to compute the capitalized value of lifetime resources $\tilde{y}^{x}=\tilde{b}^{x}+\tilde{y}_{L}^{x}$ for all French cohorts born between $x=1800$ and $x=2030$. Unsurprisingly, we find that the inheritance share in lifetime resources $\hat{\alpha}^{x}=\tilde{b}^{x} / \tilde{y}^{x}$ has been following a marked U-shaped pattern: $\hat{\alpha}^{\mathrm{x}}$ was about $20 \%-25 \%$ for $19^{\text {th }}$ century cohorts, fell to less than $10 \%$ for cohorts born in the 1900 s-1930s, then gradually rose to $15 \%-20 \%$ for cohorts born in the 1950s-1960s, and is expected to stabilitize around $20 \%-25 \%$ for cohorts 1970-2030 (benchmark scenario). If we instead plot the ratio $\gamma^{x}=\tilde{b}^{x} / \tilde{y}_{L}{ }^{x}$ between average inheritance resources and average labor resources $\left(\gamma^{x}=\hat{\alpha}^{x} /\left(1-\hat{\alpha}^{x}\right)\right)$, then all levels are simply shifted upwards. I.e. $19^{\text {th }}$ century cohorts received in inheritance the equivalent of about $30 \%$ of their lifetime labor income; this figure declined to about $12 \%$ for cohorts 1900-1930, and is projected to be about $30 \%$ for cohorts 1970-2030 (see Figure 13).

Here it might be useful to give some orders of magnitude. Consider the cohorts born in the 1960s, who have already received a large fraction of their gifts and bequests in the 1990s2000s. We find that their average lifetime resources, capitalized at age 50 (in the 2010s), are about 1.78 millions $€$, out of which about $320,000 €$ come from inheritance, and about 1.46 millions $€$ come from labor income. ${ }^{81}$ So we have: $\hat{\alpha}^{x}=18 \%$ and $\gamma^{x}=22 \%$. Given that $\lambda$ is close to 1 , these average labor income resources roughly correspond to the product of average per adult labor income (currently about $25,000 €$ in France) by average adult life length (about 60 years). With the cohorts born in the 1970s, we find 2.02 millions $€$, $440,000 €$ and 1.58 millions $€$. So $\hat{\alpha}^{x}=22 \%$ and $\gamma^{x}=28 \%$. On Figure 13 we therefore plot $\gamma^{x}=22 \%$ for the 1960s and $\gamma^{x}=28 \%$ for the 1970s.

As predicted by the simplified theoretical model (Proposition 4), the historical evolution of the cohort-level inheritance-labor income ratio $\gamma^{x}$ (Figure 13) is the mirror image of the pattern found for the cross-sectional inheritance flow-national income ratio $b_{y t}$ (Figure 9). There are two interesting differences, however.

First, the U-shaped pattern is less marked for $\gamma^{x}$ than for $b_{y t}$. At its lowest point, i.e. in the 1950s, the inheritance flow byt was less than $5 \%$ of national income. In comparison, the lowest point of $\gamma^{x}$, which was attained for cohorts born in the 1900s-1930s, is somewhat above $10 \%$. This is because all members of a given cohort do not inherit exactly at the same time. E.g. cohorts born in the 1900s-1930s inherited everywhere between the 1940s and 1970s. So when we compute cohort level averages of inheritance resources, we tend

[^30]to smooth cross-sectional evolutions of the inheritance flow-national income ratio. The cohort level pattern is nevertheless quite spectacular. Cohorts born in the $19^{\text {th }}$ century were used to receive by inheritance the equivalent of about $30 \%$ of their lifetime labor income. This figure suddenly fell to little more than $10 \%$ for cohorts born in the 1900s1930s, and it took several decades before returning to $19^{\text {th }}$ century levels. The point is that cohorts born in the 1900s-1930s (and to a lesser extent those born in the 1940s-1950s) had to rely mostly on themselves in order to accumulate wealth. Maybe it is not too surprising if they happen to be strong believers in lifecycle theory.

Next, it is striking to see that in our benchmark simulations $\hat{\alpha}^{x}$ and $\gamma^{x}$ attain approximately the same levels for cohorts born in the 1970s and after as for $19^{\text {th }}$ century cohorts ( $\hat{\alpha}^{x} \approx 20 \%-25 \%, \gamma^{x} \approx 30 \%$ ), in spite of the fact that we project $b_{y t}$ to stabilize below $19^{\text {th }}$ century levels ( $15 \%-16 \%$ instead of $20 \%-25 \%$ ). This is due to a differential tax effect. $\hat{\alpha}^{x}$ and $\gamma^{x}$ were computed from the simulated model, which uses observed after-tax resources, so these are effectively after-tax ratios. The aggregate labor income tax rate $\mathrm{T}_{\mathrm{L}}$ rose from less than $10 \%$ in the $19^{\text {th }}$ century-early $20^{\text {th }}$ century to about $30 \%$ in the late $20^{\text {th }}$ century-early $21^{\text {st }}$ century. ${ }^{82}$ The aggregate inheritance tax rate has remained relatively small throughout the $19^{\text {th }}-20^{\text {th }}$ centuries (about $5 \%$, with no trend). ${ }^{83}$ This mechanically raises the after-tax value of inheritance resources relatively to labor resources. Since modern fiscal systems tax labor much more heavily than inherited wealth, the inheritance flow-national income ratio does not need to be as large as during the $19^{\text {th }}$ century in order to generate the same share of inheritance in disposable lifetime resources. ${ }^{84}$

For illustrative purposes, we did the same computations with the growth slowdown-rising wealth returns scenario ( $\mathrm{g}=1.0 \%,\left(1-\mathrm{T}_{\mathrm{K}}\right) \mathrm{r}=5.0 \%$ ), under which $\mathrm{b}_{\mathrm{yt}}$ is projected to return to the $19^{\text {th }}$ century levels (see Figure 9). Because of the differential tax effect, we project that $\hat{a}^{\times}$will be about $25 \%-30 \%$ for cohorts born in the 1970s-1980s, and as large as $35 \%-40 \%$ for cohorts born in the 2010s-2020s, which corresponds to an inheritance-labor ratio $\gamma^{x}$ over $60 \% .^{85}$ That is, we project that cohorts born in the coming years will receive in inheritance the equivalent of over $60 \%$ of what they will receive in labor income during their entire lifetime, far above $19^{\text {th }}$ century levels (see Figure 13). This shows that taxes can have a strong impact on the balance between inheritance and labor resources.

[^31]
### 7.2. Labor-based vs inheritance-based inequality

Now that we have computed the inheritance share in average lifetime resources, we are in a position to put inequality back into the picture. Our objective is to illustrate that changes in aggregate ratios $\hat{\alpha}^{x}$ and $\gamma^{x}$ matter a great deal for the study of inequality. We do this by making simple assumptions about the intra-cohort distributions of labor income and inheritance, taken from the recent literature on top income and top wealth shares.

Our distributional assumptions are summarized on Table 3. The inequality of labor income has been relatively stable in France throughout the $20^{\text {th }}$ century. So we assume constant shares for the bottom $50 \%$, the middle $40 \%$, and the top $10 \%$ of the intra-cohort distribution of labor income for all cohorts born in 1820-2020. Wealth concentration has always been much larger than that of labor income. It was particularly high during the 1820-1913 period, when the top 10\% (the "upper class") owned over $90 \%$ of aggregate wealth, with little left for the middle $40 \%$ (the "middle class") and the bottom $50 \%$ (the "poor"). Basically, there was no middle class. Today, the poor still own less than $5 \%$ of aggregate wealth. But the middle class share rose from $5 \%$ to $35 \%$, while the upper class share dropped from $90 \%$ to $60 \%$. Wealth concentration declined mostly during the 19141945 period, and seems to have stabilized since the 1950s-1960s (as a first approximation). ${ }^{86}$ For simplicity, we apply 1910 inherited wealth shares by fractiles to all cohorts born in 1820-1870, we apply 2010 shares to all cohorts born in 1920-2020, and we assume linear changes in shares for cohorts born between 1870 and 1920.

By applying these assumptions to the lifetime inheritance-labor income resources ratio $\gamma^{x}$ plotted on Figure 13, we obtain the inequality indicators plotted on Figures 14-17. Consider first the ratio between the lifetime resources available for the top $50 \%$ successors and those available for the bottom $50 \%$ labor earners. Since the top $50 \%$ wealth share has been stable at $95 \%$, and the bottom $50 \%$ labor income share has been stable $30 \%$, this ratio follows exactly the same U-shaped pattern as the aggregate $\mathrm{r}^{\mathrm{x}}$, with levels multiplied by about three. In the $19^{\text {th }}$ century, the top $50 \%$ successors received in inheritance about $100 \%$ of what the bottom $50 \%$ labor earners received in labor income throughout their lifetime. Then this ratio dropped to $30 \%-40 \%$ for cohorts born in the 1900s-1930s. According to our computations, this ratio has now well recovered, and is be about $90 \%$ for cohorts born in the 1970s-1980s (see Figure 14).

Take again the example of the cohorts born in the 1970s. On average they will receive $440,000 €$ in inheritance. But the bottom half will receive almost no inheritance $(40,000 €)$, while the upper half will receive almost twice this amount $(840,000 €)$. This is roughly what

[^32]the bottom $50 \%$ labor earners will receive in labor income ( $950,000 €$ ). So we get the ratio of $88 \%$ plotted for the 1970s on Figure 14. On average, the bottom $50 \%$ labor earners earn little more than the minimum wage: their lifetime labor income roughly corresponds to the product of about $15,000 €$ by adult life length (about 60 years). For the sake of concreteness they can be thought of as minimum wage workers.

Consider now the ratios between what top $10 \%$ and top $1 \%$ successors receive in inheritance and what minimum wage workers receive in labor income. Due to the decline in wealth concentration, these inequality indicators are still lower for current generations than what they used to be in the $19^{\text {th }}$ century. But they are much higher than what they used for cohorts born in 1900-1940, in spite of the fact that intra cohort distributions have remained the same. This illustrates the importance of changes in the aggregate ratio $\gamma^{x}$.

For cohorts born between the 1900s and the 1950s, it was almost impossible to become rich through inheritance. Even if you belong to the top $10 \%$ or top $1 \%$ successors, or if you marry with such a person, the corresponding lifetime resources would be a lot smaller than those you can attain by making your way to the top $10 \%$ or top $1 \%$ of the labor income hierarchy of your time (see Figures 15-16). This is what most people would describe as a "meritocratic society". Material well-being required high labor income. For the first time maybe in history, it was difficult to live as well by simply receiving inheritance.

In the $19^{\text {th }}$ century, the world looked very different. Top $10 \%$ inheritance resources were roughly equivalent to top $10 \%$ labor resources. Top $1 \%$ inheritance resources were almost three times as large as top $1 \%$ labor resources. l.e. top rentiers vastly dominated top labor earners. If you want to attain high living standards in the $19^{\text {th }}$ century, then inheriting from your parents or your spouse's family is a much better strategy than work. This looks very much like a "rentier society".

Life opportunities open to today's generations are intermediate between the meritocratic society of the 1900-1950 cohorts and the rentier society of the $19^{\text {th }}$ century. For cohorts born in the 1970s, we find that the lifetime resources attained by the $1 \%$ successors and top $1 \%$ labor earners will be roughly equivalent. I.e. finding a top $1 \%$ job or a top $1 \%$ spouse will get you to the same living standards: you obtain about 10 millions $€$ in both cases (see Table 4). In the $19^{\text {th }}$ century, the spouse strategy was three times more profitable. For early $20^{\text {th }}$ century cohorts, the job strategy was twice more profitable.

The decline in wealth concentration makes it less likely to inherit sufficiently large amounts to sustain high living standards with zero labor income. But it makes it more likely - for a given aggregate inheritance-labor ratio $\gamma^{x}$ - to receive amounts which are not enough to be a rentier, but which still make a big difference in life, at least as compared to what most
people earn. Using standard Pareto assumptions on the shape of the intra cohort distribution of inherited wealth, we find that the cohort fraction inheriting more than minimum wage lifetime income (about $950,000 €$ for 1970 s cohorts) was less than $10 \%$ in the $19^{\text {th }}$ century, and will be as large as $12 \%-14 \%$ for cohorts born in the $1970 \mathrm{~s}-2000 \mathrm{~s}$. Among cohorts born in the 1900s-1930s, this almost never happened: only $2 \%-3 \%$ of each cohort inherited that much (see Figure 17).

We did the same computations under the low-growth, high-return scenario (see Figures 14-17). Unsurprisingly, given that we project the aggregate inheritance-labor ratio $\gamma^{x}$ to rise well above $19^{\text {th }}$ century values, we also find that our lifetime inequality indicators reach unheard of levels. At the top $1 \%$ level, the spouse strategy again becomes almost three times more profitable: the aggregate effect entirely compensates the distribution effect.

These computations should be viewed as illustrative and exploratory. They ought to be improved in many ways. First, progressive taxation of inheritance and labor income can obviously have a strong impact on such inequality indicators, both in the short run (mechanical effect) and in the long run (endogenous intra-cohort distribution effect). Here we ignored progressive taxes altogether. I.e. in our aggregate computations we simply assumed that inheritance and labor income taxes were purely proportional.

Next, we made no assumption about the individual-level rank correlation between the intra-cohort distributions of inheritance and labor income. Our inequality indicators hold for any joint distribution $G\left(\tilde{\mathrm{~b}}_{\mathrm{i}}{ }^{\mathrm{x}}, \tilde{\mathrm{y}}_{\mathrm{Li}}{ }^{\mathrm{x}}\right)$. In practice, $\operatorname{corr}\left(\tilde{\mathrm{b}}_{\mathrm{i}}{ }^{\mathrm{x}}, \tilde{\mathrm{y}}_{\mathrm{Li}}{ }^{\mathrm{x}}\right)$ might be endogenous. With publicly financed education and the lessening of credit constraints, one might expect the correlation to decline over time. But this could be counterbalanced by the fact that top heirs now need to work in order to reach the same relative living standards as in the past. So the correlation might have increased. It could also be that the moral value attached to work has risen somewhat, so that top successors work more than they used to. Or maybe they have always worked. We do not know of any evidence on this interesting issue.

Finally, we looked at a country with a relatively stable distribution of labor income. So for simplicity we assumed full stability, including at the top. In practice, the top $1 \%$ share actually rose a little bit in France in the late 1990s-early 2000s (from about 6\% to 7\%-8\% of aggregate labor income). This is too small a trend to make a significant difference so far. But if we were to make the same computations for the U.S., where the top $1 \%$ share rose from $6 \%-7 \%$ in the 1970 s to $15 \%-20 \%$ in the 2000 s, this would have strong and contradictory impacts on our inheritance-labor inequality indicators. The rise of the working rich reduces the inequality between top successors and top labor earners. But it increases the inequality between the working poor and successors as a whole. It also has dynamic effects on the future intra-cohort distributions of inherited wealth.

### 7.3. The share of inheritance in aggregate wealth accumulation

The inheritance flow-national income ratio $\mathrm{b}_{y t}=\mathrm{B}_{\mathrm{t}} / Y_{\mathrm{t}}$ analyzed in this paper is also closely related to the share of inheritance in aggregate wealth accumulation, which we note $\varphi_{\mathrm{t}}$.

There are two competing definitions of $\varphi_{t}$ in the economics literature. Modigliani (1986, 1988) define $\varphi_{t}{ }^{M}$ as the share of non-capitalized past bequests in total wealth, while Kotlikoff and Summers $(1981,1988)$ use the share of capitalized past bequests $\varphi_{t}{ }^{\text {KS }}$ :

$$
\begin{gather*}
\varphi_{t}^{M}=\hat{B}_{t} / W_{t} \text {, with: } \hat{B}_{t}=\int_{s \leq t} \quad B_{s t} d s  \tag{7.4}\\
\varphi_{t}{ }^{K s}=\widetilde{B}_{t} / W_{t} \text {, with: } \widetilde{B}_{t}=\int_{s \leq t}  \tag{7.5}\\
B_{s t} e^{r s t} d s
\end{gather*}
$$

With: $\mathrm{B}_{\text {st }}=$ aggregate bequests received at time s by individuals who are still alive at time t $r_{s t}=$ cumulated return to wealth between time $s$ and time $t$

Consider again the deterministic, stationary demographic structure introduced in section 5. Everybody becomes adult at age A, has one kid at age H , inherits at age I=D-H, and dies at age D. Each cohort size is normalized to 1 , so that total (adult) population $N_{t}$ is equal to life length D-A. Along a steady-state path with constant growth rate g, rate of return r , wealth-income ratio $\beta=W_{t} / Y_{t}$ and inheritance flow-income ratio $b_{y}=B_{t} / Y_{t}$, we have: ${ }^{87}$

$$
\begin{align*}
& \varphi_{t}^{M}=\int_{t-H \leq s \leq t} \frac{b_{y}}{\beta} e^{-g(t-s)} d s=\frac{b_{y}}{\beta} \frac{1-e^{-g H}}{g}  \tag{7.6}\\
& \varphi_{t}^{K s}=\int_{t-H \leq s \leq t} \frac{b_{y}}{\beta} e^{(r-g)(t-s)} d s=\frac{b_{y}}{\beta} \frac{e^{(r-g) H}-1}{r-g} \tag{7.7}
\end{align*}
$$

Proposition 5. Define $\varphi_{t}{ }^{M}$ the non-capitalized bequest share in aggregate wealth and $\varphi_{t}{ }^{\mathrm{Ks}}$ the capitalized bequest share. In steady-state: $\varphi^{M}=\frac{b_{y}}{\beta} \frac{1-e^{-g H}}{g}$ and $\varphi^{\mathrm{Ks}}=\frac{b_{y}}{\beta} \frac{e^{(r-g) H}-1}{r-g}$

Equations (7.6)-(7.7) are again pure accounting equations. They hold for any saving model. If we now apply them to the saving models analyzed in section 5 , then we just need to replace $b_{y}$ by the relevant steady-state value. So for instance in the class saving model or in the dynastic model, we have $b_{y}=\beta / H$. Therefore:

$$
\varphi^{M}=\frac{1-e^{-g H}}{g H} \text { and } \varphi^{K S}=\frac{e^{(r-g) H}-1}{(r-g) H}
$$

[^33]It immediately follows that ${ }_{\eta} \mathrm{g}>0, \varphi^{\mathrm{M}}<1$, and ${ }_{\eta} \mathrm{r}-\mathrm{g}>0, \varphi^{\mathrm{KS}}>1$.

Example: With $\mathrm{H}=30$, then $\varphi^{\mathrm{M}}=75 \%$ if $\mathrm{g}=2 \%$ and $\varphi^{\mathrm{M}}=52 \%$ if $\mathrm{g}=5 \%$.
If $\mathrm{r}-\mathrm{g}=3 \%$, then $\varphi^{\mathrm{KS}}=162 \%$. If $\mathrm{r}-\mathrm{g}=5 \%$, then $\varphi^{\mathrm{KS}}=232 \%$. $^{88}$

More generally, if steady-state $b_{y}$ is close to $\beta / H$, or not too much below, which as we saw in section 5 is generally the case with low growth and/or high returns, the same properties hold. That is, $\varphi^{\mathrm{M}}$ is structurally below $100 \%$, while $\varphi^{\mathrm{KS}}$ is structurally above $100 \%$.

The Modigliani definition $\varphi^{M}$ is particularly problematic, since it fails to recognize that inherited wealth produces flow returns. This mechanically leads to artificially low values for the inheritance share $\varphi^{\mathrm{M}}$ in aggregate wealth accumulation. It is particularly puzzling to see that $\varphi^{\mathrm{M}}$ can be equal to $75 \%$ or $52 \%$ in the class saving model - a model where by construction $100 \%$ of wealth comes from inheritance, and where successors are just consuming part of the return to their inheritance and saving the rest. As was pointed out by Blinder (1988), a Rockefeller with zero lifetime labor income would appear to be a lifecycle saver in Modigliani's definition, as long he does not consume the full return to his inherited wealth. In effect, Modigliani defines saving as labor income plus capital income minus consumption (and then defines lifecycle wealth as the capitalized value of past savings, and inherited wealth as aggregate wealth minus lifecycle wealth), while KotlikoffSummers define saving as labor income minus consumption. Given that the capital share is generally larger than the saving rate, this of course makes a big difference.

The Kotlikoff-Summers definition is conceptually more consistent. But in a way it suffers from the opposite drawback. For reasonable parameter values, $\varphi^{M}$ is bound to be larger than $100 \%$ (or close to $100 \%$ ). It is also extremely sensitive to the exact value of $\mathrm{r}-\mathrm{g}$.

By applying both definitions $\varphi_{t}{ }^{M}$ and $\varphi_{t}{ }^{\text {Ks }}$ (out-of-steady-state equations (7.4)-(7.5)) to our simulated model based upon two-century-long observed French data, we find the following results (see Figures 18-19). The uncapitalized inheritance share was about $80 \%$ of aggregate wealth during the $19^{\text {th }}$ century and until World War 1 . It then dropped to $50 \%-$ $60 \%$ in the 1930s-1950s, and to $40 \%$ in the 1960s-1980s. It is interesting to note that the historical nadir happens rather late for $\varphi_{t}{ }^{M}$ (in the 1970s), much later than the historical nadir for $b_{y t}$ (which occurred in the 1950s). This time lag simply stems from the fact that $\varphi_{t}{ }^{M}$ is based upon the cumulated value of byt of the previous decades. In the benchmark scenario, we find that $\varphi_{t}{ }^{M}$ will be above $60 \%$ in the 2010s and should stabilize above $70 \%$ after 2040. In the low-growth, high-return scenario, we find that $\varphi_{t}{ }^{M}$ stabilizes above $80 \%$ during the $21^{\text {st }}$ century - as in the $19^{\text {th }}$ century (see Figure 18).

[^34]When we capitalize past bequests, we find that $\varphi_{t}{ }^{\text {KS }}$ is always above $100 \%$, including during the low-inheritance postwar period, and that it is vey sensitive to r-g. In the $19^{\text {th }}$ century, $r$ was so large ( $5 \%-6 \%$ ) and $g$ so low (1\%) that we mechanically find extremly high $\varphi_{\mathrm{t}}{ }^{\mathrm{KS}}$ (as large as $450 \%$ in the $1870 \mathrm{~s}-1880 \mathrm{~s}$ ). ${ }^{89}$ The capitalized bequest share $\varphi_{\mathrm{t}}{ }^{\mathrm{KS}}$ was about $250 \%-300 \%$ around 1900-1910, then gradually dropped to about $150 \%$ in the 1960s-1980s. Again the nadir happens very late, due to the same time lags as above, and to the decennial variations in growth and asset returns (e.g. returns were low in the 1970s). In the benchmark scenario, we find that $\varphi_{t}{ }^{\text {KS }}$ stabilizes around $150 \%$ in the $21^{\text {st }}$ century, due to the relatively low projected r-g. In the low-growth, high-return scenario, we find that $\varphi_{t}{ }^{\text {M }}$ stabilizes above $250 \%-300 \%$ (the same level as in 1900-1910), due to the much larger r-g (see Figure 19).

We conclude from these computations that $\varphi_{t}{ }^{M}$ and $\varphi_{t}{ }^{K S}$ are fragile concepts. First, it is apparent from our French findings that the study of wealth accumulation and inheritance requires long term perspectives and adequate data sources. One should be careful when computing $\varphi_{t}{ }^{M}$ and $\varphi_{t}{ }^{K S}$ from one data point and steady-state assumptions. In the KSM controversy, both sides used single-data-point estimates of the U.S. inheritance flow $b_{y t}$, and applied steady-state formulas similar to equations (7.6)-(7.7) in order to compute $\varphi_{\mathrm{t}}{ }^{\mathrm{M}}$ and $\varphi_{t}{ }^{\text {KS }}$. Due to the limitations of U.S. estate tax data (which only covers the very top), they did not have direct measures of the fiscal inheritance flow. So they computed byt by using national wealth estimates and age-wealth profiles for year 1962 (using the 1962 Survey of consumer finances). Kotlikoff and Summers (1981) applied the capitalized definition, and found that $\varphi_{t}{ }^{\text {KS }}$ was about $80 \%$ (and possibly larger than $100 \%$ ) in the U.S. in the 1960s-1970s. By using essentially the same data, Modigliani (1986) concluded that $\varphi_{t}{ }^{\mathrm{M}}$ was as low as $20 \%-30 \%$ in the U.S. in the $1960 \mathrm{~s}-1970$ s. ${ }^{90}$ Using SCF data from the 1980s, Gale and Scholz (1994) found that $\varphi_{t}{ }^{M}$ was closer to $40 \% .{ }^{91}$

These U.S. estimates (say, $\varphi_{t}{ }^{\mathrm{N}} \approx 20 \%-40 \%, \varphi_{\mathrm{t}}{ }^{\mathrm{KS}} \approx 80 \%-100 \%$ ) are somewhat lower than our French estimates for the 1960s-1980s. It could well be that inheritance flows are indeed somewhat lower in the U.S., due to higher economic and (especially) demographic growth, and/or to the crowding out effect of funded pension wealth. However, U.S. estimates are based upon relatively fragile data, so it could also be that they understate true economic inheritance flows. In particular, they tend to rely on relatively low gift-bequest ratios $v_{t}$ (and sometime ignore gifts altogether) - a parameter which is hard to estimate in the absence of good fiscal data. This probably contributes to explain why the U.S. literature tends to

[^35]adopt relatively low inheritance flow-aggregate wealth ratios $b_{w t}$, typically as low as $1 \%$ $1.5 \%$, while we always find ratios above $2 \%$ in France. ${ }^{92}$

In any case, inheritance flows have probably changed a lot in the U.S. since the 1970s1980s. In order to settle the issue, it would be necessary to construct homogenous, yearly (or decennial) U.S. series on $\beta_{\mathrm{t}}, \mu_{\mathrm{t}}, \mathrm{b}_{\mathrm{wt}}$ and $\mathrm{b}_{\mathrm{yt}}$ up until the present day, as we have done for France. Given U.S. data limitations, one way to proceed would be to use the retrospective information on bequests and gifts available in SCF questionnaires. One needs however to find ways to adequately upgrade these self-reported bequest and gift flows, which in French wealth surveys appear to be far below fiscal flows. ${ }^{93}$

Next, and most importantly, even in a steady-state world with perfect data, none of the definitions $\varphi_{t}{ }^{M}$ and $\varphi_{t}{ }^{\text {KS }}$ would be really satisfactory. On the one hand, the Modigliani definition ignores the fact that inheritance produces flow returns, which amounts to assuming away the existence of rentiers (this should be part of the empirical demonstration, not of the assumptions). On the other hand, the Kotlikoff-Summers definition $\varphi_{\mathrm{t}}{ }^{\text {KS }}$ is mostly a measure of the magnitude of the capitalized resources available for consumption by successors. It does not really say anything about the relative importance of inherited vs self-made wealth. For instance, in case successors entirely consume their bequest the day they receive it, then $\varphi_{t}{ }^{\text {KS }}$ would still be far above $100 \%$, even though $0 \%$ of aggregate wealth belongs to successors, and $100 \%$ belongs to selfmade individuals who received zero bequest.

The problem with both definitions is that they are based upon a representative-agent approach. In practice, the wealth accumulation process always involves two different kinds of people and wealth trajectories. In every economy, there are inheritors or "rentiers" (people who typically consume part the return to their inherited wealth, and during the course of their lifetime consume more than their labor income), and there are savers or "self-made men" (people who do not inherit much but do accumulate wealth through labor income savings, so that their capitalized consumption is less than their capitalized labor income). A natural way to proceed would be to distinguish explicitly between these two

[^36]groups, and to define $\varphi_{\mathrm{t}}$ as the wealth share of the second group. The downside is that this definition is more data demanding. While $\varphi_{t}{ }^{M}$ and $\varphi_{t}{ }^{\text {KS }}$ can be computed using aggregate data, $\varphi_{t}$ requires micro level data on the joint distribution $H_{t}\left(W_{t i}, \tilde{b}_{t i}\right)$ of current wealth and capitalized inherited wealth.

## 8. Concluding comments

What have we learned from this paper? In our view, the main contribution of this paper is to demonstrate empirically and theoretically that there is nothing inherent in the structure of modern economic growth that should lead a long run decline of inherited (non-human) wealth relatively to labor income.

The fact that the "rise of human capital" is to a large extent an illusion should not come as a surprise to macroeconomists. With stable capital shares and wealth-income ratios, the simple arithmetic of growth and wealth accumulation is likely to operate pretty much in the same way in the future as it did in the past. In particular, the $r>g$ logic implies that past wealth and inheritance are bound to play a key role in the future.

As we have shown, there is no reason to expect demographic changes per se to lead to a decline in the relative importance of inheritance. Rising life expectancy implies that heirs inherit later in life. But this is compensated by the rise of inter vivos gifts, and by the fact that wealth also tends to get older in aging societies - so that heirs inherit bigger amounts.

Now, does this mean that the rise of human capital did not happen at all? No. It did happen, in the sense that human capital is what made long run productivity growth and self sustained economic growth possible. We know from the works of Solow and the modern endogenous growth literature that (non-human) capital accumulation alone cannot deliver self-sustained growth, and that human capital is what made $g>0$. The point, however, is that a world with $g$ positive but small (say, $g=1 \%-2 \%$ ) is not very different from a world with $\mathrm{g}=0 \%$.

If the world rates of productivity and demographic growth are small in the very long run (say, by 2050-2100), then the r>g logic implies that inheritance will eventually matter a lot pretty much everywhere - as it did in ancient societies. Past wealth will tend to dominate new wealth, and successors will tend to dominate labor income earners. This is less apocalyptic than Karl Marx: with $\mathrm{g}=0 \%$, the wealth-income ratio rises indefinitely, leading either to a rising capital share, or to a fall in the rate of return, and in any case to non sustainable economic and political outcomes. With $g>0$, at least we have a steady-state. But this is a rather gloom steady-state.

The main limitation of this paper is that we did not attempt to analyze socially optimal tax policy. We have seen in our simulations that $20^{\text {th }}$ century capital taxes, by reducing the differential between ( $1-\mathrm{T}_{\mathrm{K}}$ )r and g, can and did have a significant impact on the steadystate magnitude of inheritance flows, i.e. on the extent to which wealth perpetuates itself over time and across generations. In order to properly address these issues, one would need however to explicitly introduce inequality and normative concerns into the model, which we did not do in this paper, and which we plan to do in future research. We hope that our results will be useful for scholars interested in capital and inheritance taxation.

The other important - and closely related - limitation of this paper is that we constantly assumed a common rate of return $r$ on private wealth for all individuals. In the real world, the average $r$ is larger than $g$, but the effective $r$ varies enormously across individuals, over time and over assets. Available data and anecdotal evidence suggest that higher wealth individuals tend to get higher average returns (e.g. because of fixed costs in portfolio management, or risk aversion effects, or both). ${ }^{94}$ By assuming a common rate of return, we almost certainly underestimate the inheritance share and overestimate the labor share in capitalized lifetime resources - possibly by large amounts.

In some cases, inherited wealth might also require human skills and effort in order to deliver high returns. That is, it sometime takes labor input to get high capital income. If anything, the empirical relevance of the theoretical distinction between labor and capital income has probably increased over the development process, following the rise of financial intermediation and the separation of ownership and control. I.e. with perfect capital markets, any dull successor should be able to get a high return. But the hererogeneity and potential endogeneity of asset returns are important issues which should be taken into account in a unified positive and normative analysis of inheritance. This raises major conceptual and empirical challenges for future research.

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Figure 1: Annual inheritance flow as a fraction of national income, France 1820-2008


| Table 1: Accumulation of private wealth in France, 1820-2009 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Real growth <br> rate of <br> national <br> income | Real growth <br> rate of <br> private <br> wealth | Savings- <br> induced <br> wealth <br> growth rate <br> $g_{w s}=\mathrm{s} / \beta$ | Capital-gains- <br> induced wealth <br> growth rate | Memo: <br> Consumer <br> price inflation |
|  | g | $\mathrm{g}_{\mathrm{w}}$ | q | $p$ |  |
| $1820-2009$ | $1.8 \%$ | $1.8 \%$ | $2.1 \%$ | $-0.3 \%$ | $4.4 \%$ |
| $1820-1913$ | $1.0 \%$ | $1.3 \%$ | $1.4 \%$ | $-0.1 \%$ | $0.5 \%$ |
| $1913-2009$ | $2.6 \%$ | $2.4 \%$ | $2.9 \%$ | $-0.4 \%$ | $8.3 \%$ |
| $1913-1949$ | $1.3 \%$ | $-1.7 \%$ | $0.9 \%$ | $-2.6 \%$ | $13.9 \%$ |
| $1949-1979$ | $5.2 \%$ | $6.2 \%$ | $5.4 \%$ | $0.8 \%$ | $6.4 \%$ |
| $1979-2009$ | $1.7 \%$ | $3.8 \%$ | $2.8 \%$ | $1.0 \%$ | $3.6 \%$ |

Figure 2: Wealth-income ratio in France 1820-2008


Figure 3: Mortality rate in France, 1820-2100


Figure 4: The ratio between average wealth of decedents


Figure 5: Inheritance flow vs mortality rate in France, 1820-2008


Figure 6: Steady-state cross-sectional age-wealth profile in the class savings model ( $\left.s_{L}=0, s_{K}>0\right)$


Figure 7: Steady-state cross-sectional age-wealth profile in


Figure 8: Private savings rate in France 1820-2008


Figure 10: Labor \& capital shares in national income, France 1820-2008


Figure 9: Observed vs simulated inheritance flow $B / Y$, France 1820-2100


| Table 2: Rates of return vs growth rates in France, 1820-2009 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Growth rate of national income $\mathrm{g}$ | Rate of return on private wealth $r=\alpha / \beta$ | Capital tax rate $T_{K}$ | After-tax rate of return $\begin{gathered} r_{d}= \\ \left(1-T_{K}\right) \alpha / \beta \end{gathered}$ | Real rate of capital gains q | Rate of capital destruct. (wars) <br> d | After-tax real rate of return (incl. $k$ gains \& losses) $r_{d}=$ $\left(1-T_{k}\right) \alpha / \beta+$ $q+d$ |
| 1820-2009 | 1.8\% | 6.8\% | 19\% | 5.4\% | -0.1\% | -0.3\% | 5.0\% |
| 1820-1913 | 1.0\% | 5.9\% | 8\% | 5.4\% | -0.1\% | 0.0\% | 5.3\% |
| 1913-2009 | 2.6\% | 7.8\% | 31\% | 5.4\% | -0.1\% | -0.7\% | 4.6\% |
| 1913-1949 | 1.3\% | 7.9\% | 21\% | 6.4\% | -2.6\% | -2.0\% | 1.8\% |
| 1949-1979 | 5.2\% | 9.0\% | 34\% | 6.0\% | 0.8\% | 0.0\% | 6.8\% |
| 1979-2009 | 1.7\% | 6.9\% | 39\% | 4.3\% | 1.0\% | 0.0\% | 5.3\% |

Figure 11: Rate of return vs growth rate France 1820-1913


Figure 12: Capital share vs savings rate France 1820-1913


Figure 13: The share of inheritance in lifetime ressources received by cohorts born in 1820-2020


Figure 14: Top 50\% successors vs bottom 50\% labor income earners (cohorts born in 1820-2020)


Figure 15: Top 10\% successors vs top 10\% labor income earners (cohorts born in 1820-2020)


Figure 16: Top 1\% successors vs top 1\% labor income earners (cohorts born in 1820-2020)


Figure 17: Cohort fraction inheriting more than bottom 50\% lifetime labor resources (cohorts born in 1820-2020)


Table 3: Intra-cohort distributions of labor income and inheritance, France, 1910 vs 2010

| Shares in | Labor | Inherited wealth |  |
| :---: | :---: | :---: | :---: |
| inherited wealth | 1910-2010 | 1910 | 2010 |
| Top 10\% "Upper Class" | 30\% | 90\% | 60\% |
| incl. Top 1\% "Very Rich" | 6\% | 50\% | 25\% |
| incl. Other 9\% "Rich" | 24\% | 40\% | 35\% |
| Middle 40\% "Middle Class" | 40\% | 5\% | 35\% |
| Bottom 50\% "Poor" | 30\% | 5\% | 5\% |

Table 4: Lifetime inequality: illustration with cohorts born in the 1970s

| Lifetime |
| :---: |
| ressources |
| capitalized at age |
| 50 |


$3960000 €$

$1960000 €$


Figure 18: The share of non-capitalized inheritance in


Figure 19: The share of capitalized inheritance in



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    ** I am grateful to seminar participants at the Paris School of Economics, Universitat Pompeu Fabra (Barcelona), the Massachussetts Institute of Technology, Harvard University, New York University, Boston University and the University of Chicago for helpful reactions. All comments are welcome (piketty@ens.fr).

    This is an abridged version of the working paper (Piketty, 2010).
    The full-length version of this work, as well as a detailed data appendix, are available on-line at www.jourdan.ens.fr/piketty/inheritancel .

[^1]:    ${ }^{1}$ It is critical to include both bequests (wealth transmitted at death) and gifts (wealth transmitted inter vivos) in our definition of inheritance, first because gifts have always represented a large fraction of total wealth transmission, and next because this fraction has changed a lot over time. Throughout the paper, the words "inheritance" or "bequest" or "estate" will refer to the sum of bequests and gifts, unless otherwise noted.

[^2]:    ${ }^{2}$ Here we simply report raw wealth shares from the 2007 SCF (see Kennickell (2009, Table 4)), with no correction whatsoever. Kennickell later compares the top wealth levels reported in the SCF with other sources (such as Forbes 500 rankings), and finds that the SCF understates top wealth shares.
    ${ }^{3}$ See Piketty, Postel-Vinay and Rosenthal (2006).
    ${ }^{4}$ See e.g. Atkinson (1983, p.176, table 7.4) for U.K. top wealth shares broken down by age groups.

[^3]:    ${ }^{5}$ See section 3.2 below.

[^4]:    ${ }^{6}$ See Atkinson and Piketty $(2007,2010)$ for the complete set of country studies, and Atkinson, Piketty and Saez (2010) for a recent survey. To a large extent, this project is a simple extension of Kuznets (1953) pioneering and innovative work. Kuznets was the first researcher to combine income tax return data with national income accounts data in order to compute top income shares series, using U.S. data over the 19131948 period. In a way, what we do in the present paper is also following Kuznets: we attempt to integrate national income and wealth accounts with income and estate tax data.
    ${ }^{7}$ Partial corrections were made for a number of countries, but there was no systematic attempt to develop an imputation method. One should be aware of the fact that for most countries (including France, the U.K. and the U.S.), our series measure the share of top reported incomes (rather than top economic incomes).
    ${ }^{8}$ Wolff and Zacharias (2009) attempt to combine income and wealth data from the Survey of consumer finances (SCF) in order to obtain more comprehensive measures of top capital income flows in the US during the 1980s-1990s. As they rightly point out, it is not so much that the "working rich" have replaced "couponclipping rentiers", but rather that "the two groups now appear to co-habitate at the top end of the distribution".

[^5]:    ${ }^{9}$ See Kopczuk and Saez (2004) for the U.S., Piketty, Postel-Vinay and Rosenthal (2006) for France, and Roine and Waldenstrom (2009) for Sweden. These studies follow the pioneering work by Lampman (1962) and Atkinson and Harrison (1978), who respectively use U.S. 1922-1956 estate tax tabulations and U.K. 1923-1972 estate tax tabulations in order to compute top wealth share series.
    ${ }^{10}$ Given the relatively low quality of available wealth data for the recent period, especially regarding top global wealth holders, one should be modest and cautious about this conclusion.
    ${ }_{11}$ One exception is Edlund and Kopczuk (2009), who use the fraction of women in top estate brackets as a proxy for the relative importance of inherited vs self-made wealth. This is a relatively indirect way to study inheritance, however, and it ought to be supplemented by direct measures.
    ${ }^{12}$ E.g. Galor and Moav (2006) take as granted the "demise of capitalist class structure", but are not fully explicit about what they mean by this. It is unclear whether this is supposed to be an aggregate phenomenon (involving a general rise of labor income relatively to capital income and/or inheritance, as suggested by their informal discussion of the "rise in human capital") or a purely distributional phenomenon (involving a compression of the wealth distribution, for given aggregate wealth-income and inheritance-income ratios, as suggested by their theoretical model). De Long (2003) takes an explicitly long term perspective on inheritance and informally discusses the main effects at play. However his intuition according to which the rise of life expectancy per se should lead to a decline in the importance of inheritance relatively to labor income turns out to be wrong, as we show in this paper.

[^6]:    ${ }^{13}$ See e.g. Kessler and Masson (1989), Gale and Scholz (1994), Gokhale et al (2001).
    ${ }^{14}$ See e.g. Castaneda, Dias-Gimenes and Rios-Rull (2003), DeNardi (2004), Nirei and Souma (2007), Benhabib and Bisin (2009), Benhabib and Zhu (2009), Fiaschi and Marsili (2009) and Zhu (2010). See Cagetti and De Nardi (2008) for a recent survey of this literature.

[^7]:    ${ }^{15}$ For standard references on the "estate multiplier" formula, see Foville (1893), Colson (1903) and Levasseur (1907). The approach was also largely used by British economists (see e.g. Giffen (1878)), though less frequently than in France, probably because French estate tax data was more universal and easily accessible, while the British could use the income flow data from the schedular income tax system.
    ${ }^{16}$ See e.g. Colson (1927), Danysz (1934) and Fouquet (1982).
    ${ }^{17}$ See Mallet (1908), Séailles (1910), Strutt (1910), Mallet and Strutt (1915) and Stamp (1919). This other way to use estate tax data was followed by Lampan (1962), Atkinson and Harrison (1978), and more recent authors (see above). See also Shorrocks (1975).
    ${ }^{18}$ The accounting equation given in section 3 below ( $e_{t}=W_{t} / \mathrm{B}_{t}=1 / \mu_{t} \mathrm{~m}_{t}$ ) is of course identical to the mortality multiplier formula, except that we use it the other way around: we use it to compute inheritance flows from the wealth stock, while it has generally been used to compute the wealth of living from decedents' wealth.
    ${ }^{19}$ See e.g. Brumberg and Modigliani (1954), Ando and Modigliani (1963) and Modigliani (1986).

[^8]:    ${ }^{20}$ In 2008, French national income $Y_{t}$ was about 1,700 billions $€$, aggregate private wealth $W_{t}$ was about 9,500 billions $€$, and adult population was about 47 millions, so $y_{t} \approx 35,000 €$ and $w_{t} \approx 200,000 €$. The number of adult decedents was about 540,000 , so the mortality rate $m_{\mathrm{t}} \approx 1.2 \%$. Here we give round up numbers to simplify exposition. For $\mu_{\mathrm{t}}$ we actually report the gift-corrected ratio $\mu_{\mathrm{t}}{ }^{*}$ (see below), so "average inheritance per decedent" corresponds to "total bequests and gifts divided by number of decedents". For complete computations and exact values, see Appendix A, Table A2, line 2008.
    ${ }^{21}$ See section 7 below.
    ${ }^{22}$ All detailed demographic series and references are given in Appendix C.

[^9]:    ${ }^{23}$ Throughout the paper, "adult" means "20-year-old and over". In practice, children wealth is small but positive (parents sometime die early). In our estimates, we do take into account children wealth, i.e. we add a (small) correcting factor to the $\mu_{\mathrm{t}}$ ratio in order to correct for the fact that the share of adult wealth in total wealth (both among the deceased and among the living) is slightly smaller than $100 \%$. See Appendix B2.
    ${ }^{24}$ See Appendix B2. We use the mortality rates differentials broken down by wealth quartiles and age groups estimated by Attanasio and Hoynes (2000). If anything, we probably over-estimate differential mortality a little bit. Consequently, our resulting $\mu_{t}$ series and inheritance series are probably (slightly) under-estimated.
    ${ }^{25}$ The fact that we use estate tax data to compute our economic inheritance flow series does not affect the independence between the economic and fiscal series, because for the economic flow computation we only use the relative age-wealth profile observed in estate tax returns (not the absolute levels).
    ${ }^{26}$ Whether one starts from wealth-of-the-living or wealth-at-death raw age-wealth profiles, one needs to use differential mortality factors in one way or another in order to compute the $\mu_{\mathrm{t}}$ ratio.

[^10]:    ${ }^{28}$ All national accounts series, references and computations are described in a detailed manner in Appendix A. Here we simply present the main data sources and conceptual issues.
    ${ }^{29}$ In particular, the factor income decompositions (wages, profits, rents, business income, etc.) series released by Villa (1994) rely primarily on the original series constructed by Dugé de Bernonville (1933-1939), who described very precisely all his raw data sources and computations. For more detailed technical descriptions of the Dugé and Villa series, see Piketty (2001, pp.693-720).
    ${ }^{30}$ We used the $19^{\text {th }}$ century series due to Bourguignon and Lévy-Leboyer (1985) and Toutain (1987).

[^11]:    ${ }^{31}$ The concepts and methods used in Insee-Banque de France balance sheets are broadly similar to the flows-of-funds and tangible-assets series released by the U.S. Federal Reserve and Bureau of Commerce.
    ${ }^{32}$ More details on these issues are provided in Appendix A4.

[^12]:    ${ }^{33}$ For a more detailed technical analysis of the series, see Appendix A3 and A4.
    ${ }^{34}$ All "real" growth rates (either for national income or for private wealth) and "real" rates or return referred to in this paper are defined relatively to consumer price inflation. Any CPI mismeasurement would translate into similar changes for the various rates without affecting the differentials and the ratios.
    ${ }^{35}$ Net foreign assets gradually rose from about $2 \%$ of private wealth in 1820 to about $15 \%$ around 19001910, i.e. from about $10 \%$ of national income to about $100 \%$ of national income. See Appendix A, Table A16.

[^13]:    ${ }^{36}$ In the benchmark estimates reported on Table 1, private saving flows are defined as the sum of personal savings and net corporate retained earnings (our preferred definition). If we instead use personal saving flows, we find a lower $\mathrm{g}_{\mathrm{ws}}(2.0 \%)$ and a modest positive $q$ effect $(+0.4 \%)$. Taken literally, this would mean that asset prices are currently about $40 \%$ higher than what they were in 1913, but that if we deduct the cumulated value of corporate retained earnings, then they are actually $30 \%$ smaller. Within our accounting framework, retained earnings account for about a third of total real capital gains during the 1949-2009 period, which seems reasonable. For detailed results, see Appendix A5, Table A19, from which Table 1 is extracted.

[^14]:    ${ }^{37}$ Here we piece together the following data sources: for the late $19^{\text {th }}$ century and early $20^{\text {th }}$ century, we use the private wealth and national income estimates of the authors of the time (see e.g. Giffen (1878) and Bowley (1920)); for the period going from the 1920s to the 1970s, we use the series reported by Atkinson and Harrison (1978); for the 1990s-2000s we use the official personal wealth series released on hmrc.gov.uk. See also Solomou and Weale (1997, p.316), whose 1920-1995 UK wealth-income ratio series display a similar U-shaped pattern (from $600 \%$ in the interwar down to less than $400 \%$ in the 1950 s -1970s, up to $500 \%-600 \%$ in the $1980 \mathrm{~s}-1990 \mathrm{~s}$ ).
    ${ }^{38}$ Here we use for the post-1952 period the net worth series (household and non-profit sectors) released by the Federal Reserve (see e.g. Statistical Abstract of the U.S. 2010, Table 706), and for the pre-1952 period the personal wealth series computed by Kopczuk and Saez (2004, Table A) and Wolff (1989). .
    ${ }^{39}$ All estate tax series, references and computations are described in a detailed manner in Appendix B. Here we simply present the main data sources and conceptual issues.

[^15]:    ${ }^{40}$ This is reflected in the official name of the tax, which since 1791 has always been "droits d'enregistrement" (more specifically, "droits d'enregistrement sur les mutations à titre gratuity" (DMTG)), rather than "impôt sur les successions et les donations". In the U.S., the estate tax is simply called the "estate tax".
    ${ }^{41}$ See Appendix A, Table A9, col. (15). This low aggregate effective tax rate reflects the fact that top rates only apply to relatively high wealth levels (e.g. the top $40 \%$ marginal rate currently applies to per children, per parent bequests above 1.8 millions euros), and the fact that tax exempt assets and tax rebates for inter vivos gifts have become increasingly important over time. See Appendix B for more details.

[^16]:    ${ }^{42}$ See Piketty, Postel-Vinay and Rosenthal (2006).
    ${ }^{43}$ The spouse share has always been about $10 \%$ of the aggregate estate flow, vs. $70 \%$ for children and $20 \%$ for non-spouse, non-children heirs, typically siblings and nephews/nieces (see Appendix C2). It is unclear why one should exclude the spouse share and not the latter. In any case, this would make little difference.
    ${ }^{44}$ Gender-based wealth inequality is an important issue. On average, however, women have been almost as rich as men in France ever since the early $19^{\text {th }}$ century (with aggregate women-men wealth ratios usually in the $80 \%-90 \%$ range; this is largely due to the gender neutrality of the 1804 Civil Code; see Piketty et al (2006)). So the aggregate consequences of ignoring gender issues cannot be very large.

[^17]:    ${ }^{45}$ Parental transfers to non-adult children and educational investments raise complicated empirical and conceptual issues, however. One would need to look at the financing of education as a whole.

[^18]:    ${ }^{46}$ We know little as to why inter vivos gifts were so high in the early $19^{\text {th }}$ century. This seems to correspond to the fact that dowries (i.e. large inter-vivos gifts at the time of wedding) were more common at that time.
    ${ }^{47}$ See Piketty (2010, Table 2) and Appendix B2, Tables B3-B5 for detailed computations and results.
    ${ }^{48}$ See Piketty, Postel-Vinay and Rosenthal (2006).
    ${ }^{49}$ The differential-mortality-corrected profiles look even more hump-shaped (see Appendix B2).

[^19]:    ${ }^{50}$ Differential-mortality-corrected profiles are basically flat above age 50 (see Appendix B2). Using the 1998 and 2004 Insee wealth surveys, we find age-wealth profiles which are slightly declining after age 50 (the 70-to-79 and 80-to-89-year-old own about $90 \%$ of the 50 -to-59-year-old level). However this seems to be largely due to top-wealth under-reporting in surveys. Using wealth tax data (see Zucman (2008, p.68)), we find that the fraction of the 70 -to- 79 and 80 -to-89-year-old subject to the wealth tax (i.e. with wealth above 1 million $€$ ) is around $200 \%-250 \%$ of the corresponding fraction for the 50 -to- 59 -year-old (average taxpayers wealth is similar for all age groups). This steeply rising profile does not show up at all in wealth surveys, and might also be under-estimated in estate tax data (e.g. because the elderly hold more estate-tax-exempt assets).
    ${ }^{51}$ However the upward trend in gifts clearly started before new tax incentives were put in place in the late 1990s and 2000s, so it is hard to identify the the tax effect per se. For additional details, see Appendix B.

[^20]:    ${ }^{52}$ See Appendix C, Table C8. The slight decline in average age of heirs plotted on Figure 7 for the post-2040 period corresponds to another effect, namely a slight projected rise in average age at parenthood.
    ${ }^{53}$ According to on-line IRS data, the U.S. gift-bequest ratio is about $20 \%$ in 2008 ( 45 billions $\$$ in gifts and 230 billions $\$$ in bequests were reported to the IRS). Unfortunately, the bequest data relates to less than $2 \%$ of U.S. decedents (less than 40,000 decedents, out of a total of 2.5 millions), and we do not really know what fraction of gifts were actually reported to the IRS. On-line IRS tables also indicate steeply rising age-wealth-at-death profiles. This is consistent with the findings of Kopczuk (2007) and Kopczuk and Luton (2007).

[^21]:    ${ }^{54}$ In section 7 below, we translate these results expressed in cross-sectional macroeconomic flows into results expressed in longitudinal lifetime resources.
    ${ }^{55}$ If $A \leq a \leq 1-d$, then nobody has inherited, so $w_{t}(a)=0$. If $I-d \leq a \leq 1+d$, then a fraction $(a-l+d) / 2 d$ has already inherited, and for those individuals the growth and capitalization effects again cancel each other, so that $w_{t}(a)$ is a linear fraction of age: $w_{t}(a)=(a-l+d) \bar{w}_{t} / 2 d$. If $a \geq \mid+d$, then everybody has inherited, so the age-wealth profile is flat: $w_{t}(a)=\bar{w}_{t}$. Average wealth $w_{t}=\left[2 d \bar{w}_{t} / 2+(D-I-d) \bar{w}_{t}\right] /(D-A)=(D-I) \bar{w}_{t} /(D-A)$ remains the same as before, and so do all other results of proposition 2.

[^22]:    ${ }^{56}$ For $\mathrm{g}-\mathrm{s}_{\mathrm{K}} \mathrm{r}^{*}$ small, $\mu(\mathrm{g}) \approx \grave{\varphi}\left[1-\left(\mathrm{g}-\mathrm{s}_{\mathrm{K}} \mathrm{r}^{*}\right)(\mathrm{D}-\mathrm{A}-\mathrm{H}) / 2\right]$. See Piketty $(2010$, section 3$)$ and Appendix E .

[^23]:    ${ }^{57}$ See Appendix E, Figures E1-E2. For a given saving rate $s$, steady-state $\beta^{*}$ (and not only $\mu^{*}$ ) rises as g decreases, which also pushes towards higher $b_{y}{ }^{*}$. If $s \rightarrow 0$ as $g \rightarrow 0$, so as to keep $\beta^{*}=s / g$ and $r^{*}=\alpha / \beta^{*}$ constant, then in effect $\mathrm{g} / \mathrm{r}^{*} \rightarrow 0$ as $\mathrm{g} \rightarrow 0$, i.e. with low growth the capitalization effect is infinitely large as compared to the growth effect. The extreme case $g=0$ is indeterminate in the exogenous savings model: if $g=0$ and $s>0$, then as $t \rightarrow+\infty, \beta_{t} \rightarrow+\infty$ and $r_{t} \rightarrow 0$; if $g=0$ and $s=0$, then $\beta^{*}$ and $r^{*}$ are entirely determined by initial conditions; in both cases our key result still holds: $\mu_{\mathrm{t}} \rightarrow \boldsymbol{\mu}$ as $\mathrm{t} \rightarrow+\infty$.
    ${ }^{58}$ See Appendix E, Table E1 for detailed computations using formulas (5.6)-(5.7).
    ${ }^{59}$ Of course the other part of the explanation is that $\beta_{\mathrm{t}}$ was much smaller than $600 \%$ at that time. Here we report the findings obtained for $b_{y}{ }^{*}$ under the assumption of a fixed $\beta^{*}=600 \%$, so as to isolate the effect going through age-wealth profiles and the resulting $\mu^{*}$ ratio.

[^24]:    ${ }^{60}$ See Appendix E, Table E2 for detailed computations using the $\mu(\mathrm{g}, \mathrm{r})$ formula.
    ${ }^{61}$ See Piketty (2010, section 3) and Appendix E. Here we summarize the main results.
    62 The IES is typically thought to be relatively small (between 0.2 and 0.5 ), so $\sigma$ is typically $>1$. In the (unplausible) case where $\sigma<1$, in theory one could have $r^{*}<g$. However this would then violate the transversality condition, so this would not be a steady-state (the NPV of future income flows is infinite, and everybody would like to borrow infinite amounts against future resources, thereby pushing r upwards).
    63 The fact that the equilibrium, aggregate rate of return on assets $r^{*}(g)$ is always higher than $g$ and an increasing function of $g$ in standard models ( $r^{*}=\alpha g / s$ with exogenous savings, $r^{*}=\theta+\sigma g$ with dynastic savings) is well known to macroeconomists (see e.g. Baker et al (2005) for an application to pension projections).
    ${ }^{64}$ It is also well known that any wealth distribution such that the aggregate wealth-income ratio is equal to $\beta^{*}$ is a steady-state of the dynastic model. See e.g. Bertola et al (2006, chapter 3).
    ${ }^{65}$ The only difference with the exogenous saving model is that in case the age-labor income profile $\mathrm{y}_{\mathrm{Lt}}(\mathrm{a})$ is non-flat (say, because the pay-as-you-go pension system offers a replacement rate $\rho<1$ above some retirement age R), then utility maximizing agents will also accumulate lifecycle wealth, which in the dynastic entirely crowds out inherited wealth. However for plausible parameter values ( $\rho$ is about $70 \%-80 \%$ in France) we find that this crowd out effect is relatively small, and that $\mu(\mathrm{g}, \rho)$ is close to $\hat{\varphi}$. See working paper version.

[^25]:    ${ }^{66}$ See e.g. Dynan, Skinner and Zeldes (2002) for a calibrated model illustrating how plausible uncertainty about end of life health spendings can generate substantial savings and wealth accumulation
    ${ }^{67}$ See e.g. Carroll (2000), who argues that this wealth-loving model is the best explanation as to why saving rates increase so much with the level of lifetime income. See also Dynan et al (2004) and Kpoczuk (2007).
    ${ }^{68}$ See Kopczuk and Lupton (2007).
    ${ }^{69}$ The factor $\lambda$ corrects for the differences between the lifetime profile of labor income and inheritance flows, and is typically close to 1 . See section 7 below.
    ${ }^{70}$ See working paper (section 3) and Appendix E, Tables E5-E11 for detailed results.

[^26]:    ${ }^{71}$ E.g. according to Barro (2009, Table 1), the average real rate of return on stocks has been as large as $7.5 \%$ over the 1880-2005 period, vs. 1.0\% for bonds (averages over 11 Oecd countries).
    ${ }^{72}$ Thanks to linear savings, and because we focus on age-level averages, we do not need to assume that all individuals get the same return: we are just assuming that average returns are the same for all age groups.
    ${ }^{73}$ The full transition equations, and detailed simulation results, are given in Appendix D.
    ${ }^{74}$ See section 3.2 above and Appendix A5.

[^27]:    ${ }^{75}$ Using Insee household budget surveys for 1978, 1984, 1989, 1994, 2000 and 2006, one finds aggregate age-saving rates profiles that are rising somewhat until age 40-49, and almost flat above age 40-49: sligltly declining in 1978-1984-1989, flat in 1994-2000, slightly rising in 2006. In any case, these variations across age groups are always very small as compared to variations over permanent income quartiles. To the extent that wealth and capital income are adequately measured in such surveys, average savings rates also seem to vary little with respect to factor income shares. See Antonin (2009).
    ${ }^{76}$ Inheritance taxes are included, but have always been a small fraction of the total capital taxes, which mostly consist of flow taxes such as the corporate tax, personal capital income taxes, and housing taxes. See Appendix A, Tables A9-A11 for detailed series. There are approximate estimates, based on simplifying assumptions (especially regarding product taxes incidence). But the orders of magnitude seem to be right.

[^28]:    ${ }^{77}$ The capital share that has been approximately constant since the late 1980s, but is significantly larger than the level observed in the late 1970s-early 1980s.

[^29]:    ${ }_{79}^{78} \lambda=\left[e^{(r-g)(1-A)}-e^{(r-g)(l-D)}\right] /(r-g)(D-A)=1+(r-g)(2 l-A-D)$. With $I=(A+D) / 2$, the first-order term disappears.
    ${ }^{79}$ See Appendix E, Table E5 for illustrative computations using the $\lambda$ formula.

[^30]:    ${ }^{80}$ See Appendix D, Tables D7-D8 for detailed simulation results.
    ${ }^{81}$ See Appendix D, Table D7. Values are expressed in 2009 euros. As far as the shares are concerned, it is of course irrelevant at what age we capitalize lifetime resources (as long as we use the same age for inheritance and labor resources, and a common rate of return).

[^31]:    ${ }^{82}$ See Appendix A, Table A11, col.(11). Here we exclude pension-related payroll taxes from labor income taxes (otherwise the aggregate labor tax rate would exceed $50 \%$, see col.(9)). This follows from the fact that we treat pensions as replacement income, i.e. as part of (augmented) labor income.
    ${ }^{83}$ See Appendix A, Table A9, col.(15). Inheritance taxes were included in capital income flow taxes $\mathrm{T}_{\mathrm{K}}$, which can be questioned. Given their low level, however, a direct imputation method would not make a big difference to our $\alpha^{\alpha^{*}}$ and $\mathrm{y}^{\mathrm{x}}$ estimates. For a discussion of tax incidence issues, see Appendix A2.
    ${ }^{84}$ One might argue that the rise of taxes allowed for the rise of government services (e.g. education, health), and that this should be added to income. However these services are generally open to everybody, irrespective of whether one lives off labor income or inheritance. So as a first approximation $\alpha^{\alpha_{*}}$ and $\gamma^{x}$ appear to be consistent measures of the aggregate share of inheritance in disposable lifetime resources.
    ${ }^{85}$ See Appendix D, Table D8 for detailed simulation results.

[^32]:    ${ }^{86}$ For a detailed analysis of historical changes in wealth concentration in France, see Piketty et al (2006).

[^33]:    ${ }^{87}$ Alternatively one can replace $b_{y} / \beta$ by $b_{w}\left(=B_{t} / W_{t}\right)$ in equations (7.6)-(7.7).

[^34]:    ${ }^{88}$ See Appendix E, Table E12 for illustrative computations using these formulas.

[^35]:    ${ }^{89}$ See Appendix D5, Table D9 for detailed results.
    ${ }^{90}$ In addition to the estimate of the 1962 inheritance flow, both Kotlikoff-Summers and Modigliani used data on age-income and consumption profiles in the U.S. during the 1950s-1970s. Both sides were essentially applying different definitions to the same raw data (with a few differences, generally reinforcing each side). ${ }^{91}$ Using a 1975 French wealth survey, Kessler and Masson (1989) also find $\varphi_{t}{ }^{M}$ around $40 \%$.

[^36]:    ${ }^{92}$ E.g. Gokhale et al (2001) simulate the transmission of inequality via bequests by assuming inheritance flows around $6 \%$ of aggregate labor income and $1 \%$ of aggregate wealth, which seems very small to us. These flow ratios are taken from Auerbarch et al (1995, p.25). They are based upon relatively ancient agewealth profiles (taken from 1962 and 1983 SCF) and seem to wholly ignore inter vivos gifts.
    ${ }^{93}$ See Wolff (2002) for an attempt to use retrospective information on bequests and gifts reported in the 1989-1998 SCF (with no upward correction). We tried to use the retrospective questionnaires of the French wealth surveys conducted in 1992, 1998 and 2004, but found that self-reported bequest and gift flows were less than $50 \%$ of the fiscal flows (a lower bound of the true economic flows, given tax exempt assets). This is not due to imperfect recall: we also found this low ratio by comparing self-reported and fiscal flows for the past few years before each survey. We see no reason why reporting rates should be higher in similar wealth surveys in other countries, such as the SCF in the US. Reporting rates might also be biased, e.g. people who have consumed most of their inherited wealth might be particularly reluctant to report wealth transfers.

[^37]:    ${ }^{94}$ See e.g. Calvet, Campbell and Sodini (2009).

